



## Design and Construction of Concrete Overlay

**Course Number:** CE-02-111

**PDH:** 13

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9-2005

# Design and Construction Procedures for Concrete Overlay and Widening of Existing Pavements

James K. Cable  
*Iowa State University*

Fouad S. Fanous  
*Iowa State University*

Halil Ceylan  
*Iowa State University, hceylan@iastate.edu*

Douglas Wood  
*Iowa State University*

Daniel Frentress  
*Iowa State University*

*See next page for additional authors*

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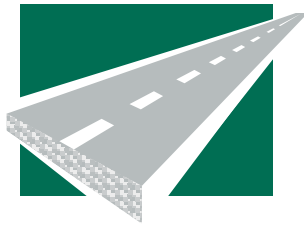
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## Recommended Citation

Cable, James K.; Fanous, Fouad S.; Ceylan, Halil; Wood, Douglas; Frentress, Daniel; Tabbert, Toni Raenette; Oh, Sun-Yoong; and Gopalakrishnan, Kasthurirangan, "Design and Construction Procedures for Concrete Overlay and Widening of Existing Pavements" (2005). *InTrans Project Reports*. Paper 54.

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C E N T E R F O R  
PORTLAND CEMENT CONCRETE  
PAVEMENT TECHNOLOGY

# Design and Construction Procedures for Concrete Overlay and Widening of Existing Pavements

Final Report  
September 2005

IOWA STATE UNIVERSITY

Sponsored by  
Federal Highway Administration (Project 6)  
and the Iowa Highway Research Board (Project TR-511)

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### Technical Report Documentation Page

<b>1. Report No.</b> FHWA DTFH61-01-X-00042 (Project 6) IHRB Project TR-511	<b>2. Government Accession No.</b>	<b>3. Recipient's Catalog No.</b>									
<b>4. Title and Subtitle</b> Design and Construction Procedures for Concrete Overlay and Widening of Existing Pavements		<b>5. Report Date</b> September 2005									
		<b>6. Performing Organization Code</b>									
<b>7. Author(s)</b> James K. Cable, Fouad S. Fanous, Halil Ceylan, Douglas Wood, Daniel Frentress, Toni Tabbert, Sun-Yoong Oh, Kasthurirangan Gopalakrishnan		<b>8. Performing Organization Report No.</b> CTRE Project 04-169									
<b>9. Performing Organization Name and Address</b> Center for Portland Cement Concrete Pavement Technology Iowa State University 2901 South Loop Drive, Suite 3100 Ames, IA 50010-8634		<b>10. Work Unit No. (TRAIS)</b>									
		<b>11. Contract or Grant No.</b>									
<b>12. Sponsoring Organization Name and Address</b> <table style="width: 100%; border: none;"> <tr> <td style="width: 50%;">Federal Highway Administration</td> <td style="width: 50%;">Iowa Highway Research Board</td> </tr> <tr> <td>U.S. Department of Transportation</td> <td>Iowa Department of Transportation</td> </tr> <tr> <td>400 7th Street SW, HIPT-20</td> <td>800 Lincoln Way</td> </tr> <tr> <td>Washington, DC 20590</td> <td>Ames, IA 50010</td> </tr> </table>		Federal Highway Administration	Iowa Highway Research Board	U.S. Department of Transportation	Iowa Department of Transportation	400 7th Street SW, HIPT-20	800 Lincoln Way	Washington, DC 20590	Ames, IA 50010	<b>13. Type of Report and Period Covered</b> Final report	
		Federal Highway Administration	Iowa Highway Research Board								
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400 7th Street SW, HIPT-20	800 Lincoln Way										
Washington, DC 20590	Ames, IA 50010										
		<b>14. Sponsoring Agency Code</b>									
<b>15. Supplementary Notes</b> Visit <a href="http://www.ctre.iastate.edu">www.ctre.iastate.edu</a> for color PDF files of this and other research reports.											
<b>16. Abstract</b>  <p>State Highway Departments and local street and road agencies are currently faced with aging highway systems and a need to extend the life of some of the pavements. The agency engineer should have the opportunity to explore the use of multiple surface types in the selection of a preferred rehabilitation strategy. This study was designed to look at the portland cement concrete overlay alternative and especially the design of overlays for existing composite (portland cement and asphaltic cement concrete) pavements.</p> <p>Existing design procedures for portland cement concrete overlays deal primarily with an existing asphaltic concrete pavement with an underlying granular base or stabilized base. This study reviewed those design methods and moved to the development of a design for overlays of composite pavements. It deals directly with existing portland cement concrete pavements that have been overlaid with successive asphaltic concrete overlays and are in need of another overlay due to poor performance of the existing surface.</p> <p>The results of this study provide the engineer with a way to use existing deflection technology coupled with materials testing and a combination of existing overlay design methods to determine the design thickness of the portland cement concrete overlay. The design methodology provides guidance for the engineer, from the evaluation of the existing pavement condition through the construction of the overlay. It also provides a structural analysis of various joint and widening patterns on the performance of such designs. This work provides the engineer with a portland cement concrete overlay solution to composite pavements or conventional asphaltic concrete pavements that are in need of surface rehabilitation.</p>											
<b>17. Key Words</b> asphaltic concrete overlays—pavement performance—portland cement concrete overlays—rehabilitation		<b>18. Distribution Statement</b> No restrictions.									
<b>19. Security Classification (of this report)</b> Unclassified.	<b>20. Security Classification (of this page)</b> Unclassified.	<b>21. No. of Pages</b> 150	<b>22. Price</b> NA								

# **DESIGN AND CONSTRUCTION PROCEDURES FOR CONCRETE OVERLAY AND WIDENING OF EXISTING PAVEMENTS**

**Final Report  
September 2005**

**Principal Investigator**

James K. Cable

Associate Professor

Department of Civil, Construction and Environmental Engineering, Iowa State University

**Co-Principal Investigators**

Fouad S. Fanous

Professor

Department of Civil, Construction and Environmental Engineering, Iowa State University

Halil Ceylan

Assistant Professor

Department of Civil, Construction and Environmental Engineering, Iowa State University

**Research Associates**

Douglas Wood, Daniel Frentress, Kasthurirangan Gopalakrishnan

**Research Assistants**

Toni Tabbert, Sun-Yoong Oh

Sponsored by  
the Federal Highway Administration (Project 6) and  
the Iowa Highway Research Board (Project TR-511)

Preparation of this report was financed in part  
through funds provided by the Iowa Department of Transportation  
through its research management agreement with the  
Center for Transportation Research and Education  
CTRE Project 04-169

**Center for Portland Cement Concrete Pavement Technology**

**Iowa State University**

2901 South Loop Drive, Suite 3100

Ames, IA 50010-8634

Phone: 515-294-8103

Fax: 515-294-0467

[www.pcccenter.iastate.edu](http://www.pcccenter.iastate.edu)

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## **ACKNOWLEDGMENTS**

The project research staff wants to thank Iowa DOT and Manchester Maintenance Garage staff for their support in the conduct of the field strain and pavement temperature testing. The traffic control equipment was essential to the installation and testing done for this project.

## **INTRODUCTION**

Iowa is currently one of the few states with two thin PCC overlay projects in place that are in excess of one mile in length. The first of these pavement overlays was placed in 1994 and has been used to investigate the optimum overlay for asphaltic concrete base pavements. The second pavement overlay was placed in 2002 and focused on additional investigation of the overlay depth and the impact of fibers and pavement widening on the pavement performance. These projects have proved that thin overlays are capable of becoming an alternative to asphaltic concrete overlays.

As a result of the previous work in Iowa, a need for a design manual for the engineer to use in the selection of pavement rehabilitation candidates for PCC widening and overlay projects was identified. This project was also envisioned to move the research results of the existing PCC overlay research in Iowa and nationally into an implementation mode.

This research also sought to answer some of the current issues in PCC overlay construction:

1. Selection criteria for implementation of successful PCC overlays, such as traffic needs, climate, underlying pavement condition, and depth of each pavement layer.
2. Traffic control requirements for various traffic volumes and mixes of vehicles.
3. Consideration of single lane paving techniques.
4. Design relationships:
  - a. Traffic volume and mix vs. overlay depth
  - b. Widening depth and width vs. structural enhancement of overlay
  - c. Structural evaluation of underlying pavement vs. overlay depth
  - d. Fiber contribution vs. overlay performance.
  - e. Need for widening tie bars, size, spacing, and method of placement.
5. Design and performance of the stress reliever layer materials, surface texture, and bonding capability.
6. Structural evaluation of the impact of the widening unit and the joint spacing of the overlay on the long-term performance of the pavement.

## **Objectives**

The objectives of this research focused on four areas:

1. Conduct of a structural analysis of the overlay and widening unit contributions to stress reductions and extended pavement life of the composite pavement.
2. Development of construction guidelines for construction of thin concrete overlays and widening units and a catalog of designs employed.
3. Development of an overlay design procedures for thin PCC overlays and widening units.
4. Validation of the structural analysis and design procedure with field load tests and strain measures for the various pavement layers of the existing two material/layer pavements.

## Research Plan

The research was carried out using the two Iowa PCC overlay projects as a basis for analysis of the performance of various design components. Those pavements included the Iowa Highway 21 (7.2 mile) section from U.S. Highway 6 north to Iowa Highway 212 and the Iowa Highway 13 project from Manchester north to the junction of Iowa Highway 3.

A finite element computer analysis coupled with field strain gage installation was used for the structural analysis. The details of the field installation and the results are shown in Part I of this report.

Individual parts of the project were subdivided into the following tasks:

### Task 1. Structural Analysis

1. Field evaluation and validation of strain measures in two existing overlay research pavements in Iowa to validate the current finite element results for the unbonded overlays.
2. Enhancement of previous structural analysis of the various overlay joint patterns and widening unit combinations of depth vs. width impact on the stress/strain imparted to the underlying pavement layers and life of the overlay.
3. Evaluation of the impact of the reinforcement ties between the widening unit and the overlay to include the following:
  - a. Slab sizes, including, but not limited to 2x2, 4x4, 4.5x4, 5x5, 5.5x5.5, 6x6, 9x9, 10x10, 11x11, 12x12, and 12x15 feet.
  - b. Overlay depths of 2, 3.5, 4, 4.5, and 6 inches.
  - c. Widening unit, varying in width from 1 ft. to 5 ft. in one-foot increments in conjunction with a constant depth of 8 inches.

### Task 2. Development of guidelines for the selection of candidate projects for PCC overlays

1. Structural and visual evaluation of the existing pavement layers.
2. Estimation of the future traffic needs.
3. Evaluation of traffic control needs during construction.

### Task 3. Development of draft design guidelines for the overlay and widening units

1. Design of depth and width to meet traffic needs and control.
2. Use of fibers and widening tie methods.
3. Design of widening units, overlay joint spacing, and widening connection to existing pavements.

### Task 4. Innovation

1. Consideration of new paving techniques to enhance pavement overlay construction and/or reduce traffic control problems during construction.

2. Consideration of new ways to introduce fibers into the mix.
3. Consideration of new joint forming methods to reduce construction time.
4. Consideration of design applications to bus loading areas and intersections or parking lots.

#### Task 5. Demonstration and validation

1. Development of a demonstration project or projects to illustrate the results of the research.
2. Validation of the results of the structural design enhancements with a field demonstration project.
3. Development of the project report and implementation presentations.
4. Evaluation of the resulting field demonstration project after one year.

The work was divided into two major areas of structural analysis and design process development. These are reported on in the same order in the following portions of the report.

## **PART I—ANALYTICAL STUDIES AND FIELD TESTING**

### **Background**

Resurfacing hot mix asphalt (HMA) pavements with thin Portland Cement Concrete (PCC) overlays, or “whitetopping” as it has come to be known, is a concept that dates back to 1918. This approach has seen a large increase in use in the past 15 years due to improved whitetopping technology and the success of several high-profile projects (NCHRP 2002). Whitetopping provides several advantages to the conventional resurfacing of pavements with HMA. It significantly reduces time and delays associated with pavement maintenance utilizing asphalt. PCC surfaces also have proven durability and long-term performance, which allows for longer life at lower life-cycle costs as compared to asphalt surfaces (Burnham and Rettner 2003).

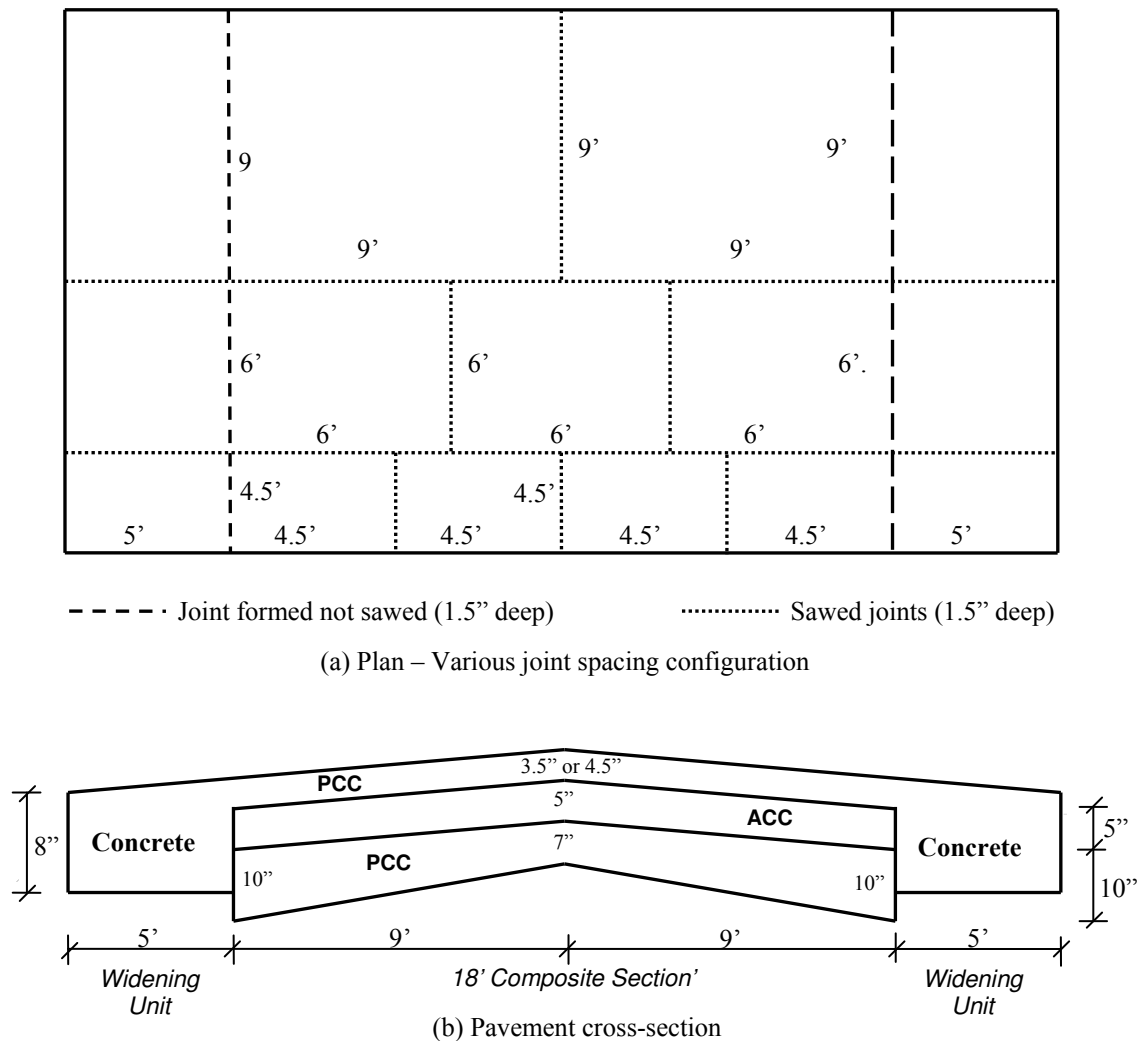
The state of Iowa is one of several states known for the large amount of PCC pavements. The original design life of the initial pavement systems was established as 20 years, and most of the systems had reached or exceeded the design life by the 1970s. These pavements were then continually resurfaced and possibly widened with asphalt cement concrete (ACC) to extend the life for another 10 to 15 years or until funding could be obtained to replace the pavements (Cable et al. 2003; Burnham and Rettner 2003). Due to the shorter design life and higher maintenance costs of asphalt pavements throughout that design life, whitetopping presents an attractive, lower cost alternative to continued pavement rehabilitation of asphalt surfaces.

In 1994, the Iowa Department of Transportation (Iowa DOT) initiated an ultra-thin whitetopping (UTW) project on a 7.2-mile segment of Iowa Highway 21 in Iowa County, near Belle Plaine, Iowa. The objective of that research was to investigate the interface bonding condition between an ultra-thin PCC overlay and an ACC base over time, with consideration given to the combination of different factors, such as ACC surface preparation, PCC thickness, the usage of synthetic fiber reinforcement, joint spacing, and joint sealing. That research continues to be one of the most referenced in demonstrating the applicability of whitetopping as a viable rehabilitation option.

In 2002, a follow-up project was initiated by Iowa DOT to investigate and verify the findings from the 1994 study (Cable et al. 2003). For this purpose, a 9.6-mile long stretch of Iowa Highway 13 (IA 13) that extends from Manchester, Iowa, to Iowa Highway 3 in Delaware County was selected as the test site. The pavement section consisted of a bottom PCC layer constructed in 1931 that was 18 ft wide, with a thickened edge that is 10" at the edges and 7" at the centerline of the roadway. The concrete pavement was used as the driving surface until subsequently overlaid with 2" of asphalt concrete in 1964 and with another asphalt concrete overlay of 3" in 1984.

Whitetopping was utilized in the summer of 2002 to rehabilitate the Iowa Highway 13 roadway and was applied considering the following variables: ACC surface preparation (milled, one-inch HMA stress relief course, and broomed only); use of fiber reinforcement in concrete (polypropylene, monofilament, proprietary structural, and no

fibers); joint spacing (4.5 x 4.5, 6 x 6, and 9 x 9-foot sections); and joint/crack preparation (bridge with concrete or #4 rebars stapled to the asphalt surface). The pavement section was also widened during the overlay operation to its current 24 ft width. The details of the construction were presented in a separate construction report presented by the Center for Portland Cement Concrete Pavement Technology at Iowa State University (Cable et al. 2003).



**Figure 1. Schematics of the composite pavement (not to scale)**

The construction report also included an analytical study utilizing the finite element method to predict the behavior of the composite pavement under truck loads. Several observations on the overall structural behavior of the pavement were made with regards to factors such as variation of soil subgrade reaction values, pavement cross-slope, and joint crack depth. The widening units were also found to be beneficial to pavement performance by reducing deflection and stresses. However, the state of bonding between



the layers, the different joint spacings, the effect of the rebars, and the effect of temperature variation were not part of the investigation (Cable et al. 2003).

The study presented herein is an extension of the initial analytical work presented in the construction report (Cable et al. 2003) and is focused on analytically investigating the factors that were not studied in the aforementioned analytical work.

## **Objectives**

The objectives of the study presented herein were as follows:

- Develop an analytical model for a finite element analysis that can accurately predict the response of the composite pavement on Iowa Highway 13
- Investigate the behavior of the pavement as whitetopping thickness, joint spacing, and depth of joint cracking was varied
- Examine the effects of bonding between the different layers on the overall structural behavior of the composite pavement
- Investigate the effects of the widening units on the deflection and stresses induced in the composite pavement when subjected to loading
- Determine the effects of bridging the pavement section and widening units with tie bars of different size and spacing
- Investigate the behavior of the pavement when subjected to different thermal conditions

## **Approach**

To achieve the aforementioned objectives, the following tasks were completed:

- Collection of information regarding the dimensions and other considerations about the pavement on Iowa Highway 13
- Determination of the appropriate types of elements for the finite element modeling of the composite pavement. This step required the following:
  - Verification of the suitability of interface elements to model the interaction between pavement layers
  - Comparison of the results obtained using a general purpose finite element model with those obtained using available specialized pavement analysis software, such as ISLAB2000
  - Determination of the appropriate mesh size for the finite element model to ensure accurate results are obtained
- Calibration of the analytical results with field test data on Iowa Highway 13.
  - Comparison of collected Falling Weight Deflectometer (FWD) test data to analysis results from pavement subjected to comparable load and ground conditions
  - Comparison of measured strain to strain results from the finite element analysis

- Analysis of the pavement model with the different design variables under consideration, which include the following:
  - Bonded and unbonded layers
  - Different joint spacing and crack depth
  - Different widening unit thickness and width
  - Different rebar bar size and spacing
- Investigation of the behavior of composite pavement under recorded temperature differentials

## **Literature Review**

### ***Analytical Studies***

Several analytical methods that range in degree of difficulty from using simple closed form solutions to complex finite element models may be utilized to investigate the performance of composite pavement structures. A three-dimensional (3-D) finite element model for the stress analysis of pavements with UTW was developed as part of a 1997 study of UTW overlays at the Ellaville Weigh Station on I-10 in northern Florida by the Florida DOT. The analysis was an attempt to understand the reason for the poor performance of the UTW sections constructed at the Ellaville Weight Station. The analysis showed that the UTW sections were found to have relatively higher stresses under critical loading conditions, which appeared to explain the poor performance and high incidences of cracked slabs. The 3-D model developed was also used to perform a parametric analysis to determine the effects that various UTW design variables have on performance, such as asphalt thickness, concrete thickness, asphalt and concrete moduli, and subgrade stiffness. The 3-D finite element model was limited by the simplifications of the material behavior to elastic material, full bonding between the layers, and no load transfer between adjacent slabs (thus providing an extreme worst case scenario). Despite these limitations, the project was a valuable demonstration of the applicability of using the finite element method to aid in investigating the performance of whitetopping.

In 1998, the Portland Cement Association (PCA) published a report detailing the development of a first generation design procedure for UTW. The report was based on a comprehensive study involving extensive field load testing, as well as the theoretical evaluation of UTW pavement behavior utilizing 3-D finite element analysis with the NISA II software package (Wu et al. 1998). Field test data was collected from three different sites: from a parking ramp rehabilitation project in the Spirit of St. Louis Airport, constructed in early 1995, and from two whitetopping test sections in Colorado that were instrumented and tested in 1996. Variables such as the slab thickness, joint spacing, joint condition, and asphalt surface preparation were considered in the study. In addition to the development of a rational design procedure for UTW, data collected from these projects have resulted in improved design and construction specifications of the UTW. Among the recommendations of the study were the installation of tie bars along the longitudinal construction joint and avoiding placing whitetopping overlay on top of a newly laid hot mix asphalt (HMA). Subsequent work has supported these findings, but emphasized that

the properties of the HMA, whether existing or new, be taken into account in the overlay design (NCHRP 2002).

Analytical work in the PCA study mentioned above also attempted to account for the load transfer between adjacent slabs, as well as the soil support using a system of unidirectional springs. Attempts at modeling the interface bond condition between layers utilizing point-to-point shear-friction gap elements were unsuccessful, and the investigative team subsequently utilized a system of springs to model the interface condition. A finite element program utilizing only shell elements to model pavements—commonly referred to as a 2-D model—was used to perform a parametric analysis, rather than the 3-D model that was developed, in the interests of reducing computational time. Results of the 2-D model were then converted into equivalent 3-D model results by using predictive equations developed from linear regression analysis of results from a control case. Results from the test sections in Colorado were also used in the development of design guidelines for whitetopping by CDOT (Tarr, Sheehan, and Okamoto 1998).

Based upon the premise that the structural design of UTW overlays requires precise predictions of loading stresses in the pavement system, a team of investigators from Tokyo, Japan, developed a 3-D finite element model that takes into account the viscoelastic behavior of asphalt and the interaction between the concrete overlay and asphalt subbase (Nishizawa, Murata, and Kokubun 2003). Analysis was performed on the program Pave3D, which was developed by one of the investigators for the analysis of pavement structures. Loading tests for both stationary and moving loads were conducted on an instrumented test pavement which was constructed in 1999 with two different joint spacings. The measured strains were compared with the computed strains from the finite element model for both stationary and moving loads. The comparison showed that the viscosity of the asphalt subbase and the interface conditions significantly affect the stress behavior of the pavement, affirming qualitative observations in the studies mentioned earlier from an analytical perspective. The study also demonstrated the applicability and advantage of more complex formulations of the finite element method in analyzing the unique behavior of whitetopped composite pavements. However, the report pointed out that precise prediction of stresses at high temperature conditions was still difficult using the 3-D model, even by incorporating viscoelasticity of the asphalt layer.

While attempts at modeling aspects of the more complex behavior of whitetopped pavements have been successful, much effort is still needed to develop a complete model that successfully predicts pavement behavior under a variety of design variables and conditions. However, in the author's opinion, the seemingly inexhaustible combinations of design variables and project specific considerations, not to mention limited resource availability, may well render this ultimate objective unreachable.

### ***Finite Element Modeling Techniques for Composite Pavements***

Two-dimensional finite element programs, such as ISLAB2000 (proprietary revision of ILSL2), J-SLAB, KenPAVE, and FEACONS, have been used in the analysis of pavement systems. These programs are based upon classical theories of analyzing thin plates (also known as medium-thick plates in pavement literature) on Winkler

foundations. They have been effectively used to analyze pavements with various slab sizes, different joint conditions, multiple layers, and with linear temperature differentials. However, these software packages do not allow users to model pavements with varying thickness or cross-slopes. Also, representing the configuration of pavements with widened sections would be difficult, if not impossible, when using 2-D finite element models to analyze such a structure; therefore, analysis of a composite pavement, such as the one found on Iowa Highway 13, requires the development of a 3-D model utilizing a general finite element program, such as ABAQUS, ADINA, or ANSYS. The analysis package ANSYS was selected for use in the work presented herein and is presented in detail in chapter “Modeling of Iowa Highway 13 Composite Pavement.”

### Modeling of Concrete and Asphalt Layers

Eight-node solid elements, also known as brick elements, can be used to model the concrete and asphalt layers of the composite pavement. Higher order solid elements, i.e., elements with a higher number of nodes, could also be utilized; however, employing higher order elements results in higher requirements for computational resources. To minimize the burden on computational resources and to maintain the accuracy of the finite element results, eight-node brick elements can be utilized by including “extra displacement functions” (Cook et al. 2002). These extra displacement functions are used to correct for the parasitic shear that results from the assumed displacement functions associated with the formulation of the eight-node solid element and allow the element to accurately represent the effects of bending in structures.

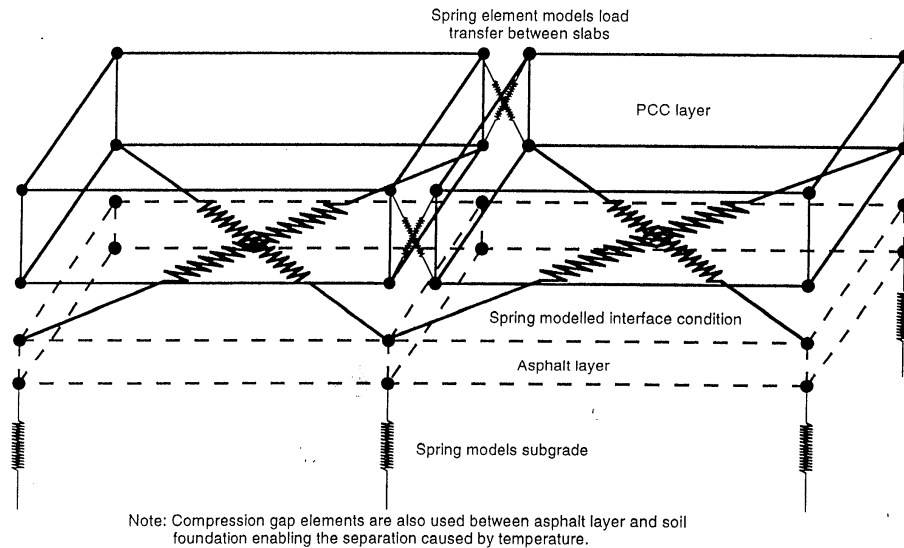
Kumara et al. utilized 20-node solid elements to model the UTW pavement layers in their Florida study (2003), whereas Wu et al. (1998) and Nishizawa et al. (2003) utilized the computationally economical eight-node solid element. In the work presented herein, eight-node solid elements with extra displacement functions were utilized in modeling the composite pavement on Iowa Highway 13.

### Interface Modeling Techniques

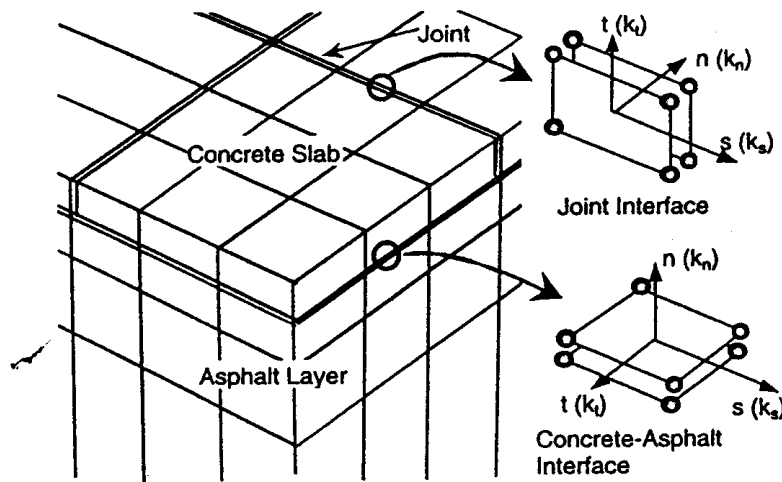
The effect of interface condition is of particular interest in investigating the behavior of the composite pavement, as previous studies have shown that it has a significant effect on the behavior of the whitetopping pavement system. In the analytical work leading to the development of the PCA design procedure for UTW, Wu et al. (1998) attempted to model the interface interaction with the use of non-linear shear-friction gap elements, which were 2-node or point-to-point interface elements that were available with the finite element analysis package NISA II. The element is capable of contact determination between the two layers: “open” or “closed” status. If the interface is “open,” no transfer of loads between the two surfaces occurs. If “closed,” the element resists normal and tangential forces through the use of three orthogonal springs with frictional capabilities in the horizontal direction. The element was capable of allowing sliding at locations where the shear forces exceeded the shear resistance, thereby simulating partial bonding of the pavement layers. Unfortunately, convergence problems in the resulting non-linear solution process forced the investigative team to abandon this approach and, instead, to

adopt a model that incorporated horizontal spring elements located at the interface of the concrete and asphalt layers. A bonded interface would be associated with very high values of the horizontal spring stiffness and an unbonded interface with very low values. Partially bonded conditions would then be modeled by moderate values of the spring stiffness, which were determined by a trial and error process. The final model adopted by Wu et al. is shown schematically in Figure 2.

Nishizawa et al. also utilized interface elements to model the interaction of concrete and asphalt layers and to model the load transfer at the joints, as shown in Figure 3 (Nishizawa, Murata, and Kokubun 2003). The interface element used by Nishizawa et al. in their study is similar to the shear-friction gap elements used by Wu et al.; however, instead of two-node elements, the interface elements in this study are surface-to-surface contact elements defined by four nodes on each surface. The element is also represented by three orthogonal springs, denoted by the stiffness  $k$  in each of the orthogonal  $t$ ,  $n$ , and  $s$  directions in Figure 3, but does not include friction capabilities. Modeling of the interface bond condition is performed by varying the tangential stiffness: high values for a bonded interface and low values for an unbonded interface. Only the bonded interface was considered during the analyses performed in this study, as the field load testing indicated that a strong bond existed between the asphalt and concrete layers. Low values for the spring stiffness were used to model the joint interfaces due to the joint gap. Similar interface element capabilities are available in the general purpose finite element program ANSYS (Kumara et al. 2003).



**Figure 2. 3-D finite element model (Wu et al. 1998)**



**Figure 3. Interface elements (Nishizawa et al. 2003)**

### Foundation Modeling Techniques

In the field of pavement analysis and design, three types of foundations can be assumed: liquid, solid, and layer, with liquid foundations being the most common, as the use of liquid foundations results in a matrix that requires very little time to solve (Huang 1993). A solid foundation is a more realistic representation of foundation behavior. Also known as a Boussinesq foundation, the deflection at any nodal point in a solid foundation depends not only upon the force at the node itself, but also upon the forces at all the other nodes. The stiffness of the foundation would be calculated using the Boussinesq equation (Huang 1993), which depends on the Poisson ratio and the elastic modulus of the foundation.

The layer foundation is known as a Burmister foundation, as Burmister's layered theory is used in the formulation of the flexibility matrix for the foundation. The layer foundation is similar to the solid foundation in that deflections at any nodal point also depend upon forces at other nodes. The formulation is much more complex, requiring multiple iterative integrations, and will not be discussed here.

Due to the wide availability of powerful processors and larger storage capacities, Huang recommended the usage of the more realistic solid foundation in lieu of liquid foundation (1993). The studies by Nishizawa et al. (2003) and Kumara et al. (2003) both utilized solid foundations in their 3-D finite element models. In their development of the UTW design procedures for Portland Cement Association (PCA) and Colorado Department of Transportation (CDOT), Wu et al. (1998) and Tarr et al. (1998) utilized the more conventional liquid foundation idealization. In the absence of actual properties of the soil found at the test site, analysis of the composite pavement on Iowa Highway 13 utilized the liquid foundation idealization. Investigation of the differences resulting from the utilization of different methods of foundation idealization is beyond the scope of this study.

## **Modeling of Iowa Highway 13 Composite Pavement**

### ***Modeling of Composite Pavement for Finite Element Analysis***

In order to obtain information on the effects of the different design variables for a composite pavement, a fairly complex model was needed. Models similar to those utilized by Nishikawa et al. (2003) and Ingram (2004) can be used. In the work presented herein, solid elements were used to construct the PCC base, asphalt, and whitetopping layers. Surface-to-surface interface elements were used at the interfaces between layers and between joints in the whitetopping. In addition, beam elements were used to model the tie bars in the pavement when applicable.

The effect of the soil beneath the composite pavement was modeled using a Winkler foundation. With this idealization, nodal springs with the appropriate values of stiffness equivalent to the desired soil subgrade modulus are typically utilized. The ANSYS program allows users to define a Winkler foundation without having to define individual nodal springs when using plate elements; thus, a thin layer of plate elements coinciding with the bottom surface of the solid elements of the bottom PCC layer was employed to represent the effect of the Winkler foundation. This is not a new methodology, and it was used extensively by Ingram (2004) in her study of the performance of different tie bar shapes in PCC pavements and also in the initial analysis of the composite pavement on Iowa Highway 30 prior to this study (Cable et al. 2003).

### **Types of Elements Used to Model the Composite Pavement**

The following is a brief description of the elements that were used in modeling and analyzing the composite pavement on Iowa Highway 13.

#### **Solid Elements**

SOLID45 is an 8-node brick element used for the 3-D modeling of the different layers in the composite pavement. The element has 3 degrees of freedom at each node: translations in the nodal x, y, and z axes. Additionally, the element is capable of representing orthotropic material properties, and has plasticity, creep, swelling, stress stiffening, large deflection, and large strain capabilities. The element is capable of supporting concentrated forces at the nodes, pressures on any surface, and temperature differentials across the body of the element.

As the element has only 2 nodes on each edge, the resulting interpolation functions for the element are linear. Consequently, analysis involving the basic 8-node element would yield constant strains and stresses across the element, which is inaccurate to account for bending effects. Higher order elements which involve additional nodes on each edge of the element would allow for the variation of stresses and strains across the element. Unfortunately, higher order elements would also require increased computing time during the analysis. The alternative to higher order elements would be to include extra shape

functions in the element stiffness formulation (Cook et al. 2002). ANSYS provides such an option when using SOLID45.

### Plate Elements

SHELL63 is an element with both bending and membrane capabilities, with in-plane and normal loads permitted. The element is defined by 4 nodes, with six degrees of freedom at each node, incorporating translations and rotations in each of the orthogonal directions. Orthotropic material properties are permitted, and the element allows for a smoothly varying thickness across the element. An Elastic Foundation Stiffness (EFS) can be defined, which is equivalent to the soil subgrade modulus associated with a Winkler foundation. This allows for a convenient method for idealizing a liquid foundation in the pavement model that is less time consuming than defining individual nodal springs.

As solid elements do not have EFS capabilities, a very thin layer of plate elements was placed beneath the pavement structure to include the foundation effects without artificially increasing the stiffness of the pavement structure. Similar to the brick element, concentrated forces, pressures, and temperature differentials may be applied to the element.

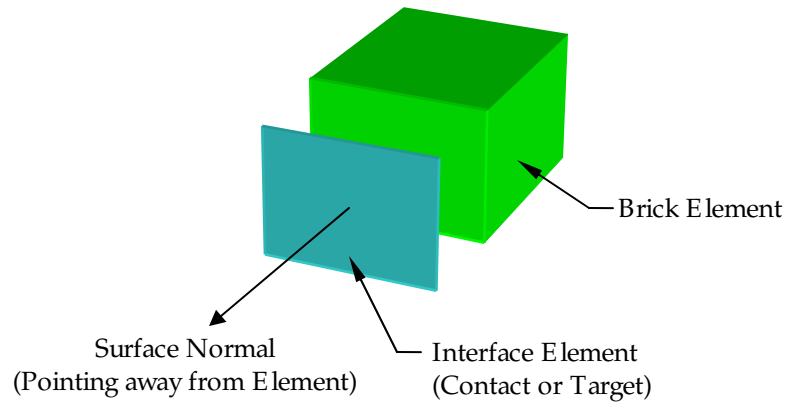
### Beam Elements

A 3-D beam element, BEAM4, was selected to model the tie bars that were placed along the edge of the pavement and the widening unit. The element has tension, compression, bending, and torsion capabilities. The cross-sectional area, area moments of inertia, torsional moment of inertia, and thicknesses in two directions may be specified. The element may also be defined with an initial strain if necessary. Once again, the element is capable of supporting forces, pressures, and temperature differentials.

### Interface Elements

ANSYS provides several elements that can be utilized to model the interface between two elements that are in contact. Contact between two surfaces can conveniently be modeled in ANSYS by utilizing the surface-to-surface contact elements TARGE170 and CONTA174. Each of these “contact pairs” is capable of representing contact and sliding between two 3-D surfaces, with the “target” elements (TARGE170) defining the stiffer surface, and “contact” elements (CONTA174) defining the deformable surface (see Figure 4). If both surfaces are of equal stiffness, either may be designated as the target or contact. The elements are superimposed on the surfaces of solid or shell elements that make up the interface and have the same geometry and node ordering as the underlying elements. It is of utmost importance that the contact and target surface normals, as defined by the right-hand rule going around the nodes of the element, i.e., counterclockwise around the nodes of the interface element, always point away from the element.





**Figure 4. Orientation of interface element**

The status of contact pairs could either be “closed,” i.e., in contact, or “open,” i.e., not in contact and no load transfer between the two surfaces takes place. Interface elements introduce geometric nonlinearity in the solution process, resulting in increased computing time. Consequently, iterative solutions must be repeated until the status of each interface does not change, while at the same time satisfying the force and displacement convergence criteria and ensuring that penetration between the surfaces stays within acceptable tolerances.

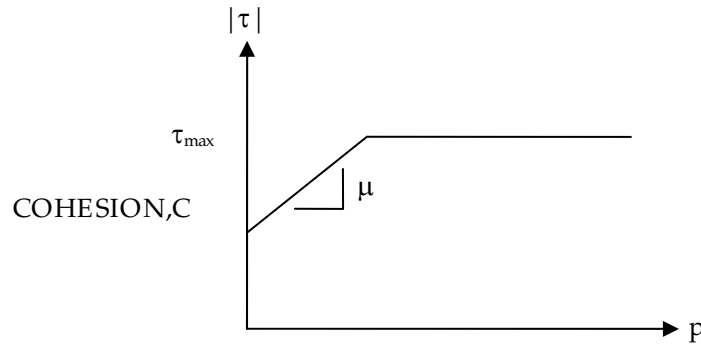
The mechanics of the contact pair involve normal and tangential contact stiffnesses. The normal contact stiffness governs the amount of penetration between the two surfaces. ANSYS estimates the normal contact stiffness based upon the material properties of the underlying elements; however, the stiffness can be adjusted by the user if necessary. Using a larger contact stiffness, while beneficial in reducing penetration, could result in convergence difficulties. Alternatively, a contact stiffness that is too low would allow too much penetration and render the results inaccurate.

The tangential stiffness governs the sliding of the contact surfaces with respect to one another and is automatically defined by ANSYS to be proportional to the coefficient of friction and the contact stiffness. The friction model adopted by ANSYS is based upon Coulomb friction, where sliding occurs when the shear stress exceeds the sliding resistance,  $\tau$ , which is expressed as follows:

$$\tau = \mu p + c ;$$

where  $\mu$  is the coefficient of friction,  $c$  is the cohesion sliding resistance between the two layers, and  $p$  is the normal contact pressure. A maximum contact shear stress,  $\tau_{\max}$ , may also be defined so that no matter what is the magnitude of the contact pressure, sliding will occur if the maximum contact shear stress is exceeded. This is illustrated schematically in Figure 5. The element also supports different values of static and

dynamic friction. A similar model is not provided for the normal direction, whereby cohesion in the normal direction can be specified.



**Figure 5. Friction model**

As bond strength information from the composite pavement on Iowa Highway 13 was available (Cable et al. 2003), this friction model could potentially allow for a more precise prediction of the pavement bond behavior by taking into account both friction between the layers and bond strength in the form of cohesion. However, this avenue of study was not pursued due to the uncertainty associated with the partial bonding mechanism, which could result from methods of construction, temperature differentials, and actual properties of the materials used in constructing the pavement structure. In addition, the model would only be able to detect instances of layer unbonding due to the loading used in the analysis, and is thus useful only when analyzing newly constructed composite pavements under controlled conditions. Bond strength information in the direction normal to the interfaces was also not available, which would render a study of the interface behavior incomplete; hence, this study was focused upon the behavior of the pavement at two extremes, i.e., fully bonded and unbonded layers.

The interface elements also provide the user with the option of pre-selecting surface interaction models for specific cases. The interface models are listed as follows:

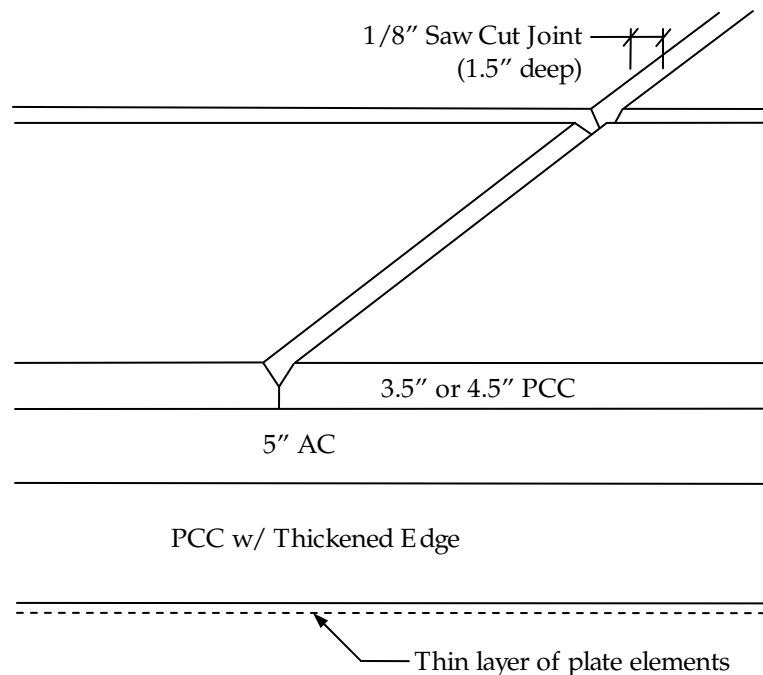
- “Standard” contact imposes no limits upon the behavior of the interface, and the interface elements are free to slide or separate as the situation warrants.
- “Rough” contact models perfectly rough contact and the input value of  $\mu$  is ignored, although separation is allowed.
- “No separation” contact allows sliding of the surfaces relative to one another, but does not allow the surfaces to “open.”
- “Bonded” contact bonds the contact and target surfaces in all directions.

The features listed above are user-friendly for modeling different cases of surface interaction without having to manually change interface spring stiffness values as was done in previous studies (Wu et al. 1998; Nishizawa, Murata, and Kokubun 2003). In this work, the “bonded” model was used for investigating the behavior of the composite

pavement when a strong bond exists in all layers. “Standard” or “no separation” was also used for unbonded layers, depending upon whether separation between the surfaces was expected.

### Finite Element Modeling of Composite Pavement on Iowa Highway 13

A portion of the Iowa Highway 13 pavement was modeled for the finite element analysis utilizing the elements presented in the preceding section. The model length was 72 ft, and the cross-section was as shown in Figure 1. The length of the model was selected to ensure that at least one truck load could be placed on the pavement. The length of 72 ft also allowed the modeling of the joint configurations under consideration, i.e., 4.5 x 4.5 ft, 6 x 6 ft, and 9 x 9 ft, such that the panel edges coincided with the model boundaries.

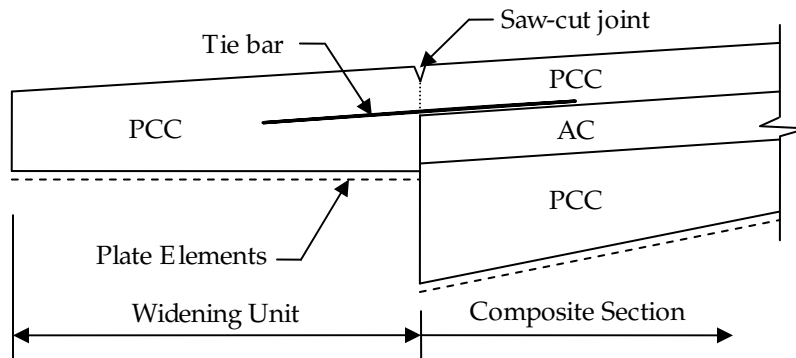


**Figure 6. Finite element model details (not to scale)**

As described previously, the top PCC (whitetopping), AC, and bottom PCC layers were meshed with solid brick elements. To model the soil beneath the pavement, a very thin layer of plate elements was placed beneath the bottom PCC layer, as well as beneath the widening units on both sides of the pavement. The whitetopping and AC layers were modeled with two layers of solid elements through the thickness, while the bottom PCC layer was modeled with three layers of solid elements. Interface elements were placed in between the layers, i.e., at the PCC-ACC interface, and at the ACC-whitetopping interface, so that the effects of interface bonding and unbonding could be studied. A similar approach was utilized to model the interface between PCC widening units and the original pavement structure, i.e., the two edges along lines 1-1 and 2-2 (Figure 8).

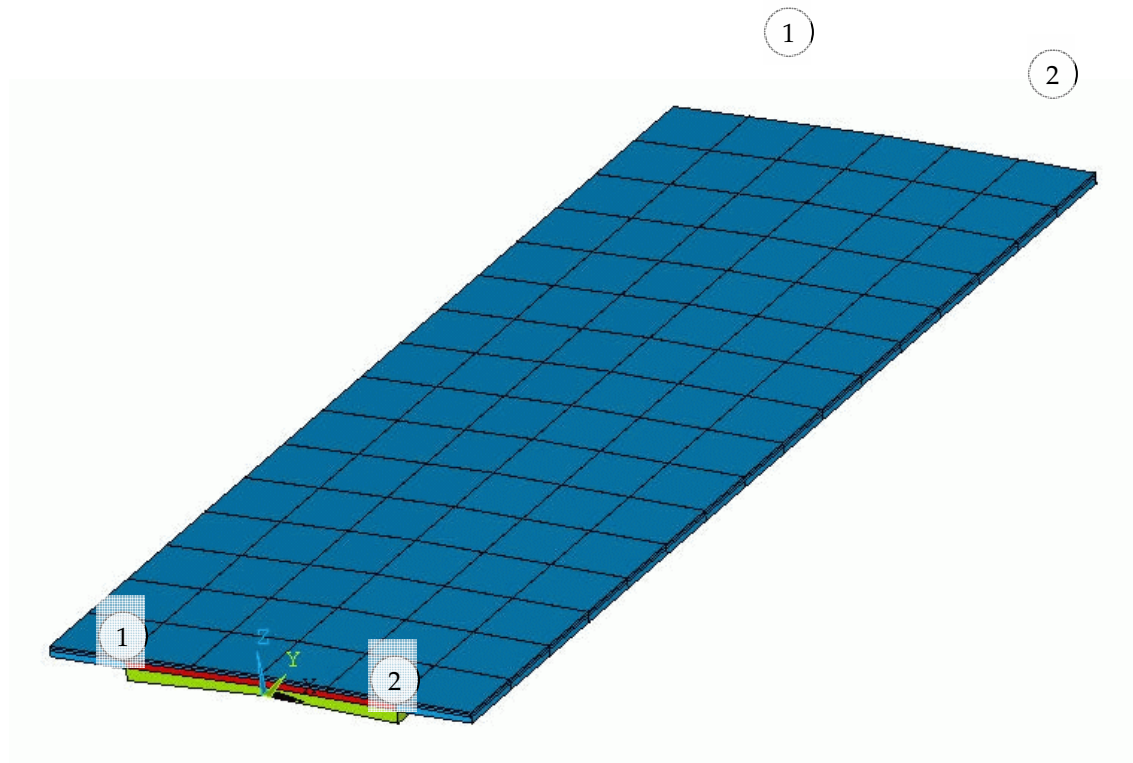
Saw-cut joints were modeled as V-cuts that were 1/8 in. wide at the whitetopping surface, with a depth of 1.5 in, as shown in Figure 6, per the construction report (Cable et al. 2003). The joint cracks in the model were analyzed with 1.5 in. depth, and with the cracks extending through the thickness of the whitetopping. Apart from the saw-cut joints, the ACC and PCC layers were assumed to be crack-free. Interface elements were utilized between the joints according to the crack depth being studied.

Each tie bar was modeled with several beam elements that were connected together to form a single tie bar. This method allows the collection of information about bending stresses, elastic strains, shear forces, and moments along the length of the tie bar.



**Figure 7. Location of tie bars (not to scale)**

Figure 8 shows a model that was constructed for the analysis of the composite pavement on Iowa Highway 13, having a whitetopping thickness of 3.5 in and joint spacing of 4.5 x 4.5 ft. A total of six models were developed to cover the range of different joint spacings and the two whitetopping thicknesses. Modifications were made to these base models when necessary to study the effects of tie bar placement and widening unit configurations.



**Figure 8. Sample composite pavement model**

### ***Verification of ANSYS Model***

Prior to the analysis of the composite pavement on Iowa Highway 13, steps were taken to verify the applicability of the elements and the modeling techniques chosen for the analysis of the composite pavement. A series of simple problems were devised, and the deflection and stress results from finite element analyses were compared with known solutions. This was accomplished by analyzing a simply supported composite beam, a plate on an elastic foundation. Shell (plate) or solid (brick) elements, as well as interface elements were used in modeling these structures for the finite element analysis. The layers forming these structures were considered to be either fully-bonded or unbonded. Analyses of the structures were performed using different element sizes for both finite element programs to aid in the selection of an appropriate mesh size for the Iowa Highway 13 composite pavement model. The results were compared to the results obtained from analyzing these two problems using the ISLAB2000 software and the published results by Voyiadjis and Kattan (1990). Complete details for these comparisons are documented by Sun-Yoong (2005).

The close agreement of the results from the ANSYS model with the theoretical results by Voyiadjis and Kattan (1990) validates the modeling techniques used in this analysis. In addition, the results showed that for the ANSYS and ISLAB2000 programs, variations in the stresses were converging as the element sizes were reduced. The differences in the results could be due to difference in the formulation of the stiffness of the shell element

used in ISLAB2000 and the solid element in ANSYS. These two comparisons also show that the size of the elements to be used in the composite pavement analysis should be limited to a size of 6" x 6" or smaller to obtain accurate results. However, one must expect that using smaller size elements will require larger computation time. In this work, element size was limited to 6" x 6".

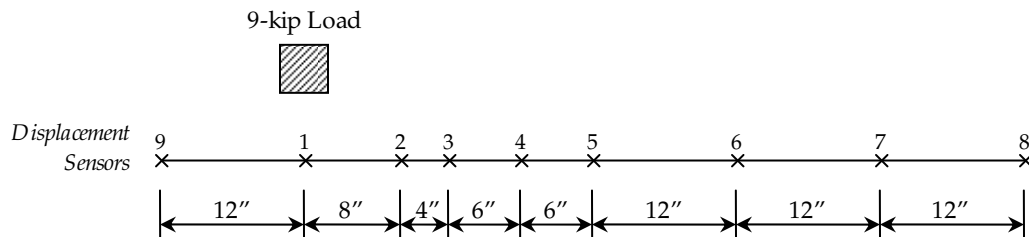
## Field Investigation of Iowa Highway 13 Composite Pavement

In order to determine the applicability of utilizing the finite element method to analyze the composite pavement on Iowa Highway 13, field testing of the pavement was carried out. In addition, since soil data was unavailable, it was necessary to determine a representative value suitable for the soil subgrade reaction modulus,  $k_s$ . This was accomplished by comparing the measured deflection results with analytical results that were obtained using different values for the soil subgrade. Next, the pavement model was analyzed with the selected value of  $k_s$  to determine the computed strains at the gage locations, which were compared to the measured strains obtained from field testing.

### Field Test

#### Collection of Deflection Data

Deflection data from the composite pavement was obtained using Falling Weight Deflectometer (FWD) testing, which has been widely used in pavement research. FWD testing was performed a total of five times from May 2002 to May 2004 at various locations along the 9.6-mile test site on Iowa Highway 13. Two of the five tests had been performed prior to overlaying and widening of the original pavement with PCC. Details of the testing procedure, testing equipment, and test locations were documented in the construction report (Cable et al. 2003). Figure 9 is a schematic showing the arrangement of the sensors on the FWD test equipment used on this project.



**Figure 9. Schematic of FWD deflection sensors**

The test locations along Iowa Highway 13 were kept constant throughout the different test dates, and were selected such that all pavement sections constructed with different combinations of the design variables were included in the testing program. The maximum deflections (corresponding to sensor no. 1) presented in Tables 1 and 2 are the average values of several deflection readings gathered from the field test. These are tabulated according to surface preparation, joint spacing, and type of fiber used in the overlay. Detailed test data was documented in the construction report (Cable et al. 2003).

**Table 1. Breakdown of maximum deflection data from FWD test: 3.5" whitetopping pavement**

	Max Deflection (in)								
	Scarify			HMA Stress Relief			Patch		
Fiber Type	4.5 x 4.5	6 x 6	9 x 9	4.5 x 4.5	6 x 6	9 x 9	4.5 x 4.5	6 x 6	9 x 9
No Fibers	0.00412	0.00495	n/a	0.00520	0.00369	n/a	0.00595	0.00518	n/a
Fiber Type A	n/a	n/a	n/a	0.00452	0.00526	n/a	0.00568	0.00641	n/a
Fiber Type B	0.00556	0.00442	n/a	0.00500	0.00433	n/a	0.00445	0.00531	n/a
Fiber Type C	n/a	0.00567	n/a	n/a	n/a	0.004472	n/a	0.00560	n/a

**Table 2. Breakdown of maximum deflection data from FWD test: 4.5" whitetopping pavement**

	Max Deflection (in)								
	Scarify			HMA Stress Relief			Patch		
Fiber Type	4.5 x 4.5	6 x 6	9 x 9	4.5 x 4.5	6 x 6	9 x 9	4.5 x 4.5	6 x 6	9 x 9
No Fibers	0.00581	0.00573	n/a	0.00497	0.00417	n/a	0.00387	0.00371	n/a
Fiber Type A	0.00539	0.00294	n/a	0.00371	0.00352	n/a	0.00530	0.00489	n/a
Fiber Type B	0.00262	0.00370	n/a	0.00424	0.00592	n/a	0.00409	0.00637	n/a
Fiber Type C	n/a	n/a	0.00510	n/a	n/a	0.00450	n/a	n/a	0.00478

#### Collection of Strain Data

The composite pavement on Iowa Highway 13 was instrumented with strain gages to obtain the strains induced in the pavement under truck loading. Five locations along Iowa Highway 13 were instrumented, each with 3 sets of gages spaced approximately two joint panels apart. The exact stationing and layout of the gages are shown in Appendix A. The pavement configurations of the instrumented locations were as follows:

- Site 1: 3.5" whitetopping thickness, joints spaced 4.5 x 4.5 ft with longitudinal gage orientation
- Site 2: 3.5" whitetopping thickness, joints spaced 6 x 6 ft with transverse gage orientation
- Site 3: 4.5" whitetopping thickness, joints spaced 9 x 9 ft with longitudinal gage orientation

- Site 4: 4.5" whitetopping thickness, joints spaced 4.5 x 4.5 ft with transverse gage orientation
- Site 5: 4.5" whitetopping thickness, joints spaced 6 x 6 ft with longitudinal gage orientation

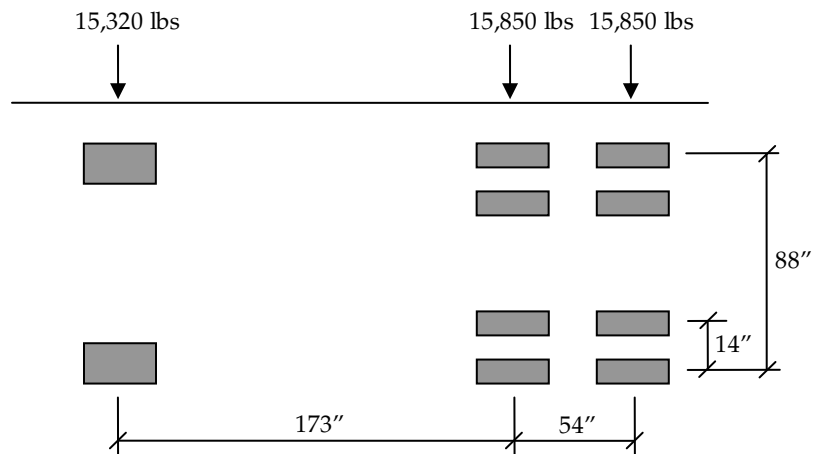
Three cores, designated as Core 1, 2, and 3, were taken at each of the five sites listed above. At each core location, three strain gages were mounted: (1) on top of the bottom PCC, (2) on top of the ACC, and (3) on top of the whitetopping surface. Installation of the gages was performed by first coring from the top of the whitetopping to the top of the base PCC layer, after which a strain gage was placed on the PCC surface. An ACC mix was then added to fill the core up to the top of the original ACC layer, which was followed by the installation of a second strain gage on the surface of the ACC fill material. Finally, a concrete mix was used to fill the core up to the top of the whitetopping PCC, and the third strain gage was then placed on the top of the whitetopping. Unfortunately, several of the strain gages placed on the top of the whitetopping were damaged by vehicular traffic before testing was performed. Temperature gages were also installed in different cores at the five test sites listed above. These gages were used to gather data on the temperature differentials experienced by the composite pavement.



**Figure 10. Temperature and strain gages along Iowa highway 13**

Two load tests were performed on the five test sites listed above with a fully loaded truck provided by the Iowa Department of Transportation (Iowa DOT). However, only the load test performed on September 10, 2004 was used in this study as static load tests were performed alongside moving load tests only on that testing date. The load configuration was as shown in Figure 11.





**Figure 11. Configuration of truck load used for strain data collection**

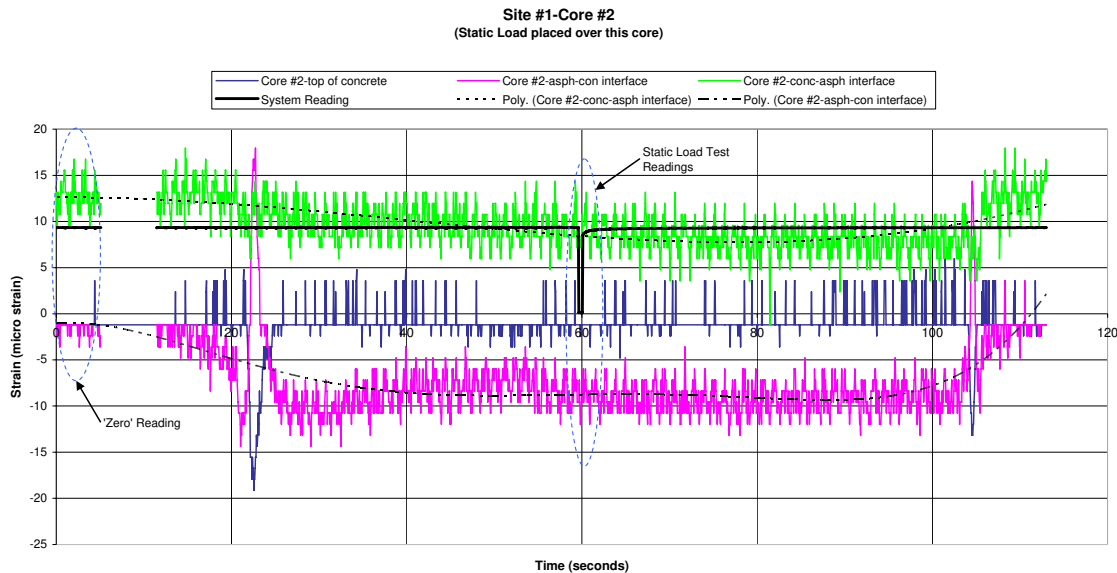


**Figure 12. Test truck provided by IDOT for strain data collection**

Strain gage readings were continuously recorded as the truck was slowly driven over the three strain gage locations at each of the 5 test sites. A static load test was also performed by stopping the truck momentarily on one of the three instrumented cores at each instrumented site. Unfortunately, analysis of the data collected from the load test suggests that many of the strain gages installed did not function as intended. Only 13 of the 45 strain gages that were installed provided any discernable information.

Figure 13 shows an unfiltered recording of the strain gage data that were collected during the load test. The colored lines represent the readings from the three strain gages installed in the different layers as the truck traveled along the composite pavement. The readings at the extreme left and right of the chart correspond to the strain gage readings taken when the truck was significantly distant from the strain gages, and hence represent the “zero” readings of the strain gages in question. The peak in the solid horizontal black line indicates the portion of the measurements that correspond to measurements collected during the static load test, which was of particular interest to this study. Appendix A contains additional unfiltered test data for the other locations.

A trend-line was fitted to the readings of each strain gage on a trial and error basis to determine a best-fit line that represents the data collected adequately. Examples of these best-fit trend-lines are shown in Figure 13 as black, dashed lines. The strain reading for the static load test was then approximated utilizing the trend-line by taking the difference between the strains corresponding to the static test and “zero” readings.



**Figure 13. Example of strain gage reading**

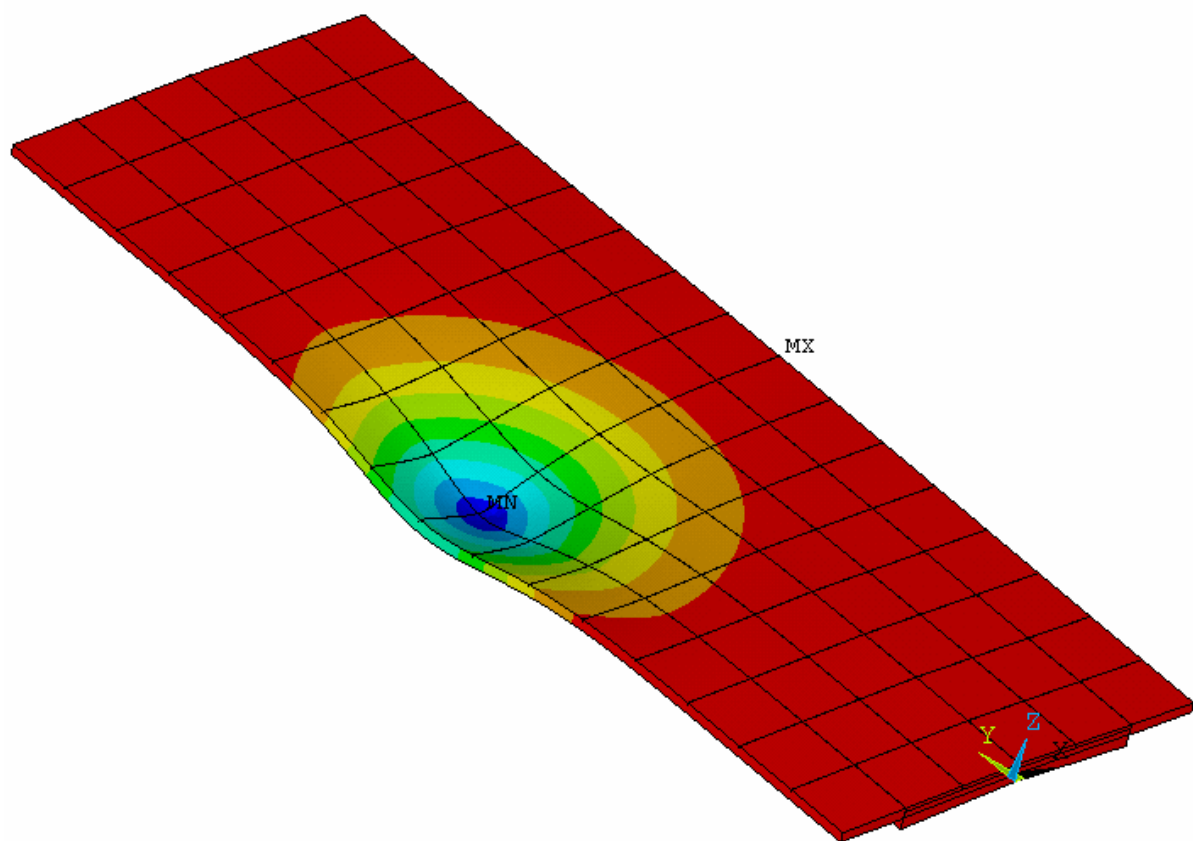
### ***Composite Pavement Analysis with Field Test Loads***

The composite pavement on Iowa Highway 13 was analyzed under the different test loads described in the previous section. This required knowledge of the properties of the pavement materials and the soil subgrade reaction. Unfortunately, detailed information regarding these parameters was not available and had to be estimated from well-established norms. Information gathered from communication with Iowa DOT provided an estimate on the compressive strength of the whitetopping layer of 4500psi. The modulus of elasticity for the ACC layer was estimated from common values encountered in the central Iowa region (Coree 2004). Values of the ACC modulus of elasticity from the spring and fall seasons were utilized to reach an estimate of 650,000 psi for the modulus of elasticity of the ACC layer in this study. This value corresponds with the time when the different field tests were performed. Typical values of 0.35 and 0.2 were assumed for the Poisson's ratio of asphalt and concrete, respectively.

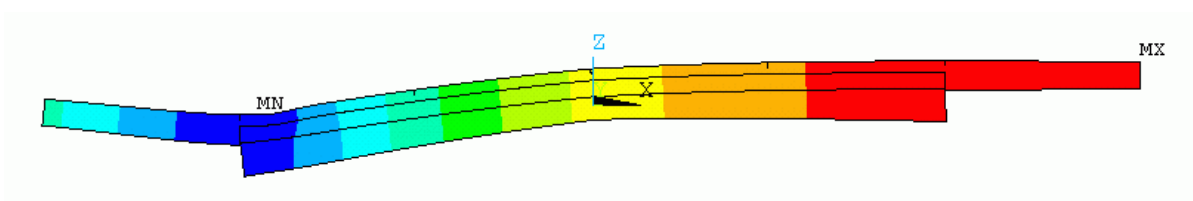
As mentioned previously, information regarding the properties of the soil beneath the pavement was not known; thus, it was necessary to determine the modulus of subgrade reaction,  $k_s$ , using a different approach. While an estimate of 75 pci was suggested (Cable 2004), the value of  $k_s$  was estimated based upon the more rational method of comparing analysis results with the deflection data obtained from FWD testing.

### **Comparison with FWD Deflection Data**

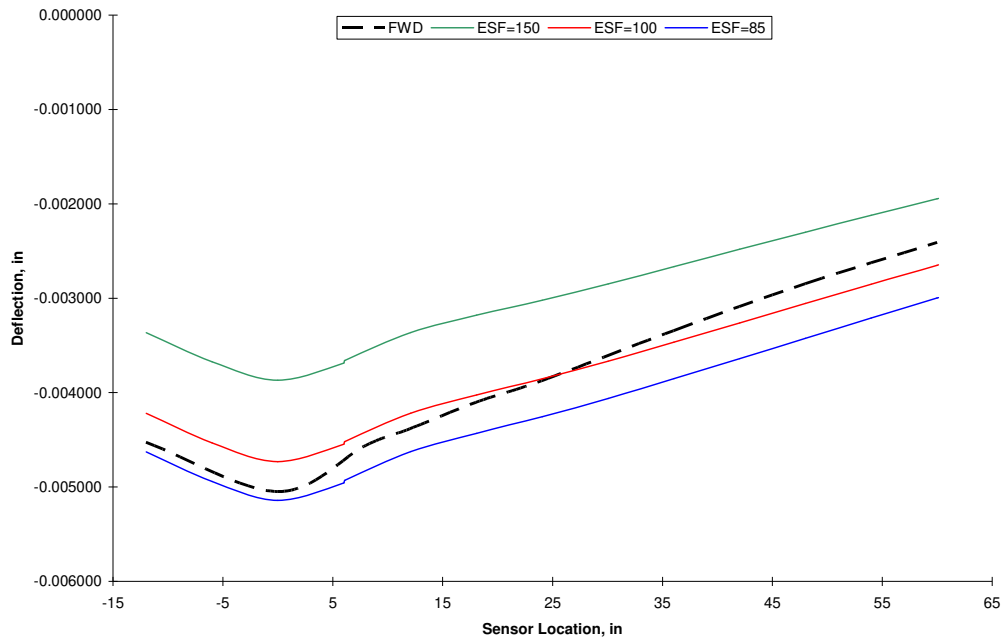
In order to determine a suitable value of the soil subgrade modulus, the six base models described in section "Finite Element Modeling of Composite Pavement on Iowa Highway 13" were subjected to a 9-kip load placed at the edge of a transverse joint and close to the edge of the 18 ft composite section. This was similar to the magnitude and location of the load applied during FWD testing of the composite pavement on Iowa Highway 13. Different soil subgrade reaction values of 85 pci, 100 pci, and 150 pci were used to investigate the effects of the soil subgrade reaction on the deflection of the pavement. Deflection results obtained from analysis were recorded at locations corresponding to the deflection sensors (see Figure 9). An example of the deformed shape of the composite pavement subjected to the 9-kip FWD loading is shown in Figure 14. Figure 15 shows the cross-section of the pavement where the maximum deflection occurred. The deflection profiles for the different pavement configurations, as predicted by the finite element analysis, and the corresponding measured deflection profiles are shown in Figures 16 to 21.



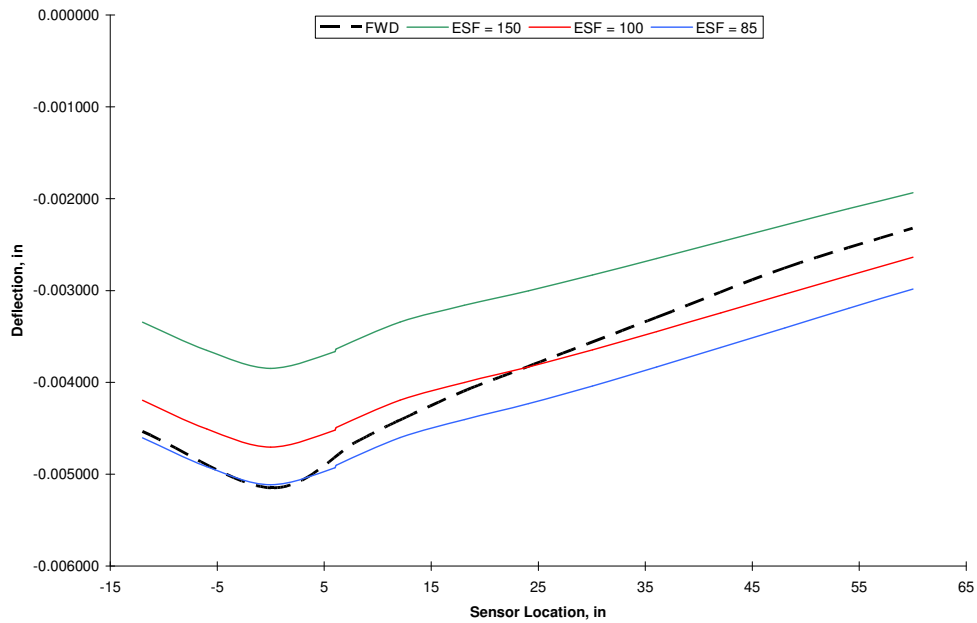
**Figure 14. Example of composite pavement deflected shape (9-kip load)  
(plan view—exaggerated scale)**



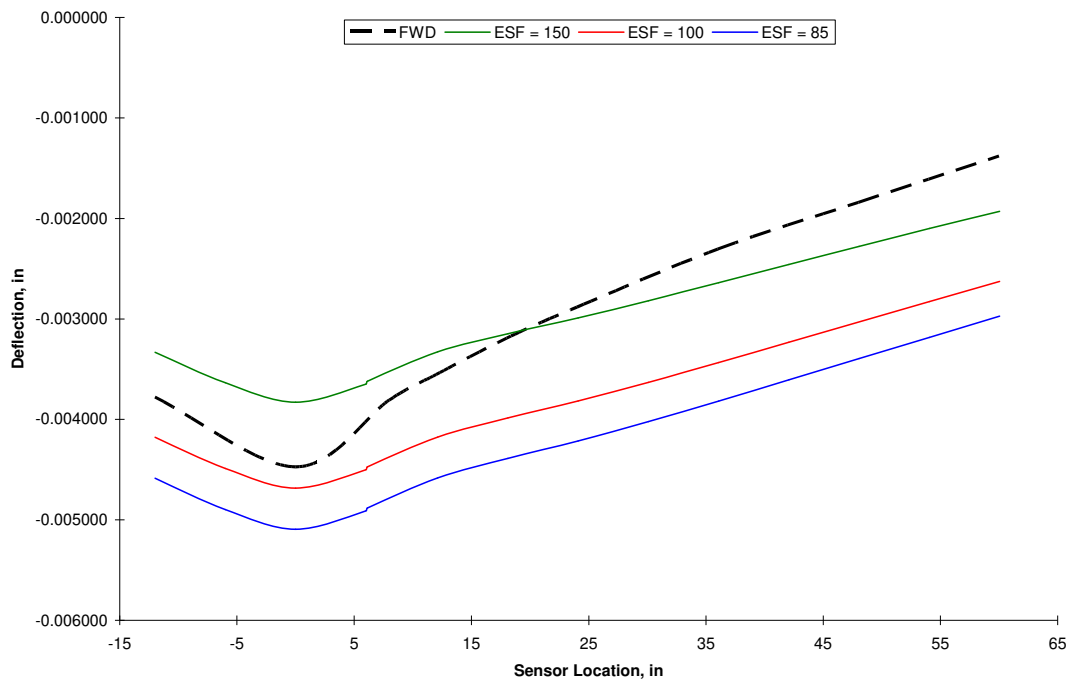
**Figure 15. Example of composite pavement deflected shape (9-kip load)  
(cross-section view—exaggerated scale)**



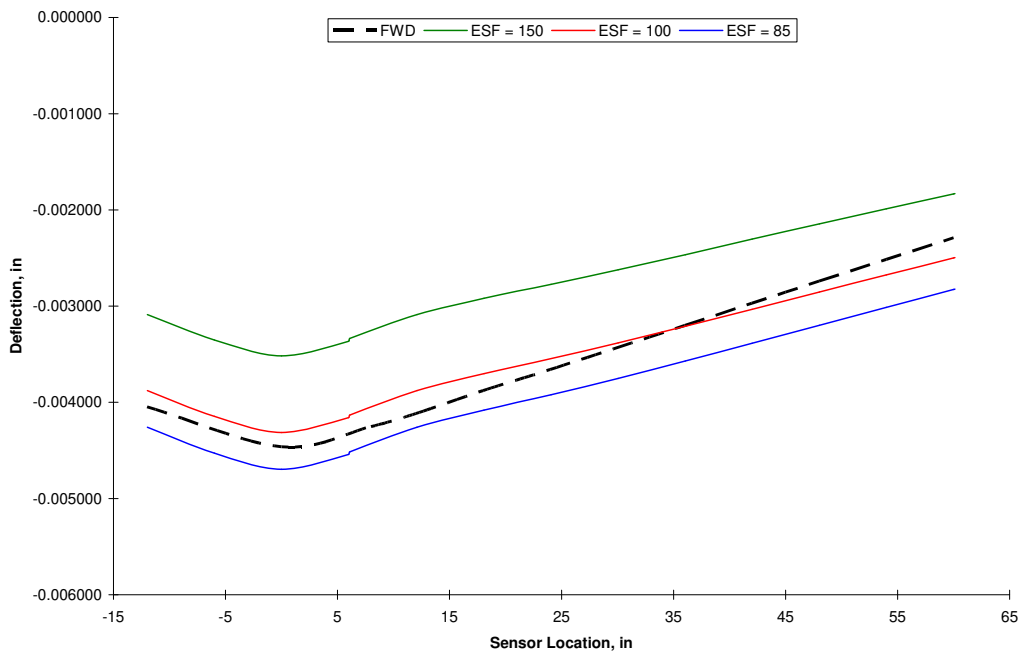
**Figure 16. Deflection comparison for pavement with 3.5" whitetopping and 4.5 ft joint spacing**



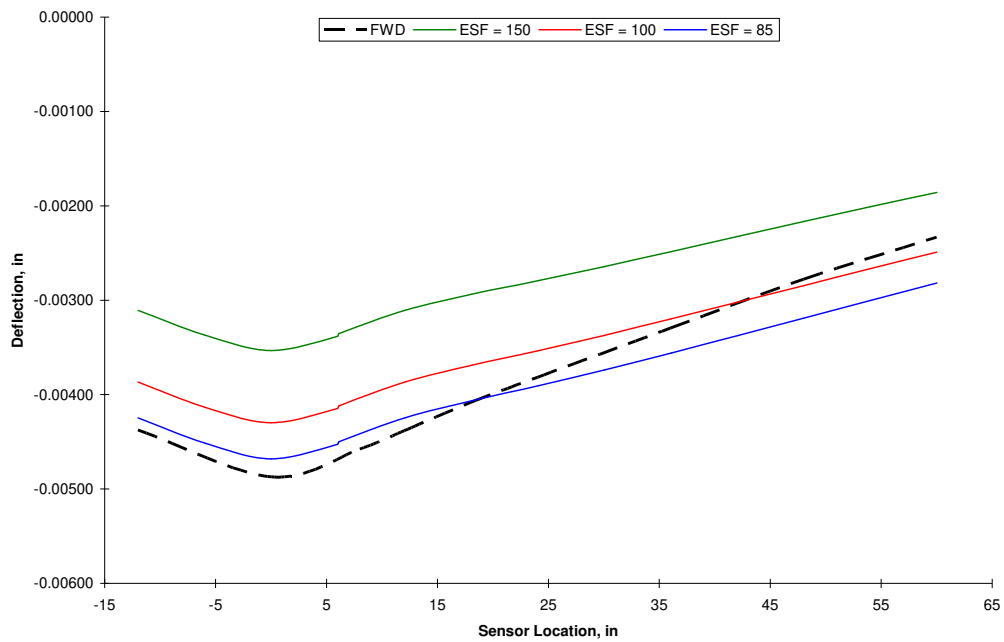
**Figure 17. Deflection comparison for pavement with 3.5" whitetopping and 6 ft joint spacing**



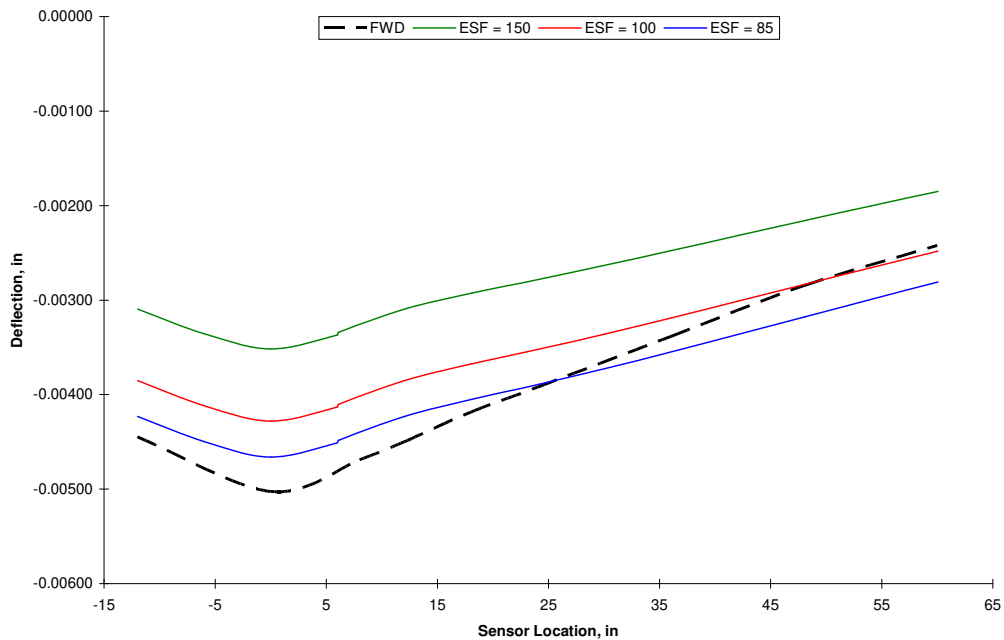
**Figure 18. Deflection comparison for pavement with 3.5" whitetopping and 9 ft joint spacing**



**Figure 19. Deflection comparison for pavement with 4.5" whitetopping and 4.5 ft joint spacing**



**Figure 20. Deflection comparison for pavement with 4.5" whitetopping and 6 ft joint spacing**

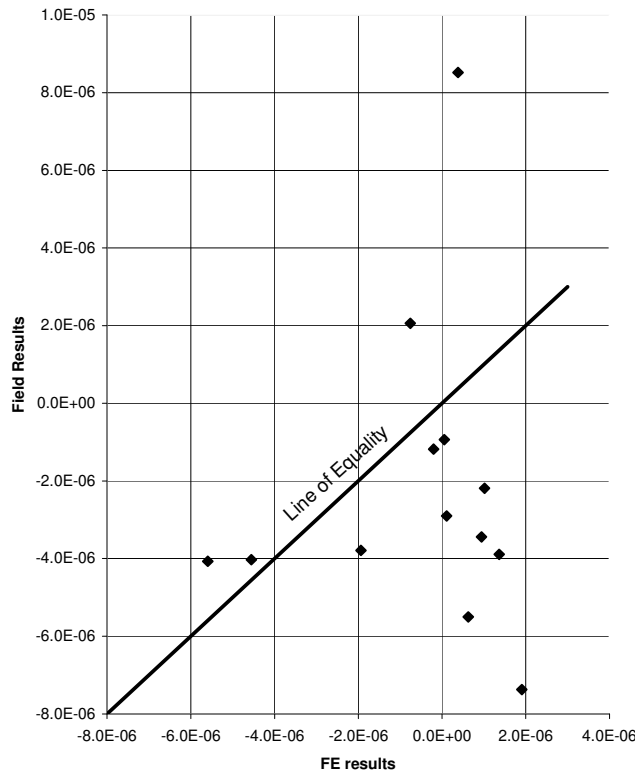


**Figure 21. Deflection comparison for pavement with 4.5" whitetopping and 9 ft joint spacing**

As can be seen from the preceding figures, the deflections obtained from FWD testing appear to be bounded by  $k_s$  values of 85~100 pci, and is closer to those obtained using  $k_s$  of 85 pci. This is slightly different from the estimate of 75 pci (Cable 2004). The lower value of 85 pci was selected as an acceptable value to represent the stiffness of the foundation beneath the composite pavement on Iowa Highway 13 and was utilized in all subsequent finite element analyses in this study.

### Comparison with Measured Strain Data

As previously stated, the pavement models were analyzed under the truck load that was used in the field test of the composite pavement (see Figure 11). Fully bonded conditions were assumed in the analysis. The strains induced in the pavement were calculated at locations corresponding to the gage locations on Iowa Highway 13 and were compared to the measurements obtained from the strain gages where available. Transverse and longitudinal strains in the three different layers were considered in the comparison, which is plotted in Figure 22. If the strain results obtained using 3-D model and the measured results were equal, distribution of the data points along the line of equality is expected.



**Figure 22. Comparison of experimental and analytical strain results**



The above comparison shows some discrepancy between the results from the finite element analysis and field test results. However, the strains obtained from finite element analysis and from the field test data were both in the range of -10 to 10 microns, while the error of the strain gages used was in the range of 4~5 microns. This could be a significant part of the reason for the poor agreement between experimental and analytical results. In addition, the method of installation of the strain gages could also have contributed to the discrepancy, as removal of the original pavement material could have altered the behavior of the pavement at the strain gage locations, which can not be accurately accounted for in the 3-D model. As most of the strain gages that were installed had malfunctioned or were damaged, the accuracy of the data from the remaining strain gages that was deemed useful could also be suspect. Interference from passing traffic while the truck load testing was performed could also have easily contributed to further error in the experimental results.

Not all reasons for the discrepancy were due to experimental factors. Localized differences in the soil properties from test site to test site could exist and would require that different values for the soil subgrade reaction be used instead of the 85 pci determined previously. Simplification of the model by assuming perfectly undamaged ACC and PCC layers underlying the whitetopping could be another source of error. Additionally, the degree of bond at the interfaces between the layers is potentially another factor contributing to the discrepancy between experimental and analytical results. Unfortunately, a lack of information regarding actual field conditions and interaction mechanism renders a highly detailed model which adequately accounts for all these factors improbable in the current analysis.

With the many factors potentially contributing to the discrepancy between field data and analytical strain values, the comparison is thus inconclusive and no determination can be made regarding the accuracy of the finite element model based upon these strain results alone. However, the favorable comparison between the deflection values and deflection profiles recorded from the field, and those obtained from analyses, generated sufficient confidence in the results from the finite element model. Hence, the finite element model was further utilized to investigate the behavior of the composite pavement on Iowa Highway 13.

## **Analysis of Iowa Highway 13 Composite Pavement**

Following the verification of the pavement model developed for the finite element program ANSYS, the 3-D composite pavement model was subjected to different loading conditions. A parametric study was carried out to investigate the effects that whitetopping thickness, interface bonding, joint spacing, depth of joint crack, widening unit configuration, and tie bar size and spacing have on overall structural behavior. The pavement was then subjected to heavy truckloads, and temperature gradients were recorded from the installed gages to determine the stresses that could be induced in the composite pavement in the field.

### ***Parametric Study of Composite Pavement***

Of particular interest in the study presented herein are the effects of the following factors on pavement behavior:

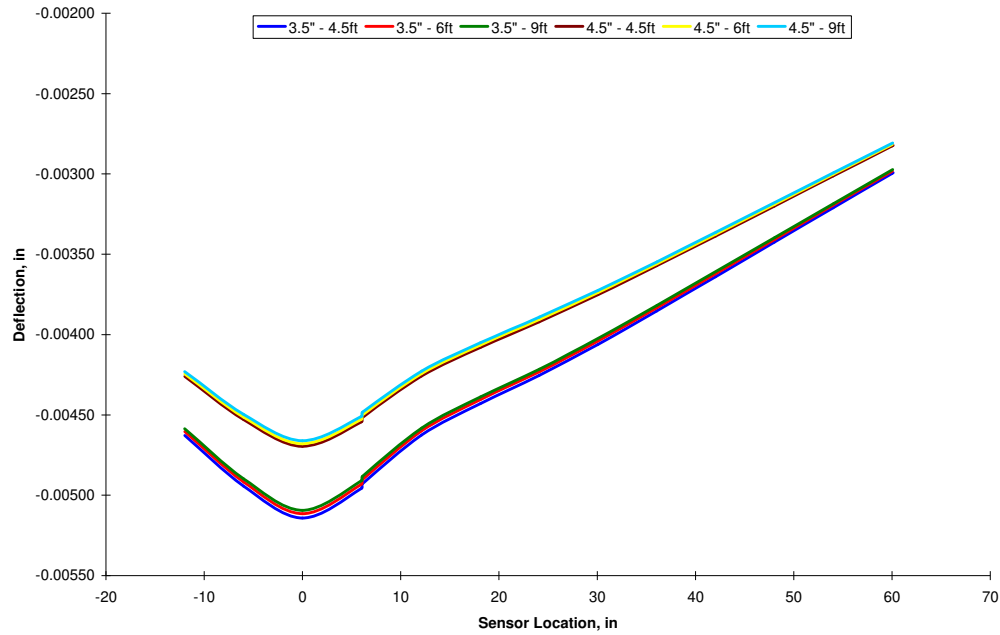
- Thickness of the whitetopping
- Spacing of the joints
- Depth of the cracks along the joints
- Bonding of the layers
- Width and depth of the widening units
- Size and spacing of tie bars

Therefore, the composite pavement was analyzed considering each of the variables listed above. As mentioned in chapter “Modeling of Iowa Highway 13 Composite Pavement,” in the development of the 3-D finite element model, only the saw-cut joints in the whitetopping layer were modeled, and the rest of the pavement structure was assumed to be un-cracked. The soil subgrade reaction modulus,  $k_s$ , was assumed to be 85 pci. The pavement layers were considered to be fully bonded to one another, except when investigating the effects of interface bond behavior. Material properties of the different layers listed in the previous chapter were again utilized in this portion of the study. For the purposes of the parametric study, the pavement was subjected to a 9-kip load located at the edge of a transverse saw-cut joint and at the edge of the widening unit–composite section longitudinal joint shown in Figure 7.

### **Whitetopping Thickness and Joint Spacing**

The whitetopping overlay on Iowa Highway 13 was constructed with two different thicknesses. One should expect that the thicker whitetopping would provide better pavement performance. In order to quantify this difference in the behavior of the composite pavement, a total of six pavement models, configured with combinations of the two whitetopping thicknesses (3.5 in. and 4.5 in.) and three saw-cut joint configurations (4.5 x 4.5 ft, 6 x 6 ft and 9 x 9 ft), were analyzed under a 9-kip load. Deflection profiles, similar to those obtained by FWD testing, were constructed from the results of the analyses and are presented in Figure 23. The numerical values for the maximum deflection for each case are tabulated in Table 3. The maximum compressive

and tensile stresses that were induced in the pavement by the applied load in each of the three layers are presented in Tables 4 and 5.



**Figure 23. Deflection profiles for pavements with 3.5" and 4.5" whitetopping thickness**

**Table 3. Maximum composite pavement deflections (9-kip load)**

Joint Spacing	Max Deflection (in.)	
	3.5"	4.5"
4.5ft x 4.5ft	0.00514	0.00470
6ft x 6ft	0.00512	0.00468
9ft x 9ft	0.00509	0.00466

**Table 4. Maximum transverse stresses (psi) for different joint configurations (9-kip load)**

	Joint Spacing	Whitetopping		ACC		PCC	
		Tension	Comp.	Tension	Comp.	Tension	Comp.
3.5"	4.5ft x 4.5ft	37.004	-108.463	14.346	-15.827	37.241	-7.667
	6ft x 6ft	37.131	-106.945	14.123	-15.976	37.733	-7.924
	9ft x 9ft	36.917	-104.428	14.123	-15.924	37.422	-8.221
4.5"	4.5ft x 4.5ft	35.643	-102.592	13.490	-12.743	34.841	-6.220
	6ft x 6ft	35.453	-101.091	13.571	-12.769	34.617	-6.455
	9ft x 9ft	34.282	-98.525	13.512	-12.721	34.287	-6.674

**Table 5. Maximum longitudinal stresses (psi) for different joint configurations (9- kip load)**

	Joint Spacing	Whitetopping		ACC		PCC	
		Tension	Comp.	Tension	Comp.	Tension	Comp.
3.5"	4.5ft x 4.5ft	31.729	-123.174	11.544	-17.347	70.942	-16.835
	6ft x 6ft	31.079	-122.264	11.428	-17.514	70.560	-16.633
	9ft x 9ft	30.530	-121.010	11.415	-17.435	70.162	-16.572
4.5"	4.5ft x 4.5ft	31.528	-113.645	10.832	-13.994	62.897	-11.745
	6ft x 6ft	31.000	-112.791	10.899	-14.036	62.615	-11.744
	9ft x 9ft	30.466	-111.497	10.863	-13.960	62.309	-11.690

As can be seen from Figure 23 and Table 3, the deflections experienced by the pavements with thinner whitetopping overlays were about 10% larger than those with 4.5" overlays. The pavements with thicker whitetopping overlays also exhibited lower stresses, particularly in the longitudinal direction, in the range of 5.5% to 7.9% for stresses in the whitetopping layer. The thicker whitetopping layer also reduced stresses in the underlying ACC and PCC layers, with reduction of up to 11.2% in the tensile stresses at the bottom PCC layer. The combination of deflection and stress results indicate that the 4.5" overlay exhibits better performance with deflections and stresses as the design criteria.

The deflection profiles in Figure 23 also seem to suggest that the different joint spacings do not significantly affect pavement behavior when subjected to vertical loads. While overlays with joint spacing at 4.5 x 4.5 ft had the largest deflection and stresses, and overlays of 9 x 9 ft joint spacing exhibited the least amount of deflection and stresses for both thicknesses, the differences were not significant. This contradicts findings from other studies (Tarr, Sheehan, and Okamoto 1998; Kumara et al. 2003), which demonstrate that pavement deflection varies with joint spacing, especially when subjected to temperature loading. The reason for the discrepancy with the findings of other studies was due to the assumption made in the current study that the underlying ACC and PCC layers were crack-free and continuous, while other studies focused on the testing or analyzing of composite pavement panels in isolation. This demonstrates that the condition of the layers underlying the overlay has a significant effect on pavement behavior.

#### Joint Crack Depth

The saw-cut joints in the whitetopping were modeled with two different depths to determine the effects of joint crack propagation through the depth of the overlay on pavement behavior. Pavement models with 3.5" whitetopping overlay and the three different joint spacings were analyzed considering the two different crack depths, and the maximum deflections obtained are tabulated in Table 6.

**Table 6. Maximum deflections due to varying overlay crack depths (9-kip load)**

Joint Spacing	Max. Deflections (in)	
	1.5"	Full Depth
4.5ft x 4.5ft	0.00514	0.00526
6ft x 6ft	0.00512	0.00522
9ft x 9ft	0.00509	0.00516

The results in Table 6 revealed that modeling the joints assuming that the cracks propagated through the depth of the overlay only resulted in slightly larger deflections. The deflection profiles for the models with full overlay depth cracks exhibited the same behavior as the corresponding model with 1.5" crack depth. The maximum stresses in the pavement layers with the joints modeled as cracked through the overlay thickness are given in Table 7.

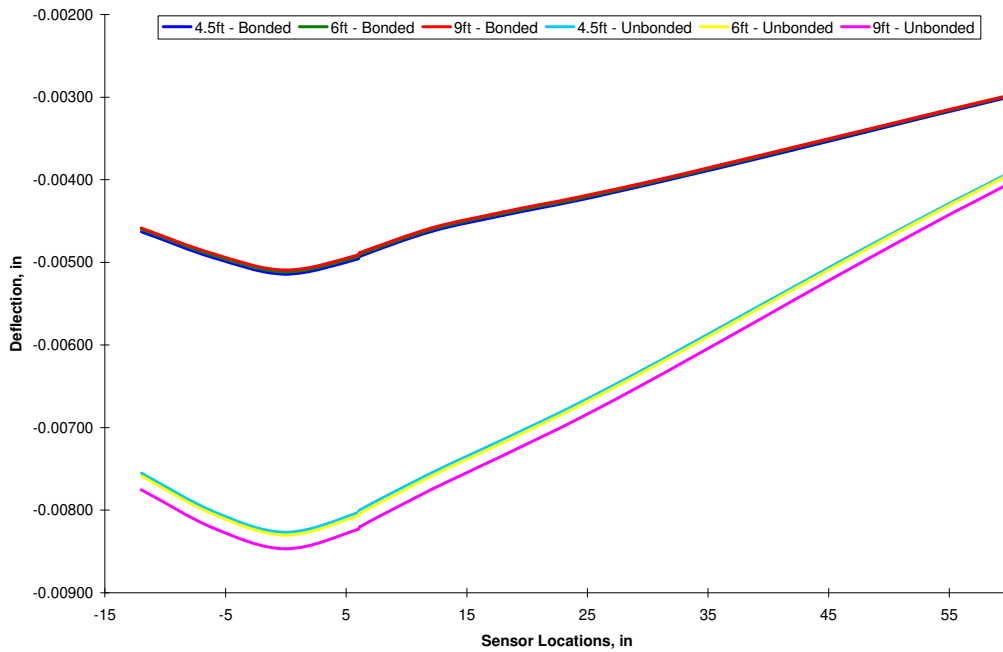
**Table 7. Maximum stresses (psi) for full overlay depth joint cracks (9-kip load)**

Joint Spacing	Whitetopping		ACC		PCC	
	Tension	Comp.	Tension	Comp.	Tension	Comp.
<i>Transverse:</i>						
4.5ft x 4.5ft	38.747	-107.409	14.880	-16.096	39.331	-8.566
6ft x 6ft	38.226	-105.969	14.775	-16.03	38.803	-7.973
9ft x 9ft	37.795	-102.956	14.645	-16.088	38.371	-8.542
<i>Longitudinal:</i>						
4.5ft x 4.5ft	31.998	-113.212	11.646	-17.837	72.920	-17.535
6ft x 6ft	31.381	-114.030	11.578	-17.721	72.175	-17.342
9ft x 9ft	30.692	-110.502	11.508	-17.716	71.429	-17.211

The results from Table 7 were compared to the transverse and longitudinal stresses for 3.5" whitetopping presented in Tables 4 and 5. While the stresses induced in models with joints modeled as full overlay depth cracks were generally larger, the differences between the cases were not significant. The small differences in deflection and stresses obtained from analysis could once again be attributed to the assumption of undamaged and crack-free ACC and PCC layers underlying the whitetopping overlay.

#### Bond Condition Between Layers

The effect of the interface bond on pavement behavior was investigated by analyzing the composite behavior by assuming either full bonding between all three layers or no bonding between all three layers, thus providing results for two extreme cases. The whitetopping overlay thickness was assumed to be 3.5 in. for this comparison, and the three different joint configurations of 4.5 x 4.5 ft, 6 x 6 ft, and 9 x 9 ft were also included in the investigation. Figure 24 compares the deflection profiles obtained from the analyses and demonstrates that interface bonding significantly affects the deflection behavior of the pavement.



**Figure 24. Comparison of deflections for bonded layers and unbonded layers**

Maximum deflections increased by approximately 61%–66% when the layers were unbonded, as compared to the deflections obtained when the layers were fully bonded. The deflection profiles above suggest that the assumption of fully bonded contact between the layers could be reasonable, as the value of  $k_s$  needed to match the deflections of an unbonded pavement with those obtained from field testing would have been unrealistically high for the test site. To further illustrate the effects of interface bond condition on pavement behavior, maximum tensile and compressive stresses for the cases of bonded and unbonded layers are tabulated in Tables 8 and 9.

**Table 8. Maximum transverse stresses (psi) for bonded/unbonded composite pavement (9-kip load)**

Joint Spacing	Whitetopping		ACC		PCC	
	Tension	Comp.	Tension	Comp.	Tension	Comp.
<i>Bonded</i>						
4.5ft x 4.5ft	37.004	-108.463	14.346	-15.827	37.241	-7.667
6ft x 6ft	37.131	-106.945	14.123	-15.976	37.733	-7.924
9ft x 9ft	36.917	-104.428	14.123	-15.924	37.422	-8.221
<i>Unbonded</i>						
4.5ft x 4.5ft	80.231	-146.043	49.855	-21.601	70.222	-73.291
6ft x 6ft	79.631	-143.794	49.482	-23.149	72.016	-74.644
9ft x 9ft	88.612	-138.081	48.314	-26.923	75.375	-77.126

**Table 9. Maximum longitudinal stresses (psi) for bonded/unbonded composite pavement (9-kip load)**

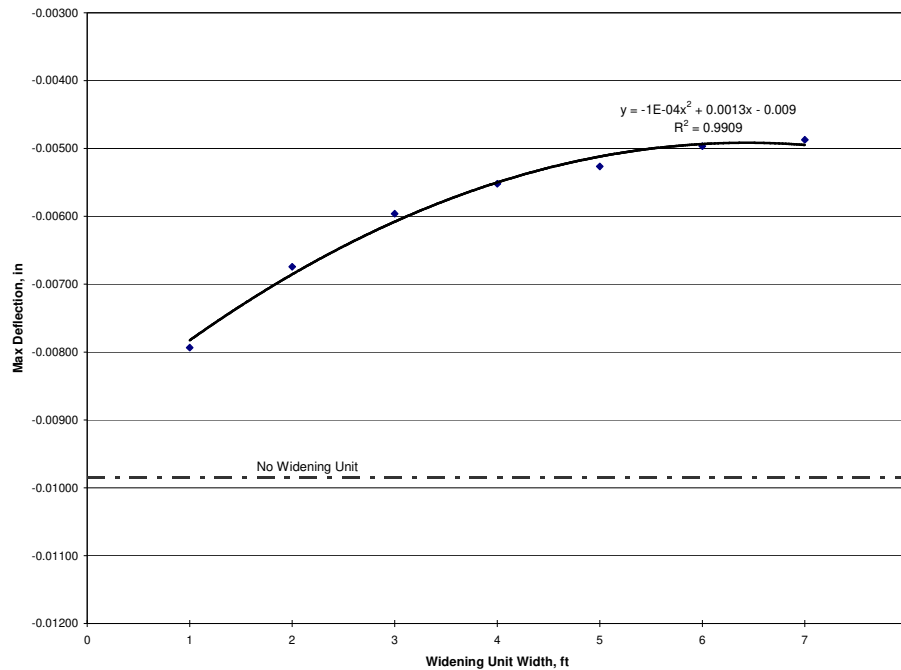
Joint Spacing	Whitetopping		ACC		PCC	
	Tension	Comp.	Tension	Comp.	Tension	Comp.
<i>Bonded</i>						
4.5ft x 4.5ft	31.729	-123.174	11.544	-17.347	70.942	-16.835
6ft x 6ft	31.079	-122.264	11.428	-17.514	70.560	-16.633
9ft x 9ft	30.530	-121.010	11.415	-17.435	70.162	-16.572
<i>Unbonded</i>						
4.5ft x 4.5ft	79.917	-135.582	44.879	-22.265	105.197	-96.862
6ft x 6ft	79.377	-133.616	43.697	-23.660	105.939	-96.935
9ft x 9ft	78.986	-130.792	42.849	-26.772	107.795	-97.673

The results showed that removing the bond between the layers resulted in significant increases in the stresses that were induced in the composite pavement. For example, increases as much as 288% in the tensile stresses were seen in the asphalt layer, while tensile stresses in the whitetopping overlay increased as much as 152% when the layers were unbonded. Larger loads resulting from the heavy-truck traffic on Iowa Highway 13 can be expected, and maintaining bonded conditions between the layers is essential in keeping deflections and stresses low due to these larger loads.

Data on the bond strength of the composite pavement were documented in the construction report (Cable et al. 2003), and the average bond strength was in the range of 155 to 302 psi, depending on the surface preparation. These are higher than the shear stresses between the interfaces that were obtained from the analyses. The analyses revealed a maximum interface shear stress of no more than 40 psi with the 9-kip load that was utilized.

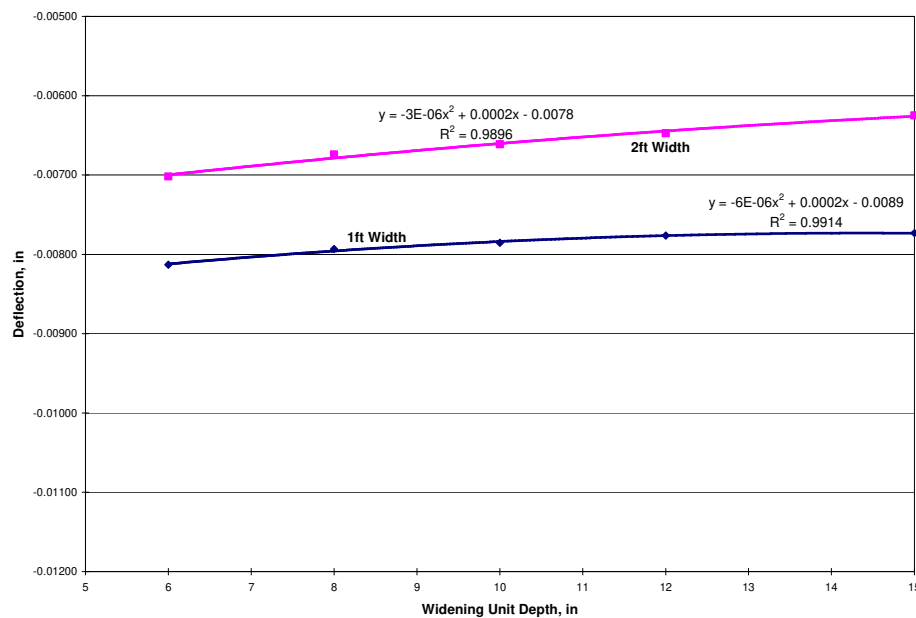
#### Widening Unit Dimensions

Several analyses were performed to determine the differences in deflections that would be induced in the pavement with varying widening unit dimensions, specifically different widths and depths. For this purpose, the composite pavement was analyzed considering widening unit widths of 1, 2, 3, 4, 5, 6, and 7 feet. The edge thickness was assumed to be 8". The maximum deflections corresponding to the different widths were obtained from finite element analysis and are plotted in Figure 25. The maximum deflection obtained from the analysis of an un-widened pavement is also included for comparison.



**Figure 25. Maximum deflections—varying widening unit widths (9-kip load)**

The effect of different depths of the widening units on deflections was also investigated by varying the edge thicknesses of the widening units. Widening units with thicknesses of 6, 8, 10, 12, and 15 inches were analyzed in conjunction with widths of 1 and 2 feet. The maximum deflections that were induced in the pavement are plotted in Figure 26.

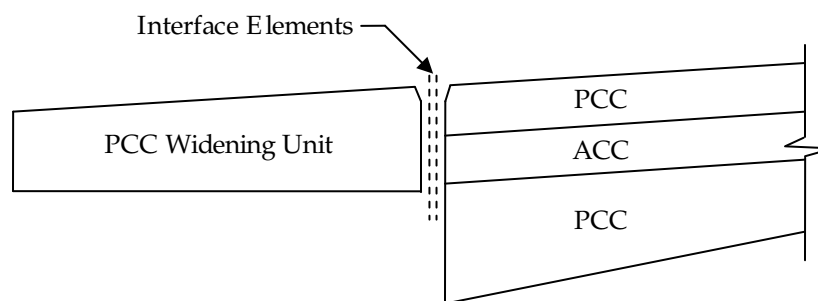


**Figure 26. Maximum deflections—varying widening unit depths (9-kip load)**



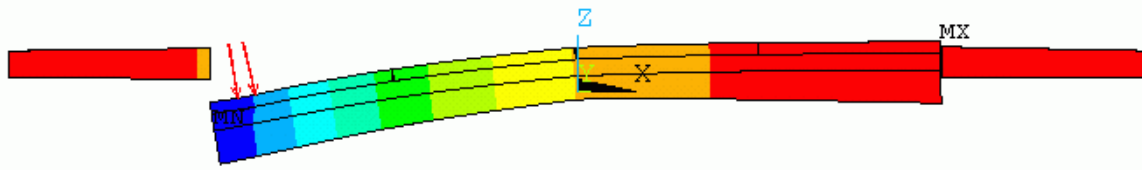
The figures show that as the widening unit width was increased, deflections induced in the composite pavement decreased. Similar to result found in the initial analytical work (Cable et al. 2003), the pavement experienced a 53% reduction in maximum deflection when the widening units were configured with 5 ft width and 8 in thickness; however, with successively larger widening unit widths, the reduction in deflection gained diminished. Figure 26 suggests that any benefit in deflection reduction for widening units larger than 7 ft would be minimal. On the other hand, while increasing widening unit depth leads to decreasing pavement deflection, the reduction gained was not as dramatic as that for increasing widening unit width. The results suggest that for widened pavements structures, increasing widening unit width may be the most efficient method for achieving lower deflections.

The initial analytical work presented in the construction report had speculated on the reason for the lower deflections experienced by the widened composite pavement on Iowa Highway 13. The study proposed that the arched shape of the pavement cross-section along with the widening units permitted the development of lateral confinement forces that helped reduce the magnitude of deflection. The 3-D finite element model was also utilized to investigate the validity of the “arch effect” proposed in the initial analytical work. Modifications were made to the finite element model by inserting interface elements between the widening units on either side of the composite pavement, as illustrated in Figure 27. The interface elements were defined with the “standard” interface condition, thus allowing sliding and separation of the widening units from the 3-layer composite section, which would prevent load transfer between the widening unit and the 18 ft composite section. This procedure isolates the proposed “arch effect” on the behavior of the pavement, i.e., development of additional lateral confinement due to the arch-shaped cross-section, thus allowing the deflection reduction to be quantified independently of load transfer between the widening unit and the composite section.



**Figure 27. Insertion of interface elements between widening unit and composite section**

The pavement model with the modifications described above was analyzed under a 9-kip FWD load, and the maximum deflection was compared to a pavement model in which the widening units were completely removed. Figure 28 shows the plot of the deflected shape produced by finite element analysis.



**Figure 28. Separation at widening unit–composite section interface  
(cross-section view—exaggerated scale)**

As can be seen, separation occurred at the widening unit–composite section interface, implying successful removal of the load transfer effect. However, no difference was found between the deflections of the widened and un-widened pavements when the load transfer effect was removed, implying that the reduction in deflection previously seen was not due to the additional confinement effects of an arch-shaped pavement as was speculated. If the reduction in deflection is to be realized when constructing a widened pavement structure, positive load transfer will have to be ensured between the composite section and the widening units.

The behavior of the composite pavement was further investigated by setting the interface interaction of the interface elements located between the widening units and the composite section to “no separation.” The maximum deflection obtained from analysis was 0.00541 in, which was only slightly greater than the deflection obtained from the original, unmodified model, i.e., 0.00526 in. This result suggests that as long as the widening units are not allowed to separate from the composite section, the benefits of deflection reduction will be realized.

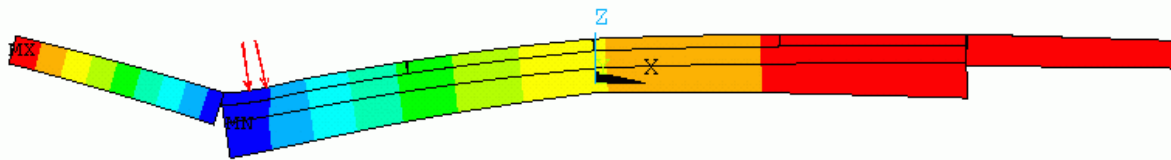
### Tie Bar Size and Spacing

The results in the previous section demonstrate that maintaining a means for load transfer between the widening units and the composite section is essential to reducing deflections induced in the pavement. Load transfer across the joint could be ensured by mechanisms such as aggregate interlock at the joint interface or by the installation of tie bars across the joint; however, the contribution of aggregate interlocking across the joint is not easily quantifiable or controllable by design. An alternative is to use tie bars to ensure sufficient load transfer between the two widening units and the composite section.

As detailed in the construction report, 36 in. long #4 rebars were spaced at 30 in. on center at the longitudinal joints between the widening units and the composite section (see Figure 7) at selected locations along the test section on Iowa Highway 13. With the assumption of the absence of the aggregate-interlock mechanism, the 3-D pavement model was utilized to investigate if the tie bar size and spacing listed above was sufficient to ensure load transfer between the widening units and the composite section. As described in chapter “Modeling of Iowa Highway 13 Composite Pavement,” the tie bars were modeled for finite element analysis using beam elements. Analysis results showed that in the absence of the aggregate interlocking between the widening unit and the pavement, a maximum deflection similar to that of the composite section without

widening units was obtained. This indicated that the bar size and spacing utilized in the project were not sufficient to ensure load transfer across the joint.

Consequently, additional analyses were performed to determine if the tie bar mechanism could be utilized to ensure load transfer across the longitudinal widening unit–composite section joint. The first configuration that was investigated was the utilization of #4 rebars spaced 12 in. on center; however, the analysis results showed that there was insignificant reduction in the pavement deflection. The analysis was repeated considering #8 rebars that were spaced at 30 in. on center. The results yielded a maximum deflection of 0.00773 in, which was less than that obtained with the two previous tie bar configurations. The deflected shape of the pavement is shown in Figure 29, which demonstrates that the tie bar configuration involving #8 rebars spaced at 30 in. on center is successful at preventing complete separation between the widening units and the composite section, thus preventing a complete loss of load transfer at the joint.

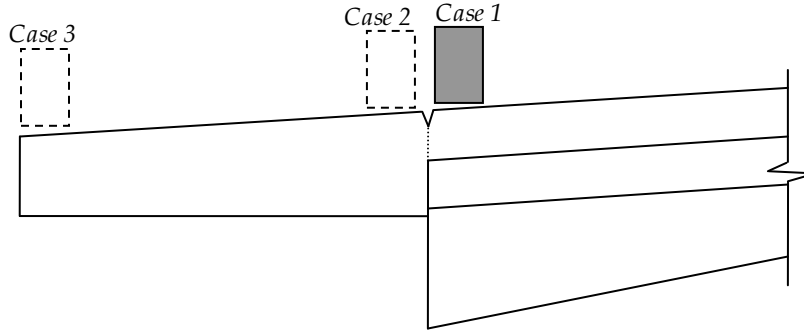


**Figure 29. Partial separation at widening unit–composite section interface  
(cross-section view—exaggerated scale)**

The results indicate that the use of tie bars can ensure a degree of load transfer between the widening units and the composite section. However, bars that were larger and more closely spaced than those used in the project would be needed to achieve perfect load transfer between the widening units and the composite section, assuming tie bar action was the only load transfer mechanism considered.

### ***Pavement Behavior When Subjected to Truck Loading***

Following the parametric study of the previous section, the 3-D composite pavement model was subjected to truck loading to investigate the behavior that the composite pavement on Iowa Highway 13 may exhibit under day-to-day service conditions. The pavement model considered had an overlay thickness of 3.5" and joint spacing of 4.5 x 4.5 ft with fully bonded layers. The truck configuration used for the collection of field strain data (Figure 11) was selected for this part of the investigation, as the fully loaded truck was rated as a heavy traffic load. Analysis of the composite section was performed by positioning a single truck at three different locations across the pavement section to reflect variable driving patterns on the roadway. Figure 30 shows the position of the outer wheel path on the pavement section.



**Figure 30. Location of truck outer wheel on composite pavement**

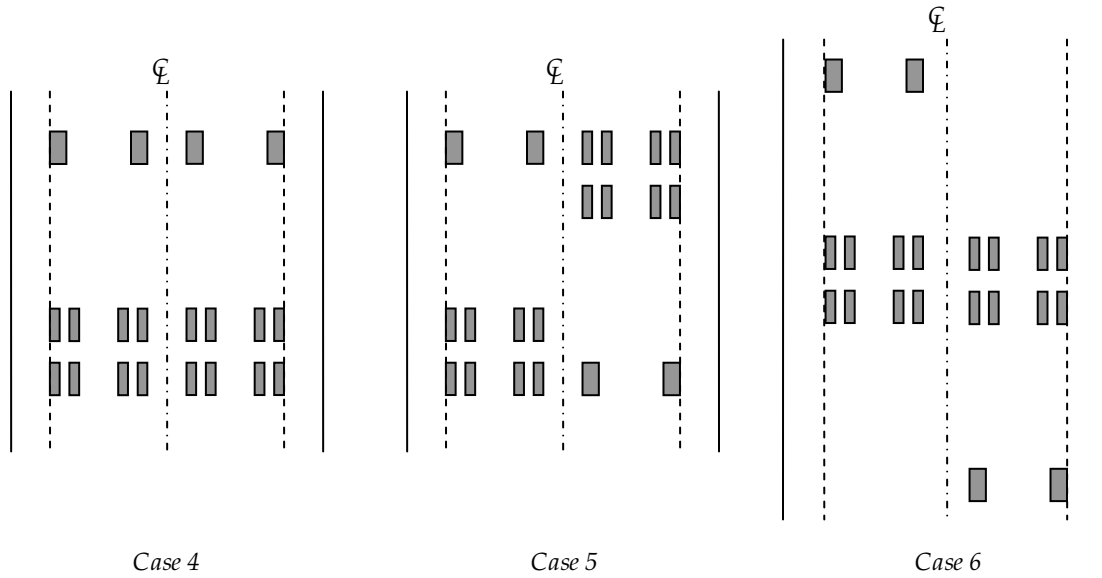
The maximum deflections and stresses in the different layers obtained from the analyses of the three different loading cases are presented in Table 10. The two cases where the outer wheel path was located on a widening unit exhibited significantly worse deflection and stresses than when the outer wheel path was confined to the composite section. In particular, stresses in the whitetopping overlay for the case where the outer wheel path was located on the edge (Case 3) of the widening unit were markedly higher than for the other two cases.

**Table 10. Maximum deflection and stresses in the composite pavement (single truck load)**

Layer	Max Deflection, in	Max Trans. Stress, psi		Max. Long. Stress, psi	
		Tension	Comp.	Tension	Comp.
Case 1					
Whitetopping	-0.009863	52.370	-94.003	35.030	-101.823
Asphalt		20.884	-9.935	14.088	-10.320
Base Concrete		52.675	-12.497	64.459	-20.935
Case 2					
Whitetopping	-0.011782	74.257	-96.860	71.587	-104.510
Asphalt		10.392	-9.542	6.406	-9.121
Base Concrete		42.519	-11.600	62.225	-24.420
Case 3					
Whitetopping	-0.028069	92.695	-81.632	174.090	-190.696
Asphalt		3.430	-26.944	2.405	-15.105
Base Concrete		21.311	-59.621	62.909	-26.972

The pavement model was further analyzed by loading both lanes of the pavement model with the test truck load configuration. The outer wheel paths were confined within the composite section on both sides of the pavement in all cases. The different configurations of the truck loads that were considered are shown schematically in Figure 31. The

maximum deflection and stresses obtained from the analyses of the cases are shown in Table 11.



**Figure 31. Configuration of truck loads with two lanes loaded**

**Table 11. Maximum deflection and stresses in the composite pavement (double truck load)**

Layer	Max. Deflection, in	Max. Trans. Stress, psi		Max. Long. Stress, psi	
		Tension	Comp.	Tension	Comp.
<i>Case 4</i>					
Whitetopping	-0.012728	67.871	-93.065	70.988	-111.15
Asphalt		8.082	-9.543	5.095	-9.187
Base Concrete		35.243	-11.194	68.968	-26.657
<i>Case 5</i>					
Whitetopping	-0.011782	69.089	-92.203	71.255	-111.037
Asphalt		8.17	-9.536	5.055	-9.297
Base Concrete		40.52	-12.194	63.49	-25.106
<i>Case 6</i>					
Whitetopping	-0.012517	67.924	-83.378	70.908	-95.052
Asphalt		8.323	-9.513	5.244	-9.005
Base Concrete		37.194	-11.696	68.62	-28.632

Generally, the cases where the truck loads were placed side-by-side yielded the highest stresses. While the stresses for Cases 4 and 5 were not always higher than that obtained by the single truck in Case 1, longitudinal tensile stresses were approximately twice that of Case 1. In addition, the maximum contact stress in the plane of the interface elements for the cases investigated above were less than 80 psi, obtained from the whitetopping–ACC interface in the edge loading case (Case 3). This was again much less than the bond strength values presented in the construction report (Cable et al. 2003).

As the loading in Case 5 induced the highest tensile stresses in the whitetopping layer, a final analysis was performed by placing the outer wheels for two trucks at the edges of the pavement, positioned side-by-side and facing opposite directions, similar to the orientation in Case 5. The results from this analysis considering this load configuration hereafter referred to as Case 7. The results are summarized in Table 12.

**Table 12. Maximum deflection and stresses due to worst case loading of the composite pavement**

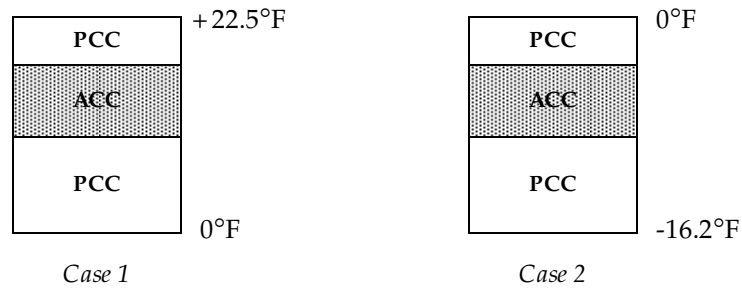
Layer	Max. Deflection, in	Max. Trans. Stress, psi		Max. Long. Stress, psi	
		Tension	Comp.	Tension	Comp.
<i>Case 7</i>					
Whitetopping	-0.027157	99.525	-86.779	173.324	-191.823
Asphalt		3.896	-29.246	2.826	-16.486
Base Concrete		14.630	-64.866	62.937	-26.608

As can be seen, the use of two truck loading placed on the edge of the pavement induced the highest transverse stresses in the composite pavement, while the longitudinal stresses were not significantly different from the case with a single truck loading on the pavement edge (Case 3). The maximum in-plane contact stress for this case was found to be a little less than 70 psi, occurring at the whitetopping–ACC interface.

### ***Pavement Behavior When Subjected to Temperature Differential***

The behavior of the composite pavement when subjected to temperature differentials was considered separately. As material non-linearities and large deflections were not considered in the course of this study, superposition of the results from static load and temperature analyses would sufficiently represent the effects of these two loading conditions on the pavement.

In order to investigate the effects of temperature differentials on the composite pavement on Iowa Highway 13, the composite pavement developed and presented in chapter “Modeling of Iowa Highway 13 Composite Pavement” was subjected to two temperature gradients that produced upward and downward curling of the pavement. The two gradients were +22.5°F at the top and -16.2°F at the bottom, as illustrated in Figure 32. These gradients were the maximum gradients that were obtained from temperature gage recordings from the 5 test sites on Iowa Highway 13.



**Figure 32. Temperature differentials applied to the composite pavement**

The pavement model selected for the analysis had an overlay thickness of 3.5 in, with joints that were cracked through the thickness of the overlay. All three joint spacings, i.e., 4.5 x 4.5 ft, 6 x 6 ft, and 9 x 9 ft, were investigated and the pavement layers were considered to be fully bonded. Typical values of the coefficient of thermal expansion were assumed for the PCC and ACC layers, i.e.,  $5.5 \times 10^{-6}$  in/in/°F and  $5.0 \times 10^{-6}$  in/in/°F, respectively.

Analysis of the composite pavement with the positive temperature gradient, i.e., Case 1, resulted in the upward deflection at the centerline of the pavement and downward deflection of the pavement edges, creating a downward curl. The exact opposite occurred in Case 2, where the centerline of the pavement was deflected downward and the pavement edges were deflected upward, resulting in an upward curling of the composite pavement.

The maximum deflections and maximum stresses at the interfaces of the different layers that were obtained from analyzing the different pavement configurations are summarized in Table 13. The maximum interface shear and normal stresses occurred at the whitetopping-ACC interface for all cases. Case 2 was found to induce larger deflections and interface stresses in the composite pavement, regardless of joint spacing.

Contrary to the findings in previous sections, the interface stresses for the two temperature loading cases were significant. Interface shear stress in the case of negative temperature differentials could possibly exceed the value of the interface bond strength of the composite pavement, which was in the range of 155 to 302 psi, depending on surface preparation (Cable et al. 2003). The normal tensile stresses induced at the interface in Case 2 were at least twice the in-plane shear stresses, which could be a significant factor leading to interface debonding. Clearly, consideration of the partial bonding mechanism is of great importance when accounting for the effect of temperature differentials in the pavement section.

**Table 13. Maximum deflections and whitetopping–ACC interface stresses (temperature differential)**

Joint Spacing	Max. Deflection (in.)	Max. Contact Stresses (psi)		
		In-Plane	Normal - Comp.	Normal - Tension
<i>Case 1</i>				
4.5ft x 4.5ft	0.023587	102.419	-284.883	22.879
6ft x 6ft	0.023691	104.450	-267.336	15.824
9ft x 9ft	0.023270	136.424	-280.078	50.049
<i>Case 2</i>				
4.5ft x 4.5ft	0.032213	166.854	-335.221	370.967
6ft x 6ft	0.033286	157.815	-329.699	397.073
9ft x 9ft	0.034255	194.646	-383.496	396.829

The maximum transverse and longitudinal stresses induced in the three layers of the composite pavement were obtained from analyses of the pavement model under the two temperature gradients considered and are presented in Tables 14 and 15.

**Table 14. Maximum transverse stresses in the composite pavement (temperature differential)**

Joint Spacing	Whitetopping		ACC		PCC	
	Tension	Comp.	Tension	Comp.	Tension	Comp.
<i>Case 1</i>						
4.5ft x 4.5ft	153.452	-419.785	97.207	N/A	133.186	-38.388
6ft x 6ft	145.111	-426.310	93.690	N/A	125.073	-37.648
9ft x 9ft	149.312	-431.886	95.099	N/A	129.470	-36.203
<i>Case 2</i>						
4.5ft x 4.5ft	215.513	-147.404	123.999	-29.069	27.603	-182.550
6ft x 6ft	195.673	-158.787	119.820	-32.929	18.085	-194.571
9ft x 9ft	246.435	-152.000	137.351	-31.668	38.235	-201.728

**Table 15. Maximum longitudinal stresses in the composite pavement (temperature differential)**

Joint Spacing	Whitetopping		ACC		PCC	
	Tension	Comp.	Tension	Comp.	Tension	Comp.
<i>Case 1</i>						
4.5ft x 4.5ft	148.489	-461.134	87.923	N/A	182.985	N/A
6ft x 6ft	148.907	-490.741	86.236	N/A	182.943	N/A
9ft x 9ft	145.869	-502.778	87.674	N/A	181.357	N/A
<i>Case 2</i>						
4.5ft x 4.5ft	240.687	-131.503	128.068	N/A	61.191	-218.978
6ft x 6ft	268.864	-143.246	122.084	N/A	11.913	-218.919
9ft x 9ft	282.616	-153.459	141.475	N/A	25.812	-244.599



These results demonstrate that the stresses induced in the composite pavement by temperature differentials could be several times those induced by vertical loads. While the stresses induced in Case 1 were not significantly different in the pavements with different joint spacing, differences in stresses due to the different joint spacing used were more pronounced in the case of the negative temperature gradient. The joint spacing of 9 x 9 ft generally resulted in larger stresses in the different layers, particularly in the whitetopping overlay, which is to be expected as shorter joint spacings have been shown to reduce curling stresses (Tarr, Sheehan, and Okamoto 1998).

Once again, the assumption that the underlying layers are undamaged and crack-free might have contributed to the relatively small differences found between the different joint spacings, as the pavement behavior was essentially monolithic. One may expect larger differences between the stresses in pavements with different joint configurations as joint crack depth propagates through the thickness of the pavement section.

As the contact stresses indicate a high possibility of debonding of the three pavement layers, attempts were made to predict the stresses and deflections of the pavement model with the layers unbonded. The interface element behavior was set to “standard” to allow for separation of the layers as well as sliding, as differential curling of the different layers was expected due to the distribution of the temperature gradients.

While test runs with smaller, discrete composite panels successfully modeled the differential curling of smaller, discrete composite panels, convergence difficulties were encountered when modeling the unbonded behavior of the full pavement model developed in this study. In the author’s opinion, the complexity of the expected solution due to the combination of irregular geometry, multiple contact pairs with “standard” interface behavior, and the applied temperature gradients could have contributed to the non-convergence. Due to the lack of time, this portion of the study was not pursued further.

## **PART II—OVERLAY DESIGN METHODOLOGY**

There are a number of existing design procedures that have been or could be used for whitetopping overlay design. At least four different design procedures have been identified in the literature, including those developed by the states of Colorado (Tarr et al. 1998; Sheehan et al. 2004) and New Jersey (SWK Pavement Engineering 1998), the Portland Cement Association (Wu et al. 1998) and the American Association of State Highway and Transportation Officials (AASHTO), or the American Concrete Pavement Association method (American Concrete Pavement Association 1998). Some of the more advanced procedures that have been recently developed include the modified American Concrete Pavement Association (ACPA) procedure (Riley et al. 2005) and the Total Systems Analysis Approach (The Transtec Group 2005) for design of whitetopping pavements. A review of some of these design procedures is presented in the following section.

### **Literature Review of Existing Methods**

#### ***ACPA/PCA Ultra-Thin Whitetopping Design Guidelines***

In 1998, the Portland Cement Association (PCA) and American Concrete Pavement Association (ACPA) sponsored a research study to develop thickness design guidelines for ultra-thin whitetopping (UTW) pavements (Wu et al. 1998). As part of the PCA/ACPA study, thin slabs (2 to 4 in.) with short joint spacings (24 to 50 in.) located at the Spirit of St. Louis Airport in Chesterfield, Missouri, were instrumented with strain gages and loaded using a 20 kip single axle load (SAL). The ultra-thin whitetopping test results indicated that the slab corner was the critical ultra-thin whitetopping load location, and the critical location inducing maximum asphalt strain occurred at the midpoint of the longitudinal joint.

The effects of whitetopping concrete and asphalt interface partial bonding were quantified using the PCA/ACPA study field testing results. Measured field load-induced flexural stresses were compared to fully bonded theoretical stresses to determine an adjustment factor increasing modeled ultra-thin whitetopping load stresses due to the partially bonded condition. A factor of 1.36 (36% increase in stress due to partial bonding) was determined based on the field data. This adjustment factor was applied to stresses computed during a parametric study to convert and adjust modeled stresses to simulate measured field behavior.

Linear regression techniques were then used to develop prediction equations for the ultra-thin whitetopping section critical stresses. The equations included parameters of the whitetopping pavement that have a significant impact on the induced concrete flexural stresses and asphalt flexural strains. The PCA/ACPA design procedure was developed as a guide for determining the Portland cement concrete (PCC) thickness necessary for ultra-thin whitetopping applications in low-volume traffic situations such as intersections, streets, and off ramps.

The development of the UTW design procedure involved the following steps (Riley et al. 2005):

1. Verify the 3-D finite element model by comparing the predicted stresses with the load testing results from the Spirit of St. Louis test pavements.
2. Characterize the degree of bond in the field and correlate that with additional load carrying capacity offered by the asphalt layer.
3. Correlate stresses predicted by the 3-D model and the 2-D model so that the 2-D model could be used to make multiple runs, thereby taking less time.
4. Develop design guidelines:
  - a. Compute load and temperature stresses using the 2-D model under a wide range of parameters
  - b. Convert the 2-D stresses to 3-D stresses based on the correlation in Step 3
  - c. Increase the 3-D stresses by 36 percent to account for the partially bonded condition observed in the field
  - d. Calculate and tabulate both stresses and strains for UTW pavements under different loading and temperature conditions
  - e. Obtain a desired UTW pavement design by limiting both the concrete and asphalt stresses with safe limits given a certain amount of traffic and environmental loadings over the pavement's life

The design parameters and material properties required to determine stresses and strains for a design include the following:

- Concrete thickness (in)
- Joint spacing/slab size (in)
- Concrete flexural strength (psi)
- Concrete modulus of elasticity (psi)
- Asphalt thickness (in)
- Asphalt modulus of elasticity (psi)
- Composite modulus of subgrade reaction (psi)
- Temperature differential between top and bottom of concrete (°F)
- Coefficient of thermal expansion (CTE) of the concrete (in/in/°F)
- Axle load distribution (weights and numbers of axles by type—single, tandem)
- Average daily truck traffic (ADTT)
- Design life (years)
- Fatigue relationship (number of load applications vs. stress ratio)

The PCA/ACPA design method is technically an analysis procedure that allows for the prediction of the number of loads to fatigue failure for a given UTW configuration (Wu et al. 1998). The models used are mechanistic-empirical in nature. Initially, the concrete thickness and joint spacing (slab size) are selected. The procedure then uses these inputs together with other inputs to calculate fatigue of the PCC at the corner of the UTW and fatigue at the bottom of the Hot Mix Asphalt (HMA) under joint loading. Temperature effects are also considered. The final design is reached through an iterative (or trial and error) process.

The design equations for calculating stresses and strains in the development of ACPA's UTW design procedure are as follows:

Asphalt microstrain for 18-kip Single Axle Load (SAL) at joint

$$\log_{10}(\varepsilon_{HMA,18kSAL}) = 5.267 - 0.927 \log_{10} k + 0.299 \log_{10} \left( \frac{L_{adj}}{l_e} \right) - 0.037 l_e \quad (1)$$

Asphalt microstrain for 36-kip Tandem Axle Load (TAL) at joint

$$\log_{10}(\varepsilon_{HMA,36kTAL}) = 6.070 - 0.891 \log_{10} k - 0.786 \log_{10}(l_e) - 0.028 l_e \quad (2)$$

Concrete stress for 18-kip SAL at corner

$$\log_{10}(\sigma_{pcc,18kSAL}) = 5.025 - 0.465 \log_{10} k + 0.686 \log_{10} \left( \frac{L_{adj}}{l_e} \right) - 1.291 \log_{10}(l_e) \quad (3)$$

Concrete stress for 36-kip TAL at corner

$$\log_{10}(\sigma_{pcc,36kTAL}) = 4.898 - 0.599 \log_{10} k + 1.395 \log_{10} \left( \frac{L_{adj}}{l_e} \right) - 0.963 \log_{10}(l_e) - 0.088 \left( \frac{L_{adj}}{l_e} \right) \quad (4)$$

Asphalt microstrain for temperature differential at joint

$$\Delta \varepsilon_{HMA,\Delta T} = -28.698 + 2.131 \alpha_{pcc} \Delta T + 17.692 \left( \frac{L_{adj}}{l_e} \right) \quad (5)$$

Concrete stress for temperature differential at corner

$$\Delta \sigma_{PCC,\Delta T} = 28.037 - 3.496 \alpha_{pcc} \Delta T + 18.382 \left( \frac{L_{adj}}{l_e} \right) \quad (6)$$

where

- $\varepsilon_{HMA,18kSAL}$  = HMA bottom strain due to an 18-kip single-axle load ( $\mu\epsilon$ )
- $\varepsilon_{HMA,36kTAL}$  = HMA bottom strain due to a 36-kip tandem-axle load ( $\mu\epsilon$ )
- $\sigma_{PCC,18kSAL}$  = UTW corner (top) stress due to an 18-kip single-axle load (psi)
- $\sigma_{PCC,36kTAL}$  = UTW corner (top) stress due to a 36-kip tandem-axle load (psi)
- $\Delta \varepsilon_{HMA,\Delta T}$  = Additional HMA bottom strain due to temperature gradient ( $\mu\epsilon$ )
- $\Delta \sigma_{PCC,\Delta T}$  = Additional UTW corner (top) stress due to temperature gradient (psi)
- $\alpha_{PCC}$  = Thermal coefficient of expansion of the PCC ( $\epsilon/^{\circ}F$ )
- $\Delta T$  = Temperature gradient in UTW ( $^{\circ}F$ )
- $L_{adj}$  = Adjusted slab length (in.) defined as  $L_{adj} = 12(8 - [24/((L/12) + 2)])$

$$\begin{aligned}
& k = \text{Modulus of subgrade reaction (psi/in.)} \\
& l_e = \text{Effective radius of relative stiffness for a fully bonded system (in.)} \\
& = \{E_{pcc} * [t_{pcc}^3 / 12 + t_{pcc} * (NA - t_{pcc} / 2)^2] / [k * (1 - \mu_{pcc}^2)] \\
& \quad + E_{ac} * [t_{ac}^3 / 12 + t_{ac} * (t_{pcc} - NA + t_{ac} / 2)^2] / [k * (1 - \mu_{ac}^2)]\}^{0.25} \\
& NA = \text{neutral axis from top of concrete slab (in.)} \\
& = [E_{pcc} * t_{pcc}^2 / 2 + E_{HMA} * t_{HMA} * (t_{pcc} + t_{HMA} / 2)] / [E_{pcc} * t_{pcc} + E_{HMA} * t_{HMA}] \\
& E_{pcc} = \text{Modulus of elasticity of the UTW PCC (psi)} \\
& E_{HMA} = \text{Modulus of elasticity of the HMA (psi)} \\
& t_{pcc} = \text{Thickness of the UTW PCC (in.)} \\
& t_{HMA} = \text{Thickness of the HMA (in.)} \\
& L = \text{Actual joint spacing (in.)}
\end{aligned}$$

For fatigue of the PCC, the PCA fatigue cracking equations (PCA 1984) are used. For a given stress-to-strength ratio (SR), the number of loads to fatigue failure ( $N_{PCC}$ ) is calculated as follows:

$$\begin{aligned}
& \text{For } SR > 0.55 \\
& \log_{10}(N) = (0.97187 - SR) / 0.0828 \quad (7)
\end{aligned}$$

$$\begin{aligned}
& \text{For } 0.45 \leq SR \leq 0.55 \\
& N = (4.2577 / (SR - 0.43248))^{3.268} \quad (8)
\end{aligned}$$

$$\begin{aligned}
& \text{For } SR < 0.45 \\
& N = \infty
\end{aligned}$$

Fatigue damage of the HMA was selected as the second possible failure criterion. For this, the Asphalt Institute (1982) method was employed. The failure criterion for this method is the number of loads that produce cracking in 20% of the wheel path area. The equation is a function of the modulus of elasticity of the HMA ( $E_{HMA}$ ) in psi and the maximum strain at the bottom of the HMA layer ( $\epsilon_{HMA}$ ), as follows:

$$N_{HMA} = 0.0795 * \left( \frac{1}{\epsilon_{HMA}} \right)^{3.29} * \left( \frac{1}{E_{HMA}} \right)^{0.854} \quad (9)$$

The accumulated damage can then be calculated by employing Miner's Hypothesis:

$$\sum_{i=1}^{LoadGroups} \left( \frac{n_i}{N_i} \right) \geq 1 \quad (10)$$

This analysis procedure can be conducted by dividing the expected traffic loading into load groups with single and tandem axles of known weights. The number of loads to fatigue failure in both the HMA and the PCC can be calculated, and the Miner's Hypothesis can be used to determine the fraction of the fatigue life that has been consumed. It should be noted that some of the fatigue life in the HMA may already been

consumed by the trafficking before the UTW overlay; therefore, there may be an initial value of fatigue damage for that failure mode.

The steps involved in the PCA/ACPA design procedure are as follows (Riley et al. 2005):

1. Determine the neutral axis (NA) and radius of relative stiffness ( $l_e$ ).
2. Compute the load-induced concrete stresses and asphalt strains for an 18,000 lb single-axle load (SAL) and a 36,000 lb tandem-axle load (TAL).
3. Use a linear relationship to determine the concrete stress and asphalt strain for all other weights in the axle load distribution category. For example, if the concrete stress under the 18-kip SAL is 187 psi, then the stress under a 20-kip SAL would be  $(20/18) \times 187 = 210$  psi.
4. Compute the temperature-induced concrete stresses and asphalt strains. These values are not load-related and are the same for all axle loads and types.
5. Sum the load-induced and temperature-induced stresses and strains to get total concrete stress and total asphalt strain.
6. Conduct the fatigue analyses. For a given set of parameters, one of the two materials will govern and determine the required thickness and joint spacing. For each axle load, do the following:
  - a. Compute the concrete stress ratio by dividing the total stress by the flexural strength of the concrete.
  - b. Use the stress ratio and fatigue relationship to determine the number of allowable load applications to fatigue failure for the concrete layer.
  - c. Compute the percent of fatigue used.
  - d. Sum the concrete fatigue damage for all axle loads, both single and tandem, and determine if greater than 100 percent.
  - e. Determine the allowable load repetitions for the asphalt layer using the asphalt modulus of elasticity and the calculated microstrains.
  - f. Sum the asphalt fatigue damage for all axle loads, both single and tandem, and determine if greater than 100 percent.
7. If either asphalt or concrete fatigue is greater than 100 percent, alter the design inputs and rerun the analysis.

The benefits and limitations of the PCA/ACPA UTW design procedure are identified in the NCHRP Synthesis 338 (2003).

### Benefits

- The PCA/ACPA design procedure considers the unusual geometry and bond inherent in a UTW overlay, which is not considered in other design procedures, such as those in the AASHTO design guide (ACPA 1998).
- As the design method was developed through the use of a 3-D Finite Element (FE) analysis, it more realistically predicts the pavement responses.
- The method recognizes the importance of bonding characteristics of the UTW to the HMA layer.
- The method was validated through the use of data from a number of field sites.

- The design method uses multiple failure criteria, recognizing the complexity of the UTW system.

### Limitations

- To account for the partial bonding between the PCC and HMA layers, a correction term (multiplier) was derived for the corner stress prediction. However, this stress multiplier is based on a single field test location, making extrapolation prone to error. In addition, the use of a constant correction factor oversimplifies the UTW pavement response under load, especially because a constant value for the HMA resilient modulus was used.
- The current design procedure does not account for reliability in the design. The only exception is an inherent reliability of the stress multiplier.
- In the current design procedure, two modes of failure govern the predicted service life: fatigue cracking at the corner of the UTW and fatigue cracking of the HMA layer beneath the UTW. Although HMA fatigue may be a contributor to UTW distress, HMA alligator cracking in the wheel path, as the model used currently predicts, does not apply, owing to the differences in geometry and loading.
- The developers state that for UTW pavements, “the asphalt layer is covered by concrete slabs, and pavement rutting would not be the governing distress.” However, from observations of UTW overlays in service, this mode of failure does appear to be significant, and it should possibly be considered.
- The procedure contains the requirements for a number of inputs that may be difficult to define accurately by the typical user, including, for example, a “design temperature differential.”
- The current fatigue relationship included in the PCA design method yields results at a high reliability level. However, lower type facilities, such as local roads and city streets, for which UTW was originally conceived for, are designed using reliability levels between 75 and 80 percent. This is less than the in-built reliability in the PCA models. Thus, applying the PCA models will result in excessive UTW thickness, and this makes them less suitable for UTW design (Riley et al. 2005).

### ***Colorado Thin Whitetopping Design Procedure***

The State of Colorado was interested in using thin whitetopping as a technique for rehabilitating deteriorated asphalt highway pavements and, therefore, wanted to adopt the PCA/ACPA whitetopping design procedure. However, the PCA/ACPA design procedure did not include concrete thicknesses and joint spacings Colorado state officials considered acceptable for the highway projects being considered for whitetopping rehabilitation. Therefore, research was initiated to develop thin whitetopping design guidelines for the State of Colorado.

The Colorado Department of Transportation (CDOT) rationale for developing a thin whitetopping design procedure that incorporates stress correction factors was primarily to

take advantage of the partial bonding phenomenon between the concrete and asphalt layers. This would allow the DOT to construct the most economical whitetopping pavements possible and increase the feasibility of thin whitetopping as a rehabilitation technique for asphalt pavements.

Therefore, in 1996, the Colorado Department of Transportation and Portland Cement Association co-sponsored and initiated a research project to develop a mechanistic design procedure for thin whitetopping pavements (Silwferbrand 1997). This project involved construction of three TWT pavements containing many test sections with field instrumentation. TWT sections from 5 to 7 in. thick, with joint spacings of up to 12 ft, were instrumented to measure critical stresses and strains as a result of traffic loads and temperature differentials. Construction Technology Laboratories, Inc. (CTL) installed the instrumentation, conducted the load testing on the instrumented test sections, performed a theoretical analysis, and developed a thin whitetopping design procedure for CDOT. Many variables were considered in the construction of the test sections, including concrete overlay thickness, slab dimension, existing asphalt layer thickness, different asphalt surface preparation techniques, and the use of dowel and tie bars.

The general techniques used in the development of the PCA/ACPA ultra-thin whitetopping design procedure were also used to develop the original Colorado guidelines. Field testing was conducted to evaluate critical load locations for the thicker PCC layer and larger joint spacings. The load-induced flexural strains were used to calibrate fully bonded stresses computed using finite element analysis techniques with partially bonded stresses measured in the field. Load testing was also conducted throughout the course of a day to develop temperature corrections for the load responses. Equations predicting the critical concrete flexural stresses and asphalt concrete strains for use in whitetopping design were developed, and thickness design guidelines were established for partially bonded thin whitetopping pavements using field calibrated theoretical stresses.

In addition to the Colorado mechanistic thin whitetopping design procedure originally developed in 1998 (based on an axle load distributions obtained from traffic monitoring data), the Colorado Department of Transportation also requested that the procedure be converted so that the empirical theory of Equivalent Single Axle Loads (ESALs) could be used as the traffic input information (Sheehan et al. 2004). This required extrapolating AASHTO axle load conversion factors to include typical thin whitetopping thicknesses because the AASHTO design procedure does not suggest conversion factors for a pavement thickness below 6 in. Two ESAL conversion factors were developed based on actual traffic data (for Primary and Secondary Highways) supplied by CDOT for 8 in. thick conventional pavements. In addition to ESAL conversion factors, a nonlinear relationship was realized for PCC thicknesses determined using the empirical (ESAL) and mechanistic (axle load) procedures. An additional conversion factor was derived to equilibrate the empirical and mechanistic design methods.

The development of guidelines for bonded whitetopping during the original 1998 study (Tarr et al. 1998) and the subsequent verification and revision of the design guidelines (Sheehan et al. 2004) included the following elements:



1. The critical load location for the design of whitetopping pavement was determined and verified by comparing the stress data collected for each load position.
2. Critical load-induced stresses were determined when there was approximately a zero temperature gradient.
3. An analysis of experimental and theoretical concrete stresses was made (no temperature gradient). The calibration factor originally developed to adjust theoretical fully bonded stresses to measured partially bonded concrete stresses was revised.
4. An adjustment factor originally developed to convert theoretical fully bonded maximum asphalt flexural strains to partially bonded strains was revised.
5. To account for loss of support with temperature curling effects, an equation was originally derived and presently reviewed that incorporates the percent change in stress (from zero temperature gradient) based on the unit temperature gradient ( $^{\circ}\text{F}/\text{in.}$ ).
6. The calculation of design concrete flexural stress and asphalt strain for a specific set of design parameters involves the following steps:
  - Maximum load-induced concrete stresses and asphalt strains were computed for fully bonded whitetopping pavements using the finite element program ILSL2 (Khazanovich and Ioannides 1993). A wide range of pavement parameters and material properties were originally covered, but additional ILSL2 analyses were performed and incorporated into the current study.
  - Stepwise least squares linear regression techniques were used to derive the original equations to predict concrete stresses and asphalt strains from different pavement parameters and material properties. These equations have been re-derived and the new equations presented based on the 2004 study (Sheehan et al. 2004).
  - Theoretical load-induced concrete stresses are increased to account for the partially bonded condition (step 3 above).
  - Theoretical load-induced asphalt strains are decreased to account for the partially bonded condition (step 4 above).
  - The increased load-induced concrete stresses are adjusted to account for loss of support with temperature curling effects (step 5 above).
7. Whitetopping concrete thicknesses are established by limiting both the concrete flexural stresses and asphalt flexural strains within safe limits under anticipated traffic and environmental conditions during the pavement's design life. The procedure uses fatigue concepts to evaluate the concrete and asphalt layers separately. Therefore, for a given set of pavement parameters and material properties, the concrete or the asphalt layer may govern the design.

In this design procedure, the location of critical stress is hypothesized as being centered along a longitudinal free edge joint, such as a PCC curb and gutter. Because the joints loaded by traffic will most likely not be in a free edge condition, the design procedure considers tied longitudinal joints. The relationship between the free edge stress and tied edge stress is given as follows:

$$\sigma_{FE} = 1.87 * \sigma_{TE} \quad (11)$$

where  $\sigma_{FE}$  is the longitudinal free joint load-induced stress (psi) and  $\sigma_{TE}$  is the load-induced stress at a longitudinal tied joint (psi).

Comparison of the theoretical stresses with the measured tied edge loading stresses showed that the measured stresses are greater than the theoretical stresses. The correction factors are reported as follows:

1998 Original Model (Tarr et al. 1998)

$$\sigma_{ex} = 1.65 * \sigma_{th} \quad (12)$$

2004 Adjusted Model (Sheehan et al. 2004)

$$\sigma_{ex} = 1.51 * \sigma_{th} \quad (13)$$

where  $\sigma_{ex}$  is the measured experimental partially bonded interfacial stresses and  $\sigma_{th}$  is the theoretical fully bonded interfacial stresses.

To assess the PCC-HMA interface, the strains were measured in the top of the HMA pavement and also in the bottom of the PCC slab in the field. It was found that the strain in the HMA is less than the strain in the PCC pavement, which is the result of slippage between the layers. The equations representing the loss of strain are as follows:

1998 Original Model (Tarr et al. 1998)

$$\epsilon_{ac} = 0.842 * \epsilon_{pcc} \quad (14)$$

2004 Adjusted Model (Sheehan et al. 2004)

$$\epsilon_{ac} = 0.897 * \epsilon_{pcc} - 0.776 \quad (15)$$

where  $\epsilon_{ac}$  is the strain in the HMA surface and  $\epsilon_{pcc}$  is the strain in the PCC bottom.

Once the theoretical load-induced stresses are adjusted for the partial bonding condition, the effect of the temperature-induced curling is applied. The relationship derived between the change in stress and measured temperature gradient is as follows:

1998 Original Model (Tarr et al. 1998)

$$\sigma_{\%} = 4.56 * \Delta_T \quad (16)$$

#### 2004 Adjusted Model (Sheehan et al. 2004)

$$\sigma_{\%} = 3.85 * \Delta_T \quad (17)$$

where  $\sigma_{\%}$  is the percent change in stress from zero temperature gradient and  $\Delta_T$  is the temperature gradient ( $^{\circ}\text{F}/\text{in.}$ ).

For the corner and tied edge loading conditions, the following combinations of parameters were investigated for single and tandem axle configurations, resulting in nearly 4000 ILLI-SLAB (ILSL2) analysis runs being performed:

- Joint spacing, L: 48, 72, and 144 in.
- Concrete slab thickness,  $t_{\text{pcc}}$ : 4, 5, 6, and 7 in.
- Asphalt layer thickness,  $t_{\text{ac}}$ : 3, 6, and 9 in.
- Concrete modulus of elasticity,  $E_{\text{pcc}}$ : 4 million psi
- Asphalt modulus of elasticity,  $E_{\text{ac}}$ : 0.05, 0.25, 0.5, 0.75, and 1 million psi
- Concrete Poisson's ratio,  $\mu_{\text{pcc}}$ : 0.15
- Asphalt Poisson's ratio,  $\mu_{\text{ac}}$ : 0.35
- Modulus of subgrade reaction, k: 50, 150, 300, and 500 psi/in.
- Truck axle configuration: single (SAL) and tandem (TAL)
- Slab loading locations: corner and longitudinal edge

As a result of this analysis, design equations were developed for the prediction of PCC stresses from both 20-kip single-axle loads and 40-kip tandem-axle loads. Similar equations were also developed for the HMA strain. All of these equations depend on the effective radius of relative stiffness for the fully bonded slabs. Adjustments are made to the stress equations to account for partial bond and the loss of support as a result of temperature-induced curling. Since the single-axle load concrete stress prediction model developed during the original study (Tarr et al. 1998) does not appear to provide satisfactory predictions of the modeled stresses, revised equations were developed in 2004 (Sheehan et al. 2004). The original and redeveloped prediction equations for computing design concrete flexural stresses and asphalt flexural strains are listed below:

#### 1998 Original Model (Tarr et al. 1998)

Concrete stress for 20-kip SAL

$$\sigma_{\text{pcc}} = 919 + 18,492 / l_e - 575.3 \log k + 0.000133 E_{\text{ac}} \quad (R^2_{\text{adj.}} = 0.99) \quad (18)$$

Concrete Stress for 40-kip TAL

$$\sigma_{\text{pcc}} = 671.2 - 0.000099 E_{\text{ac}} - 437.1 \log k + 1.582 * 104 / l_e \quad (R^2_{\text{adj.}} = 0.99) \quad (19)$$

Asphalt Strain for 20-kip SAL

$$1/\varepsilon_{ac} = 8.51114 * 10^{-9} E_{ac} + 0.008619 l_e/L$$

$$(R^2_{adj.} = 0.99) \quad (20)$$

Asphalt Strain for 40-kip TAL

$$1/\varepsilon_{ac} = 9.61792 * 10^{-9} E_{ac} + 0.009776 l_e/L$$

$$(R^2_{adj.} = 0.99) \quad (21)$$

2004 Revised Model (Sheehan et al. 2004)

Concrete stress for 20-kip SAL

$$(\sigma_{pcc})^{1/2} = 18.879 + 2.918(t_{pcc}/t_{ac}) + 425.44/l_e - 6.955x10^{-6} E_{ac} - 9.0366 \log k + 0.0133L$$

$$(R^2_{adj.} = 0.91) \quad (22)$$

Concrete Stress for 40-kip TAL

$$(\sigma_{pcc})^{1/2} = 17.669 + 2.668(t_{pcc}/t_{ac}) + 408.52/l_e - 6.455x10^{-6} E_{ac} - 8.3576 \log k + 0.00622L$$

$$(R^2_{adj.} = 0.92) \quad (23)$$

Asphalt Strain for 20-kip SAL

$$(\varepsilon_{ac})^{1/4} = 8.224 - 0.2590(t_{pcc}/t_{ac}) - 0.04419l_e - 6.898x10^{-7} E_{ac} - 1.1027 \log k$$

$$(R^2_{adj.} = 0.81) \quad (24)$$

Asphalt Strain for 40-kip TAL

$$(\varepsilon_{ac})^{1/4} = 7.923 - 0.2503(t_{pcc}/t_{ac}) - 0.04331l_e - 6.746x10^{-7} E_{ac} - 1.0451 \log k$$

$$(R^2_{adj.} = 0.82) \quad (25)$$

where

$\sigma_{pcc}$  = maximum stress in the concrete slab, psi  
 $\varepsilon_{ac}$  = maximum strains at bottom of asphalt layer, microstrain  
 $E_{pcc}$  = concrete modulus of elasticity, assumed 4 million psi  
 $E_{ac}$  = asphalt modulus of elasticity, psi  
 $t_{pcc}$  = thickness of the concrete layer, in.  
 $t_{ac}$  = thickness of the asphalt layer, in.  
 $\mu_{pcc}$  = Poissons ratio for the concrete, assumed 0.15

$\mu_{ac}$  = Poissons ratio for the asphalt, assumed 0.35  
 $k$  = modulus of subgrade reaction, pci  
 $le$  = effective radius of relative stiffness for fully bonded slabs, in.  
 $= \{E_{pcc} * [t_{pcc}^3 / 12 + t_{pcc} * (NA - t_{pcc} / 2)^2] / [k * (1 - \mu_{pcc}^2)] + E_{ac} * [t_{ac}^3 / 12 + t_{ac} * (t_{pcc} - NA + t_{ac} / 2)^2] / [k * (1 - \mu_{ac}^2)]\}^{0.25}$   
 $NA$  = neutral axis from top of concrete slab, in.  
 $= [E_{pcc} * t_{pcc}^2 / 2 + E_{ac} * t_{ac} * (t_{pcc} + t_{ac} / 2)] / [E_{pcc} * t_{pcc} + E_{ac} * t_{ac}]$   
 $L$  = joint spacing, in.

Both PCC and HMA fatigue relations were used as failure criteria in this procedure. The PCA fatigue criterion (PCA 1984) based on Miner's hypothesis was incorporated for PCC fatigue. This PCC fatigue criterion is as follows:

For  $SR > 0.55$

$$\text{Log}_{10}(N) = (0.97187 - SR) / 0.0828 \quad (26)$$

For  $0.45 \leq SR \leq 0.55$

$$N = (4.2577 / (SR - 0.43248))^3 \quad (27)$$

For  $SR < 0.45$

$$N = \infty$$

where  $SR$  is flexural stress-to-strength ratio and  $N$  is the allowable number of load repetitions.

The HMA pavements are generally designed based on two criteria: asphalt concrete fatigue and subgrade compressive strain to control pavement rutting. According to the developers, pavement rutting should not be the governing distress in whitetopping pavements since concrete slabs cover the asphalt layer in whitetopping pavements. Therefore, HMA fatigue was used as the design criterion in developing the Colorado design procedure. For the HMA fatigue, the number of allowable loads is a function of the maximum tensile strain in the HMA layer, the HMA modulus of elasticity, and the volume of binder and air voids. The amount of fatigue damage that the HMA has sustained before whitetopping construction is also considered. The asphalt concrete fatigue equation developed by the Asphalt Institute (1981) was employed in the development of the whitetopping design procedure. The HMA fatigue equation is as follows:

$$N = C * 18.4 * (4.32 \times 10^{-3}) * (1 / \epsilon_{ac})^{3.29} * (1 / E_{ac})^{0.854} \quad (28)$$

where

$N$  = number of load repetitions for 20% or greater AC fatigue cracking

$\epsilon_{ac}$  = maximum tensile strain in the asphalt layer

$E_{ac}$  = asphalt modulus of elasticity, psi

$C$  = correction factor =  $10^M$

$$M = 4.84 * [(V_b / (V_v + V_b) - 0.69]$$

$V_b$  = volume of asphalt, %

$V_v$  = volume of air voids, %

The following concerns were identified after a subsequent review of Colorado whitetopping design procedure (NCHRP 2003):

- TWT overlay thickness is substantially dependent on the subgrade modulus of reaction (k).
- TWT thickness is also sensitive to the HMA stiffness and thickness. It was stated in the procedure that the thickness of the HMA layer should not be less than 5 inches.
- TWT thickness is not sensitive to the number of 18-kip ESALs for greater than 1 million applications. However, when the loads increase, the stiffness of the HMA becomes a more significant factor. For traffic loading greater than 4 million ESALs, TWT should not be specified if the HMA modulus is less than 400 ksi.
- No guidance is provided on the proper selection of the design temperature gradient.
- The 2004 revised thin whitetopping design procedure is more sensitive than the original procedure to existing pavement subgrade characteristics, asphalt properties, and future traffic volumes. There does not appear to be specific minimum values for subgrade support or asphalt thickness necessary (as was the case for the original study).
- Due to the sensitivity of the revised thin whitetopping procedure to design procedure input parameter values, it is critical to evaluate and quantify the existing pavement conditions (i.e., subgrade support, existing asphalt modulus and thickness, remaining asphalt concrete fatigue life, anticipated traffic volumes and distributions) to get a realistic estimate of required whitetopping thickness using the revised design procedure.

### ***Illinois (Riley et al. 2005)***

Illinois first researched the experimental use of whitetopping in 1998 with the construction of three intersection projects (Winkelman 2005). Since those first three intersections, the process has been used on several more state maintained intersections and highways, as well as numerous local agency roadways and privately owned facilities. According to Pavement Technology Advisory-Whitetopping-PTA-M4 (Eff. 8/2000, Rev. 02/2005), the Illinois Department of Transportation (IDOT) has not adopted a standard design procedure for developing whitetopping overlay thickness.

In the PCA/ACPA UTW design procedures, the development of the original models for PCC fatigue included utilization of the existing fatigue relations developed by PCA (1984). According to Riley et al. (2005), the underlying assumptions in the PCA fatigue models result in an unstated, conservative factor of safety in all UTW designs developed using this procedure. In other words, the use of PCA fatigue curve imparts very high

levels of design reliability compared to those normally used for the design of local and secondary roads for which UTW was originally intended. An effort was undertaken to incorporate probabilistic concepts into the existing fatigue models (Riley et al. 2005). Approximate comparisons were made with several existing projects constructed in Illinois as a base of reference for the revised models.

To select an appropriate methodology for incorporating reliability into fatigue relationships, several studies from the literature were reviewed. It was found that a methodology proposed by McCall (1958) for incorporating probability of failure or survival into fatigue analysis and predictions of  $N$  was successfully applied in several studies. The relationship proposed by McCall is as follows:

$$\log N = \left[ \frac{-SR^{-\alpha} \log(1-p)}{\beta} \right]^{\gamma} \quad (29)$$

where  $N$  is the number of load repetitions,  $SR$  is stress ratio,  $p$  is the probability of failure and  $1-p$  is the probability of survival, and  $\alpha$ ,  $\beta$ , and  $\gamma$  are regression constants. The methodology proposed by McCall (1958) was judged to be most appropriate and formed the basis for incorporating reliability into fatigue predictions in the model developed by Riley et al. (1995).

The first step in model development consisted of assembling data from various sources. The data elements of interest for model development were applied stress, PCC strength at testing, stress ratio, the number of load applications to failure, and information indicating whether the test specimen failed at the time testing was terminated. Data for analysis were obtained from the ACPA and several published reports and literature.

The calibration of the selected model using the assembled data consisted of the following steps:

1. Group the fatigue data into categories of  $SR$
2. For each  $SR$  category, perform survival analysis and determine the probability of survival of a PCC beam subjected to fatigue at the prescribed stress ratio level
3. Assemble a database of probability of survival and  $N$  for the categories of  $SR$  established.
4. Perform nonlinear regression using the data obtained in step 3 to determine model coefficients for the selected  $N$  prediction model (Equation 29).
5. Verify the tentative model, modify as needed, and determine final model coefficients.

The result of the calibration effort was the development of a tentative model as follows:

$$\log N_f = \left[ \frac{-SR^{-10.24} \log(1-p)}{0.0112} \right]^{0.217} \quad (30)$$

The model statistics were as follows:

- $N = 87$
- $R^{2*} = 91$  percent ( $R^2$  computed from predicted and measured  $\log N = 91\%$ )
- $RMSE = 0.31$

The model verification consisted of reviewing the diagnostic statistics and conducting a sensitivity analysis. A comparison of the model developed during this study and other past studies with the current PCA model indicated that predicted  $\log N_f$  from the PCA model is the most conservative.

Since the fatigue data upon which the original design procedure and the revised procedure incorporating reliability are based is essentially similar, the same limitations to interpretation apply. In order to obtain a comparison of the results, several calculations were completed using the old procedure.

Using the existing fatigue relationship, the maximum number of loads the section could carry until fatigue capacity of the concrete or the asphalt was reached was calculated. Next, analyses were completed at 90% and 95% reliability using the new fatigue relationship to contrast that with the prior model based on the old fatigue relationship. As expected, at 90% reliability, several of the calculated loads for given conditions were less conservative than those associated with the published fatigue curve, whereas at 95% reliability, the loads are, in general, more conservative (Riley et al. 2005).

The results from the revised procedure were then compared with field experience. A number of whitetopping and UTW pavements have been built in Illinois. Since the results from this analysis are based largely on theoretical concepts, an attempt was made to compare results from the revised procedure with results obtained from the IDOT projects in Illinois. By using the new models with parameters typical of Illinois and converting an ACPA category B traffic distribution to ESALs, a rough comparison was made to see if the pavements are performing at least as well as might be forecast using the revised procedure at a 90% level of reliability (ACPA 2002). Additional comparisons were completed using the data published from the Federal Highway Administration's (FHWA) accelerated loading facility (ALF) test results (ACPA 2003).

Results from the projects considered generally indicated that all of the designs reviewed with the limited information available would meet the above criteria; though, it may be somewhat early to tell for all of the sections. The data from the ALF testing is more certain and meets the aforementioned criteria. Other conventional whitetopping projects in Illinois were not considered since they fall outside the normal limits of UTW of 2 to 4 in. The models were not developed for that range, but may later be reviewed for possibility of extrapolation to infer likely performance.

It is noted that no attempt has been made to address the fatigue of the asphalt in the paper by Riley et al. (2005). For many of these analyses, failure in the asphalt layer drove the maximum number of loads carried. It was suggested by the authors that the asphalt



fatigue relationship remains unchanged and warrants further study if an overall probabilistic relationship is desired. In its present form, the developed procedure allows some degree of assurance against failure by fatigue of the concrete when constructed as a UTW overlay.

### ***Transtec Overlay Design***

The Transtec Group, under sponsorship from the Innovative Pavement Research Foundation (IPRF), is currently developing a new state-of-the-art design procedure for whitetopping pavements. Employing a *Total Systems Analysis Approach*, the development of the new design procedure began with an in-depth study of the various failure modes that could develop in all classes of whitetopping. This approach includes the means not only to optimize the design thickness, but also to optimize other key variables such as the joint spacing, mix design, and surface preparation technique. A brief description of the upcoming whitetopping design guidelines is presented here.

This approach employs 18 unique steps, illustrated in Figure 33. Each cell in this figure is described below. The end result of this approach is the ability to make a side-by-side comparison of various alternatives which, using conventional design techniques, could not be accomplished.

#### **Step 1—User Inputs**

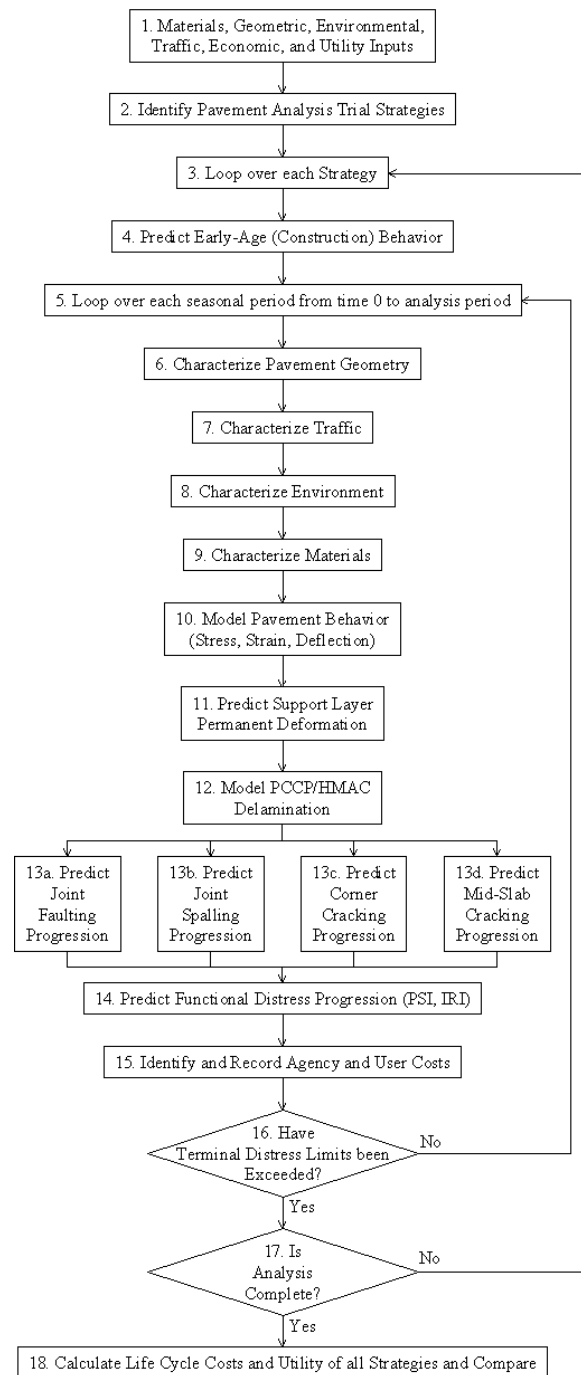
In the first step, the various user inputs are defined under seven categories: (1) general, (2) materials, (3) geometry, (4) environment, (5) traffic, and (6) economic. Each of these categories contains a number of variables that can be defined by the user. The developers acknowledge that a balance must be made between the accuracy of the software and the complexity of the inputs.

#### **Step 2—Strategy Selection**

Once the user has identified the various inputs, the strategies to be analyzed must be defined. Traditional pavement design tools will often only provide a single result—minimum thickness required to achieve a specified performance based on a small number of criteria. However, this design system is a systems analysis tool. This type of tool has the flexibility to provide the user with much more power to make the types of decisions that are critical during the pavement design.

#### **Step 3—Loop over Each Strategy**

The software tool that implements this design guide will begin the analysis by looping over each selected strategy. For example, if three different strategies were selected, the program will run three times.



**Figure 33. Schematic of framework to optimizing whitetopping design (The Transtec Group 2005)**

#### Step 4—Predict the Early-Age Behavior

Characterizing the early-age behavior of the concrete is critical to accurately predict its expected performance. The early-age period is often defined as the first 48 to 96 hours after construction. At this time, the PCC strength is relatively low, and the stresses in the slab can be significant due to the large volumetric changes that occur due to temperature

and moisture conditions in the slab. This is especially true for UTW slabs due to the high surface area to volume ratio. Algorithms from the FHWA HIPERPAV™ analysis tool will be selected to predict the early-age behavior.

#### Step 5—Loop over Each Seasonal Period

This step includes one of the characterizing elements of this unique approach. The essence of a systems analysis tool is to predict the various paving strategies as realistically as possible. This simulation is done in a chronological fashion by looping over each season from the initial construction season up to the last season of the user-defined analysis period. During this simulation, the various distresses will be predicted incrementally, and the resulting performance can then be derived from this distress history. Unlike traditional design tools, the process described here has the flexibility to compare various strategies side-by-side.

#### Step 6—Characterize Pavement Geometry

Using the various user inputs, the geometry of the pavement system is characterized in this step. This primarily involves characterizing the various layer thicknesses, so it is relatively straightforward.

#### Step 7—Characterize Traffic

The traffic for the current period is defined in this step. Adjustments to the traffic are made as follows:

- Axle-load spectra. The simulation will be performed over the full range of anticipated axle-load spectra. An integration of the number of axles by the distress due to each axle load will be made to predict the overall incremental distress.
- Seasonal distribution of traffic. For example, higher traffic may be experienced during the summer months on some facilities; therefore, an adjustment is made to reflect this effect.
- Growth. The traffic level will generally increase with time. An adjustment will be made to reflect the growth function as defined by the user. Three growth functions are provided—linear, exponential, and logistic (s-shaped) growth.
- Time of day. The simulation also loops over the time of day. This effect is important since the deflected shape of the pavement will differ from day to night, and therefore will impact the predicted traffic-induced stresses. The user can define either a functional class or an hourly traffic distribution to better define the traffic volumes during different times of the day.

#### Step 8—Characterize Environment

Various user inputs are needed to characterize the ambient environmental conditions at the specified location for the design. In order to minimize the burden to the user, these inputs will be made using a sophisticated GIS-based interface. When a location for the

design is selected, an extensive 600-megabyte database is queried for weather data from weather stations in the vicinity of the specified location.

Using an intelligent algorithm, the most relevant weather stations are selected, and the weather information for the specified location is calculated based on a weighted interpolation scheme. The database actually contains mean hourly readings for the entire year (based on 30 years of data) for each of the specified stations. For simplicity, these values are reduced seasonal means. In addition, the database contains the variances for each of these factors in order to better characterize the stochastic nature of weather phenomena.

Using the ambient environmental inputs along with the materials inputs, the temperature profiles in the pavement system will be predicted using a finite-difference algorithm, similar to that of the Integrated Climate Model (ICM) developed for the FHWA. The remaining characterization, behavior, and distress models in the systems analysis, in turn, will use these profiles.

#### Step 9—Characterize Materials

Contrary to most pavement design methods, the key properties of paving materials to predict pavement performance are not static values. Although, most design procedures simplify the characterization of materials properties such as modulus and strength, the systems analysis approach to pavements does not require this assumption to be made. This is quite beneficial since most of the key properties are a function of dynamic variables such as temperature, moisture, cumulative damage, and time.

For example, the software will use two unique models to predict the concrete strength and modulus. The first model is based on maturity methods and would be used during the early-age analysis (Step 4), and the second model is based on a more general form and would be used for subsequent analysis period (Step 9).

#### Step 10—Model Pavement Behavior

Pavement behavior modeling is a controversial issue—primarily among academia, but also among practitioners who are simply asking for the “right answer.” Over the years, many models have been developed to predict the responses of a pavement system due to both environmental and traffic loading. Regarding whitetopping, pavement responses of interest include the following:

- Critical stresses in the whitetopping layer—corner stresses and edge stresses
- Deflections and strains in the whitetopping layer at the corner and the edge
- Stresses and strains in the HMA support layer
- Stresses and strains in the base and subgrade layers
- Delamination stresses and strains (which will be covered in more detail in step 12).

Coming up with the “right answer” is quite difficult, however. The types of models range widely. On one extreme are simple closed-form solutions such as those developed by Westergaard and refined by Bradbury in the early part of last century. On the other extreme are dynamic, non-linear three-dimensional finite element prediction models. One trade-off between these models, and everything in between, is run-time versus accuracy.

Closed-form solutions may be easy to program and implement into a system such as this, but their accuracy is limited due to the simplicity of the inputs and the inherent assumptions. Three-dimensional finite element models, on the other hand, require tremendous computing power and are beyond reasonable feasibility at this time for integration into the systems analysis tool during run-time. The Transtec Group project team believes that it will provide the "best of both worlds" in the current approach.

The response model will be a hybrid “2½D” model consisting of a non-linear two-dimensional (2-D) finite element model foundation. This model will be modified via simplified correction models developed using a non-linear three-dimensional (3-D) FEM.

#### Step 11—Predict Support Layer Permanent Deformation

In thinner whitetopping pavements, failures that have been observed are often caused, either directly or indirectly, by a loss of support due to permanent deformations in the support layers. In some cases, the permanent deformation is in the HMA layer directly beneath the whitetopping. In other pavements, the failure may be in the base, or even in the subgrade.

Predicting the progression of permanent deformations in the support layers accurately is a key element in the overall systems analysis approach. This prediction model will set up the boundary conditions necessary to predict the response of the whitetopping layer in subsequent periods.

#### Step 12—Model Whitetopping-HMA Delamination

Whitetopping layers are traditionally designed and analyzed based on the assumption that a bond exists between the concrete and the HMA layers. However, a number of factors contribute to the deterioration of the bond between these layers:

- Upward warping of the slab corners and edges due to moisture loss from the top portion of the PCC slab
- Upward curling of the slab corners and edges due to negative temperature gradients in the PCC slab
- Axial shrinkage of the slab due to drying shrinkage
- Axial shrinkage or expansion of the slab due to changes in slab temperature
- Traction forces caused by passing wheel loads
- Dynamic forces of passing wheel loads
- Shrinkage of the support layers due to moisture changes
- Permanent deformation of the support layers
- Swelling of the support layers

- Healing of the HMA
- Relaxation creep in the PCC slab

The characterization and, furthermore, the interaction of these variables is quite complex. However, many of these parameters can be modeled and will be incorporated into the systems analysis.

The bond between the HMA and the concrete layers must resist delamination forces. A state of stress can be modeled at the interface using a number of models. To compare to this predicted stress, two “strengths” must be considered:

1. The bond strength of the interface between the HMA and the PCC layers
2. The strength of the HMA, considering factors such as the loading rate, stress state, and temperature.

The weakest of these strengths will govern the delamination of the layers.

#### Step 13—Model Whitetopping Structural Distresses

From the observations of the project team, four key structural distresses have noted to be predominant in whitetopping pavements to date. These include the following distresses:

- Joint Faulting—the vertical separation of adjacent slabs that is due to many factors, including poor load transfer and loss of support.
- Joint Spalling—a localized failure along a joint where pieces of PCC have failed and broken away from the slab. There are two primary sources of spalling distress—deflection-related and delamination-related. The former is caused by high deflections in the slab that create high shear stresses in the top layer of the slab at the joint, resulting in a localized failure. Delamination spalling is often caused by significant moisture loss from the slab resulting in weak horizontal planes, which then fail under subsequent traffic loading.
- Corner Cracking—a cracking failure in the vicinity of the slab corner.
- Mid-Slab Cracking—a cracking failure that occurs in the middle of a slab. This type of cracking can occur due to either high volumetric changes in the PCC, coupled with high restraint, or by fatigue due to repeated traffic loading.

#### Step 14—Predict Functional Distress Progression in Whitetopping

Although the prediction of structural distresses is a key factor in a mechanistic-based analysis system, it is highly recommended that a means to predict the functional distress also be provided. The two primary indicators in use today to quantify the functional distress are the Present Serviceability Index (PSI) and the International Roughness Index (IRI).

#### Step 15—Identify and Record Agency and User Costs

At the end of the analysis cycle, the agency and user costs will be calculated for the current period. The former requires little modeling—only a good "bookkeeping" routine that will accrue the construction costs to the agency. The user costs, however, require a more sophisticated model. This model will account for the traffic volumes, time of day of the maintenance, and other items which relate to the impact to the traffic.

#### Step 16—Check to see if Distress Limits have been Exceeded

This step will conduct an evaluation of the current state of the pavement. If the simulation has predicted a level of distress that the user denotes as being "terminating" in nature, the analysis will complete. This, in essence, allows the analysis period to be shortened to eliminate analysis options that do not meet the basic minimum criteria set by the user.

As an extreme example, if a one-inch whitetopping is selected for construction over an HMA of poor condition subjected to very heavy traffic loading, it will intuitively not reach an analysis period of 15 years. In this case, the program will drop out of the analysis when the maximum terminating level of distress is exceeded. It is also at this point that the loop completes to advance to the next season to be simulated. As mentioned in step 5, each strategy will be simulated over the analysis period as defined by the user.

#### Step 17—Check to see if Analysis is Complete

If each of the strategies that the user had selected for the systems analysis has been executed and simulated, the analysis will terminate. If not, the analysis will continue to loop through to the next strategy.

#### Step 18—Calculate and Compare Life-Cycle Costs for all Strategies

This step includes the use of sophisticated life-cycle cost analysis (LCCA) techniques to predict values that can immediately be used by the user to compare the alternative strategies.

A comparison of the whitetopping design procedures discussed in this section is made in Table 16.

**Table 16. Comparison of whitetopping design procedures**

<b>Design Procedure</b>	<b>Required User Inputs</b>	<b>Stresses and Strains (Structural Responses)</b>	<b>Failure Criteria</b>
ACPA/PCA	<ul style="list-style-type: none"> <li>• Concrete thickness (in.)</li> <li>• Joint spacing/slab size (in.)</li> <li>• Concrete flexural strength (psi)</li> <li>• Concrete modulus of elasticity (psi)</li> <li>• Asphalt thickness (in.)</li> <li>• Asphalt modulus of elasticity (psi)</li> <li>• Composite modulus of subgrade reaction (psi)</li> <li>• Asphalt Poisson's ratio</li> <li>• Concrete Poisson's ratio</li> <li>• Temperature differential between top and bottom of concrete (°F)</li> <li>• Coefficient of thermal expansion (CTE) of the concrete (in./in./°F)</li> <li>• Axle load distribution (weights and numbers of axles, by type – single, tandem)</li> <li>• Average daily truck traffic (ADTT)</li> </ul>	<ul style="list-style-type: none"> <li>• Asphalt concrete bottom strain (18-kip SAL, 36-kip TAL)</li> <li>• UTW corner (top) stress (18-kip SAL, 36-kip TAL)</li> <li>• Additional asphalt concrete bottom strain due to temperature gradient</li> <li>• Additional UTW corner (top) stress due to temperature gradient</li> </ul>	<ul style="list-style-type: none"> <li>• PCA Fatigue Cracking Equation (PCA 1984)</li> <li>• AC fatigue (The Asphalt Institute 1981)</li> </ul>
Colorado	<ul style="list-style-type: none"> <li>• Concrete thickness (in.)</li> <li>• Joint spacing/slab size (in.)</li> <li>• Concrete flexural strength (psi)</li> <li>• Concrete modulus of elasticity (psi)</li> <li>• Asphalt thickness (in.)</li> <li>• Asphalt modulus of elasticity (psi)</li> <li>• Modulus of subgrade reaction (psi)</li> <li>• Asphalt Poisson's ratio</li> <li>• Concrete Poisson's ratio</li> <li>• Axle load distribution (weights and numbers of axles, by type – single, tandem)</li> </ul>	<ul style="list-style-type: none"> <li>• Maximum strain at the bottom of the asphalt layer (20-kip SAL, 40-kip TAL)</li> <li>• Maximum stress in the concrete slab (20-kip SAL, 40-kip TAL)</li> </ul>	<ul style="list-style-type: none"> <li>• PCA Fatigue Cracking Equation (PCA 1984)</li> <li>• AC fatigue (The Asphalt Institute 1981)</li> </ul>



**Table 16. (continued)**

<b>Design Procedure</b>	<b>Required User Inputs</b>	<b>Stresses and Strains (Structural Responses)</b>	<b>Failure Criteria</b>
Illinois (Riley et al. 2005)	<ul style="list-style-type: none"> <li>• Same as ACPA</li> </ul>	<ul style="list-style-type: none"> <li>• Same as ACPA</li> </ul>	<ul style="list-style-type: none"> <li>• Probabilistic fatigue model based on PCA fatigue curve (Riley et al. 2005)</li> <li>• AC fatigue (The Asphalt Institute 1981)</li> </ul>
Transtec Overlay Design	<ul style="list-style-type: none"> <li>• General</li> <li>• Materials (dynamic properties, concrete strength based on maturity methods, etc.)</li> <li>• Geometry (layer thicknesses, joint spacing, etc.)</li> <li>• Environment (similar to ICM)</li> <li>• Traffic (axle-load spectra, seasonal distribution, growth, time of day)</li> <li>• Economic</li> </ul>	<ul style="list-style-type: none"> <li>• Critical Stresses in the Whitetopping layer – Corner Stresses and Edge Stresses</li> <li>• Deflections and Strains in the Whitetopping Layer at the Corner and the Edge</li> <li>• Stresses and Strains in the HMA Support Layer</li> <li>• Stresses and Strains in the Base and Subgrade Layers</li> <li>• Whitetopping-HMA Delamination Stresses and Strains</li> </ul>	<ul style="list-style-type: none"> <li>• Predict structural/functional distress progression in whitetopping similar to the MEPDG (Mechanistic-Empirical Pavement Design Guide) <ul style="list-style-type: none"> <li>○ Joint faulting</li> <li>○ Joint spalling</li> <li>○ Corner cracking</li> <li>○ Mid-slab cracking</li> <li>○ PSI</li> <li>○ IRI</li> </ul> </li> </ul>

## **Mechanistic Whitetopping Thickness Design Procedure**

The Colorado DOT (CDOT) thin whitetopping procedure and the Portland Concrete Association (PCA) ultra-thin whitetopping procedure both outline methods for designing a thin concrete overlay on top of an existing Asphaltic Concrete (AC) pavement. However, many of the roads in Iowa and other states consist of Portland Cement Concrete (PCC) pavements overlaid with AC. This is done in order to extend the service life of the pavement. This section outlines a process to evaluate the existing pavement conditions and determine the parameters required to apply the CDOT and PCA design procedures.

### **Evaluation of the Existing Pavement**

To evaluate the existing conditions of the composite (AC/PCC) pavement, visual inspection and deflection testing should be conducted. Deflection testing is performed with a FWD and load magnitude of 9000 pounds. The deflection testing should be done in enough intervals that will allow for an adequate evaluation of the pavement. Measurements taken from sensors, located at 0, 12, 24, and 36 inches from the center of the load plate, are adjusted for temperature effects on the AC moduli and standardized for a load of 9000 lbs. These results are used to compute the maximum deflection ( $d_0$ ) and the deflection basin AREA. The parameters or layer moduli of the existing AC/PCC pavement are then backcalculated using the two values (Hall and Darter 1994).

### ***Temperature Effects***

In order to account for temperature effects during load testing, temperature of the AC layer must be monitored. An alternative method to determine the temperature of the AC using the mean monthly air temperature was developed by Witczak and is shown below (Asphalt Institute 1982).

$$T_{ac} = MMAT \left( 1 + \frac{1}{z + 4} \right) - \frac{34}{z + 4} + 6 \quad (31)$$

where

$T_{ac}$  = mean temperature of the asphalt layer

$MMAT$  = mean monthly air temperature

$z$  = 1/3 depth from the surface of the asphalt, inches

### ***Asphalt Modulus***

A large portion of the total deflection can be attributed to the vertical compression of the AC layer under the 9000 lb load. To determine the amount of compression in the asphalt, the AC elastic modulus needs to be calculated. The method outlined below uses the Asphalt

Institute's (AI) equation for the AC modulus. The AI equation is a function of mix characteristics, mix temperature, and loading frequency. It is considered to be very reliable for dense-graded ACC mixes made up of gravel or crushed stone aggregates.

$$\begin{aligned} \log E_{ACC} = & 5.553833 + 0.028829 \left( \frac{P_{200}}{F^{0.17033}} \right) - 0.03476 * V_v \\ & + 0.070377 * \eta + 0.000005 * T_{ac}^{(1.3+0.49825*\log F)} * P_{ac}^{0.5} - \left( \frac{0.00189}{F^{1.1}} \right) \\ & * T_{ac}^{(1.3+0.49825*\log F)} * P_{ac}^{0.5} + 0.931757 * \left( \frac{1}{F^{0.02774}} \right) \end{aligned} \quad (32)$$

where,

$E_{AC}$  = elastic modulus of AC, psi  
 $P_{200}$  = percent aggregate passing the No. 200 sieve  
 $F$  = 18 Hz for the FWD load duration of 25 to 30 milliseconds  
 $V_v$  = percent air voids  
 $P_{ac}$  = asphalt content, percent by weight of mix  
 $T_{ac}$  = mean AC mix temperature at 1/3 depth, °F  
 $\eta$  = absolute viscosity at 70°F,  $10^6$  poise

Also, aging of the asphalt needs to be evaluated using the following equations developed by Ullidtz. Equation 33 should be used to determine an aged penetration of the binder at 25°C (77°F).

$$\text{aged pen}_{25} = 0.65 * \text{original pen}_{25} \quad (33)$$

If there is not sufficient information available to determine the absolute viscosity, an alternate method is shown in the following equation.

$$\eta = 29508.2 * (\text{aged pen}_{25})^{-2.1939} \quad (34)$$

### ***Backcalculation of the Subgrade K-Value and Concrete Modulus***

Backcalculation of the layer moduli was developed by Hall and Darter in order to learn more about the performance and evaluate ACC/PCC pavements. The first step of the procedure is to remove the effect of the AC layer from the measured deflections. This is done by calculating the asphalt modulus using AI method. The next step is to calculate the vertical compression,  $d_{0v}$ , of the ACC layer when the load is applied to the pavement. Depending on the assumed bond conditions, either Equation 35 or Equation 36 should be used.

AC/PCC Bonded

$$d_{0_{compress}} = -0.0000328 + 121.5006 * \left( \frac{D_{ac}}{E_{ac}} \right)^{1.0798} \quad (35)$$

AC/PCC Unbonded

$$d_{0_{compress}} = -0.00002132 + 38.6872 * \left( \frac{D_{ac}}{E_{ac}} \right)^{0.94551} \quad (36)$$

where

$d_{0_{compress}}$  = AC compression at center of load, in

$D_{ac}$  = AC thickness, in

$E_{ac}$  = AC elastic modulus, psi

After the compression of the AC layer at the center of the load is calculated, this value is subtracted from the maximum deflection ( $d_0$ ) measured by the FWD in order to find the deflection of the PCC layer.

$$d_{0_{PCC}} = d_0 - d_{0_{compress}} \quad (37)$$

where

$d_{0_{compress}}$  = vertical compression of the AC layer, in

$d_0$  = maximum deflection at center of load plate, in

$d_{0_{PCC}}$  = deflection of the PCC layer, in

Now that the asphalt layer has been accounted for, the procedure follows regular backcalculation techniques:

1. Calculate the area of the deflection basin under PCC slab using the  $d_0$  calculated above and the  $d_{12}$ ,  $d_{24}$ , and  $d_{36}$  measured at the AC surface.

$$AREA_{PCC} = 6 * \left( 1 + 2 * \left( \frac{d_{12}}{d_{0_{PCC}}} \right) + 2 * \left( \frac{d_{24}}{d_{0_{PCC}}} \right) + \left( \frac{d_{36}}{d_{0_{PCC}}} \right) \right) \quad (38)$$

where

$AREA_{PCC}$  = area of the deflection basin, in

$d_{0_{PCC}}$  = deflection of the PCC layer at center of load plate, in

$d_i$  = deflection at distance  $i$  from the center of the load plate, in

2. Calculate the radius of relative stiffness ( $l$ ).

$$l = \left[ \frac{\ln \left( \frac{36 - AREA_{PCC}}{1812.279} \right)}{-2.559} \right]^{4.387} \quad (39)$$

3. Calculate the  $L/l$ .  $L$  is the least slab dimension divided by  $l$  calculated in #2.
4. The above backcalculation procedure uses Westergard's equation for deflection of an infinite plate on a dense liquid foundation. However, many slabs are too small to approximate infinite slab behavior. Therefore if the  $L/l$  resulting value is less than eight, the following corrections must be performed to the maximum deflection and radius of relative stiffness.

$$AF_{d_0} = 1 - 1.0687 * e^{-0.66914 * \left(\frac{L}{l}\right)^{0.84408}} \quad (40)$$

$$AF_l = 1 - 5.29875 * e^{-2.17612 * \left(\frac{L}{l}\right)^{0.49895}} \quad (41)$$

$$\text{adjusted } d_0 = AF_{d_0} * \text{measured } d_0 \quad (42)$$

$$\text{adjusted } l = AF_l * \text{calculated } l \quad (43)$$

5. Calculate the  $k$ -value using Westergard's deflection equation.

$$k = \left( \frac{P}{8 * d_0 * l^2} \right) \left\{ 1 + \left( \frac{1}{2\pi} \right) \left[ \ln \left( \frac{a}{2 * l} \right) + \gamma - 1.25 \right] \left( \frac{a}{l} \right)^2 \right\} \quad (44)$$

where

$k$  = effective modulus of subgrade reaction, pci (dynamic)

$d_0$  = adjusted maximum deflection  $d_0$ , in

$l$  = adjusted radius of relative stiffness

$P$  = FWD load, pounds

$\gamma$  = Euler's constant, 0.57721566490

$a$  = load radius, 5.9 inches for the FWD

6. Using the definition of  $l$  and dividing the  $k$ -value by two, the concrete elastic modulus may be determined.

$$E_{PCC} = \frac{12 * (1 - \mu_{PCC}^2) * k * l^4}{D_{PCC}^3} \quad (45)$$

where

$E_{PCC}$  = estimated elastic modulus of the existing PCC, psi

$\mu_{PCC}$  = Poisson's ratio of the PCC

$k$  = effective modulus of subgrade reaction, pci (static)

$l$  = adjusted radius of relative stiffness

$D_{PCC}$  = thickness of the existing PCC slab, in

This backcalculation procedure is completed at each station the FWD load is dropped over the length of the project. Since the PCC moduli vary considerably over the length of the project, a cumulative percentage plot is used to account for the variability. Deflection values that produce AREA values larger than 36 are not used in calculations of the PCC moduli. K-values are then averaged and entered into the CDOT or PCA design procedures along with the required parameters to obtain a design thickness. A complete design example can be found in Appendix B.

### ***PCC Elastic Modulus***

In order to add a factor of safety to the design and to address the spread that can be seen in the calculated PCC modulus, a cumulative percentage plot is used (Hall and Darter 1994). Once the PCC moduli are backcalculated from the above procedure, a histogram is created using a reasonable grouping interval. The cumulative percentage is calculated from the histogram data using the following equation:

$$\frac{\# \text{ of moduli} \leq \text{current interval}}{\text{total \# of moduli values}} = \text{Cumulative Percentage} \quad (46)$$

The results are then plotted with the moduli values on the x-axis and the percentage on the y-axis. Depending on how conservative the engineer wants to make the design, a percentage is selected. Three percentages should be used depending on the level of design sought: 60% should be used for a lean design, 75% should be used for a middle of the road design, and 85% should be used for a conservative design.

### **Effective Thickness of Existing Pavement**

#### ***Effective "Plate" Theory***

The effective plate theory was developed by Ioannides et al. as a way to evaluate the contribution to the modulus when a concrete base is placed on top of a stabilized base (Ioannides et al. 1992). In order for this theory to work (the assumption that ACC = PCC), a decision must be made on whether the ACC is completely bonded to the PCC layer, completely unbonded, or partially bonded.

### ***Unbonded ACC and PCC Layer***

If the ACC and PCC layers are not bonded, the equation to calculate thickness of the effective “plate” is rather simple.

$$h_e = \left[ D_{AC}^3 + \frac{E_{PCC}}{E_{AC}} * D_{PCC}^3 \right]^{(1/3)} \quad (47)$$

where

$h_e$  = effective thickness of the existing pavement, in  
 $D_{AC}$  = thickness of the AC layer, in  
 $D_{PCC}$  = thickness of the PCC layer, in  
 $E_{AC}$  = elastic modulus of the AC, psi  
 $E_{PCC}$  = elastic modulus of the PCC, psi

### ***Bonded ACC and PCC Layers***

If the ACC and PCC layers are bonded, then the neutral axis of the composite plate is calculated. The first step is to calculate the depth to the neutral axis ( $x$ ).

$$x = \frac{E_{AC} D_{AC} \frac{D_{AC}}{2} + E_{PCC} D_{PCC} \left( D_{ACC} + \frac{D_{PCC}}{2} \right)}{E_{AC} D_{AC} + E_{PCC} D_{PCC}} \quad (48)$$

where

$D_{AC}$  = thickness of the AC layer, in  
 $D_{PCC}$  = thickness of the PCC layer, in  
 $E_{AC}$  = elastic modulus of the AC, psi  
 $E_{PCC}$  = elastic modulus of the PCC, psi

Next, calculate the thickness of the effective plate ( $h_e$ ).

$$h_e = \left\{ D_{AC}^3 + \frac{E_{PCC}}{E_{AC}} D_{PCC}^3 + 12 \left[ \left( x - \frac{D_{AC}}{2} \right)^2 D_{AC} + \frac{E_{PCC}}{E_{AC}} \left( D_{AC} - x + \frac{D_{PCC}}{2} \right)^2 D_{PCC} \right] \right\}^{(1/3)} \quad (49)$$

where

$D_{AC}$  = thickness of the AC layer, in  
 $D_{PCC}$  = thickness of the PCC layer, in  
 $E_{AC}$  = elastic modulus of the AC, psi  
 $E_{PCC}$  = elastic modulus of the PCC, psi

## Design Implementation

### Iowa 175

A fifteen-mile section of Iowa Highway 175 in Ida and Sac counties (western Iowa) has been identified by the District 3 staff as a candidate for rehabilitation in 2006. The site is shown in Figures 34 and 35.

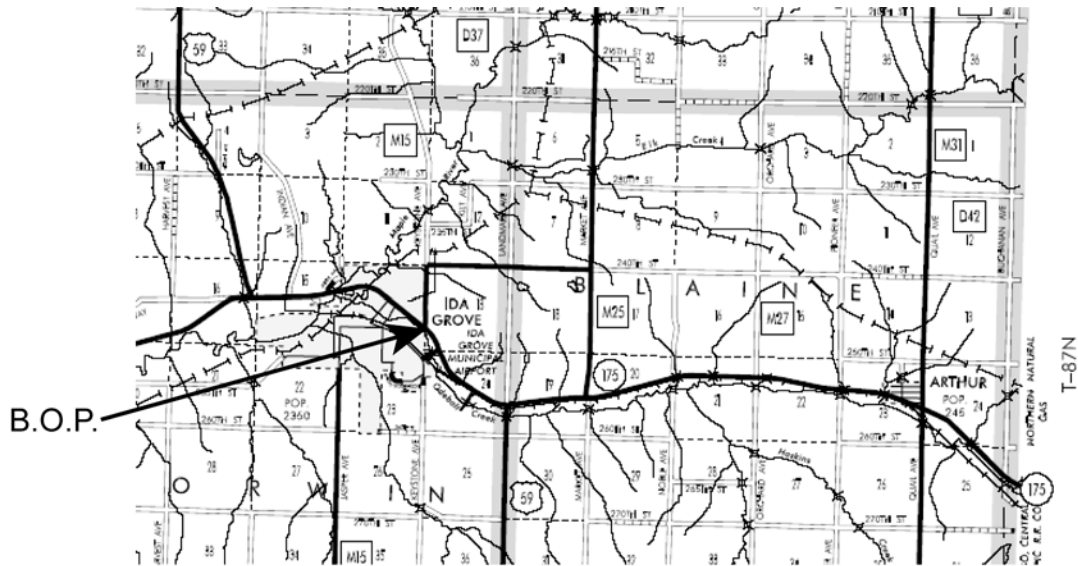


Figure 34. Ida county site map

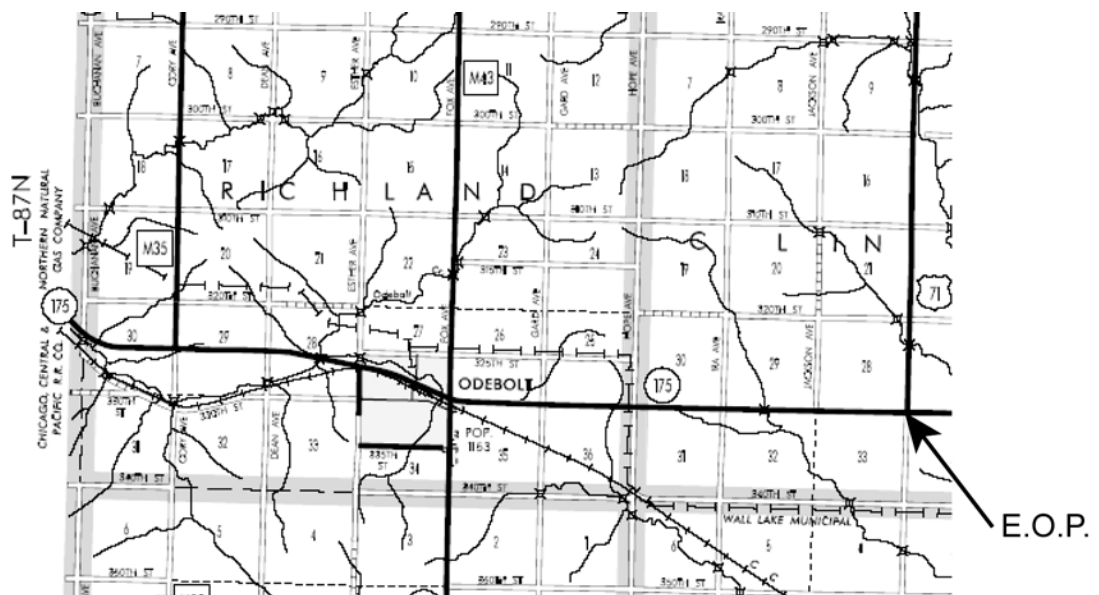


Figure 35. Sac county site map



The route consists of an existing thickened edge concrete pavement that has been widened and overlaid with Asphaltic Concrete. The original rehabilitation concepts involved various mill and fill Asphaltic Concrete options. The research team has been able to conduct field FWD deflection measurements every 0.2 mile in each direction on the project. The results of this and visual surveys of the project have been used as inputs to the previously described design procedure. The design procedure has indicated the need for a 4.5-inch PCC overlay if no bonding is assumed between the overlay and the existing ACC layer. If bond is assumed, the overlay thickness could be reduced to 3.5 inches. In each case, the pavement will be widened from 24 to 28 feet with an 8-inch deep non-tied PCC widening unit.

This work and one other project being considered in northeastern Iowa will represent the first use of this new design methodology in Iowa. These projects will represent the implementation phase of the design methodology and provide validation and upgrading of the procedure in the future for Iowa State and local road needs.

### **Overlay Planning Guidelines**

It is important that the rehabilitation program planners and rehabilitation designers understand the locations where this specific overlay design method can be best applied. The pavement engineers should pay special attention to the following characteristics of the existing roadway cross section and condition:

1. Review of “as built” plans. The performance of this type of overlay depends heavily on the materials and condition of the underlying layers at the time of the overlay. This review will help the pavement engineer understand the visual survey performance indicators in a field review.
  - a. The materials used in the concrete layer at the bottom of the existing pavement should be durable. Gain an understanding of the existence of reinforcement and its layout. Is it continuous mesh, load transfer, or a bar configuration in portions of the slab?
  - b. Identify the transverse joint spacing and the depth of the PCC slabs. Is this a uniform depth section or thickened edge pavement, and what were the cross slopes on the surface of that layer?
  - c. How many ACC overlays have been placed on this slab, what was the overlay depth and date of placement, what was the material makeup, and what surface preparations were done prior to each overlay? Are the overlay materials subject to stripping or deformation? (You must conduct coring to determine the presence or absence of stripping.) Has the pavement been widened, and if so, with what type of materials and to what depth?
  - d. What type, amount, and location of drainage layers or systems are present along the roadway? A review of existing drainage ways adjacent to the project can identify farm tile and drainage obstructions.

2. Traffic Estimate. Determine the historical mix of the traffic and the number of axle loadings it has experienced from original construction to the present time. What will be the mix and volumes of various vehicle types (especially trucks or farm equipment) expected in the design period?
3. Field review of the project. This activity should involve the combined efforts of the pavement engineer, soils engineer, planner, designer, and the local maintenance supervisor at a minimum and any pavement history/management records review for the project area. This is an important step in collecting knowledge of the pavement that does not appear in written records.
  - a. Identify each pavement distress, frequency, and severity over the length of the project. Is the distress found throughout the project or in isolated portions? Take note of field entrances of heavy farm equipment or crossroads locations such as a quarry location near the roadway.
  - b. Try to determine whether the distress is load, environmental, or material related. Examples may include excessive numbers of transverse cracks that are “tented” upwards. If these cracks are associated with joints in the underlying PCC pavement, it may mean that the concrete is deteriorated to a point where the new overlay will not bridge this problem. It may also mean there is no load transfer or the reinforcement is deteriorated to a point of no practical use. If there are many transverse cracks between PCC joints, one should consider the existence of transverse steel in the concrete layer acting as another deteriorated joint. This usually results in “tenting” of the crack. If more than 20% of these are “tented” up, it is doubtful that any kind of thin overlay will perform adequately.
  - c. Look for longitudinal working cracks at a joint between the original pavement and the widening unit. A working crack here must be considered in the jointing plan for the overlay.
  - d. Determine the location of other working cracks (longitudinal, transverse, or diagonal) that will require reinforcement in the overlay.
  - e. Identify the location of existing full depth patches and their condition. If they have failed, this is the time to replace them. If more than 20% of the transverse joints in the project have been patched in this manner and more are needed, thin concrete overlay rehabilitation should not be considered. An unbonded overlay of significant thickness (6” or greater) should be considered along with the option of removal and replacement of the entire roadway structure.
  - f. Identify areas of potential delamination in the ACC or ACC/PCC underlying pavement layers due to moisture or pavement longitudinal growth and blowups. If blowups have occurred in the past, what material was used to patch them and were moisture conditions dealt with at the site? How much additional drainage work will be required and how will it be placed relative to the existing pavement cross section?

- g. Identify special needs for additional widening to accommodate trucks entering and leaving the pavement and navigating horizontal curves.
- h. Identify special needs of the surrounding property owners that must be met during construction. Is daily access essential or can special arrangements for access be provided during construction?
- i. Identify the drainage structures that must be lengthened or widened. Will bridge decks be overlaid or will the overlay be transitioned into the existing decks? Are the drainage structures in need of replacement? If so, they should be replaced and patched with a full depth before the overlay is placed.
- j. Identify the need and location for any shoulder widening. The new pavement should have at least 3 foot of earth or granular shoulder outside the paved area to protect the pavement section.
- k. A review of detour potential routes should be considered at this time. It is not necessary, but could speed up construction and opening to traffic.
- l. Field review data collection should include the following: random coring of layers at selected distressed and good performing transverse joints, wheel paths and mid panel/quarter points to determine the stability of each layer, and potential delamination areas between various layers.
- m. FWD deflection testing should be performed at each 0.2-mile location in the outer wheel path in each direction of travel on the project roadway. This amount may be reduced over time by the design agency when they develop a level of confidence in the variability along the roadway with their results. Testing should be done with a load and with sensors placed between surface cracks and not across a reflective crack.

## **Overlay Design Guidelines**

The following items should be considered in the development of the PCC overlays.

1. Depth and condition of the various layers of the existing pavement. If the underlying PCC layer contains large amounts of steel reinforcement that is causing reflective cracking in the surface of the pavement, this pavement should not be considered for a thin PCC overlay. Treat this pavement as an in-place base and design a conventional unbonded PCC overlay of 6 inches or greater on the pavement.

If the cores taken in the field indicate debonding or delamination between the ACC layers or the ACC/PCC, interface consideration should be given to removal of the ACC to that interface. In the case the interface between the ACC/PCC is the problem, complete removal of the ACC and replacement with a one-inch ACC bond breaker should be considered to insure good performance of the new PCC overlay and to reduce the potential for reflective cracking.

2. Overlay depth should be determined from the results of the coring, deflection testing, and anticipated traffic mix and volume. It should consider the amount of ACC depth

being removed in the milling procedure and make allowance for the reduced composite section depth.

3. The entire ACC surface should be milled to a minimal depth that allows for the road surface crown to be restored while removing any high spots across the road surface. It is not necessary or advised to remove the ACC to the bottom of the ruts that may be present in the ACC surface. Millings can be used for shoulder materials in most cases.

Termini at bridges or ends of the project should be milled to a depth of 6 inches or greater at the junction with the existing pavement. Mill across the slab at this point to get a vertical edge at the junction of the new and old surfaces. If this means removal of some of the existing PCC, treat that section as a bonded section in terms of joint patterns. This provides a thickened end where vehicle impact loads are prevalent.

In the event the existing widening unit longitudinal joint is open and working, it is suggested that the widening unit be milled to a depth of the design widening unit and a new joint established at this point. Expansion joint material shall be replaced near bridge termini according to highway agency standards.

4. Joint patterns in the surface PCC overlay should be determined in relationship to the slab width of the underlying PCC pavement. Divide the lane width into segments that are nearly square in nature and allow for the retention of a lane or centerline joint. Either joint can become a reflective crack if not considered in the design. Joint spacing of the PCC overlay in feet should not exceed twice the depth in inches, unless fibers are used. In this case, do not exceed the instructions of the fiber manufacturer. The fibers will hold cracks tight and to some degree assist in bonding, but they will not stop the crack from forming. The object of joint design is to allow for the differences in cement chemistry of today and allow for curl and warp to occur in the thin surface without causing cracks. Care should be taken to eliminate longitudinal joints in the wheel paths wherever possible.

Evaluate the condition of the existing widening joint. If geotextile or metal reinforcement was used across the original joints in the overlay and the joint is tight, the designer can neglect this joint as a potential reflective crack in the overlay.

5. The use of fibers is suggested in PCC overlays of less than 4 inches as an insurance policy against loss of surface due to a crack. They will not stop cracking, but will retard loss of material around the crack. Research is ongoing to evaluate the use of the fibers to allow for larger joint patterns in the overlay that could match the underlying PCC layer joint pattern.
6. Tie bars across the longitudinal joints should be used in PCC depths of 6 inches or greater due to placement problems. In the case of the longitudinal joint between a new widening unit and the existing pavement, where the PCC overlay thickness is less than 3"–6", tie bars, nailed to the existing ACC surface at 36-inch spacings should be considered.

7. Concrete quantities should be bid in two bid items. The first should be for volume delivered in cubic yards. Be aware that this reduces the risk to the contractor, fills the rutted areas and the overlay volume, and will often overrun between 10%-20% due to irregularities in the slab wheelpaths. The second bid item is for concrete placement by the square yard that covers the placement and finishing, curing, and texturing of the concrete as will be used in a conventional PCC new pavement construction.
8. Construction survey for the overlay should involve cross sections on 25-foot intervals and points across the slab that involve the two edges of slab, centerline of roadway, center of wheelpath (rut), and lane centerpoints as a minimum. This minimizes the potential for unexpected overrun identified in item 7. It allows the engineer to identify high points in the cross section that will affect the minimum depth in a given cross section and the longitudinal grades vs. the volume of concrete required to meet a good profile and minimum depth of concrete requirements. This also requires the paving contractor to utilize two string lines to guide his machine for each edge of the roadway.

### **Overlay Construction Guidelines**

The construction of this type of overlay creates its own problems and solutions. With consideration of the following items, the project should move smoothly forward with little or no inconvenience for the traveling public. The goal of this work is to treat the construction process in the same manner as a conventional ACC overlay construction project. This requires that the designer and construction industry consider new paradigms in portland cement concrete pavement construction.

1. Scheduling of work items on the contract should direct the contractor to close portions of the road only when paving is ongoing. All removal items, drainage construction, and shouldering work should be done under traffic.

One of the critical considerations in this process is the location of the subdrains and their timing in the construction process. Consideration of the location relative to the edge of the existing vs. finished pavement edge is critical to the sequencing and traffic control.

2. Paving can be accomplished by either one-lane or two-lane construction techniques. The use of maturity testing for determination of strength gain and pilot car operations will allow for continuous use of the highway during one-lane construction. The rapid placement of this overlay proceeds at a pace that will allow multiple miles to be placed in one week in one direction and in the following week in the opposite direction. This process will require new ideas to protect the drop-off at the edge of the pavement for access points by public traffic during construction.

Two-lane construction can proceed at an equally fast pace if a detour is available. This method allows for a better performing longitudinal centerline joint. The maturity method of estimating concrete strength can be used with proper concrete mix

selection to reduce property owner inconvenience to less than 20 hours (car traffic) and construction traffic to approximately 30 hours (truck traffic) being off the placed slab.

This type of paving moves very quickly and the contractor must be prepared to not only take care of the surface area in terms of finishing, but also maintain a good surface profile. This will be the controlling activity in this type of construction.

3. The use of fibers and current texturing methods using burlap, Astroturf, and tining machines will bring some of the fibers to the surface behind the paving operation. These will not damage the pavement performance and can be removed by the first set of highway traffic or snowplow operations of the winter season.
4. Traffic control can be the same as that used on other overlay projects. It is essential that the contractor and the businesses along the project understand the construction process to be used. A preconstruction public meeting can alleviate many of the potential conflicts with deliveries and access along the project.
5. Concrete placement for this type of overlay requires that the pavement be clean of all foreign matter in front of the paving operation. This will insure the proper opportunity for bonding between the overlay and the existing surface. Temperature monitoring of the existing ACC surface should be employed to keep the surface temperature below 100 degrees Fahrenheit. In the event that temperature is exceeded, the surface should be sprayed with water to cool the surface. Excess water should be removed prior to the placement of the concrete.
6. In the event fibers are selected for introduction into the mix, the contractor should demonstrate that the introduction method will eliminate the potential for balling. The use of agitating haul units allows for the addition of the fibers at the plant and mixing during hauling. If dump trucks are used for hauling, means of blowing the fibers into the mixing drum or alternative but worker-safe modes should be demonstrated prior to beginning the work.
7. Curing and surface texturing for this type of work must remain close to the slipform paving operation due to the depth of the overlay and the changing weather conditions over the course of the day. It is recommended that multiple maturity locations be considered for each day's placement. Research indicates that the changes in existing pavement surface temperature over the course of the day may dictate that some areas be skipped by the saw in the morning in order to meet the rapid strength gain potential that could have occurred in the middle of the afternoon.
8. Due to the small distance between joints, the joint formation should be done with early entry saws and 1/8-inch-wide blades. Joint formation in both directions should be initiated as soon as concrete strengths are in the 100 to 120 psi flexural strength range or when raveling of the joint does not occur behind the saw. Depth of joint

formation should be accomplished to the same relative depth as that in full-depth pavement specifications.

The process of first sawing a transverse joint in the 15- to 20-foot range of spacing and then allowing other saws to follow with the intermediate joints can prevent premature cracks on hot weather days. In the case of thin overlays, it is important to keep the longitudinal sawed joint formation closer to the slipform than on full depth pavements. It is probable and possible to keep all the joint formation operations within 1,000 to 1,500 feet of the slipform paver for mixes that do not contain slag or similar retarding type materials.

Existing Iowa research indicates no difference in joint performance between joints that were air blasted after sawing and joints that were not cleaned. The only caution is the buildup of sawing dust and its effect on profile measurements. This can be eliminated with the use of a power broom. If water is used to cool the saw blades, then water flushing of the joints should be done.

9. The owners and contractors must change their perspective on opening this road to traffic. Shouldering should be done as soon as the pavement strength allows for construction traffic. This normally will be within two days after paving and can be monitored with the maturity method of estimating concrete strength.

## SUMMARY, CONCLUSIONS, AND RECOMMENDATIONS

### Analytical study

#### *Summary*

The state of Iowa is one of the states known for their extensive PCC pavements, where the potential for cost savings from whitetopping is a very attractive alternative to continued pavement rehabilitation with asphalt. To gain further experience in the use of whitetopping for pavement rehabilitation, the state of Iowa has sponsored several research projects to test and monitor a 9.6-mile stretch of Iowa Highways 13. The following points represent the summary of the field and the analytical investigations:

- Published analytical studies have demonstrated the feasibility of utilizing the finite element method to aid in the study of pavements constructed with a concrete whitetopping overlay.
- Owing to the irregular geometry of the composite pavement on Iowa Highway 13, three-dimensional finite element models were developed using the ANSYS finite element program to aid in the investigation of the behavior of the composite pavement. Solid and shell elements were used in modeling various configurations of the pavement structure on Iowa Highway 13.
- In order to study the effects of the interface bonding between the different layers, interface elements capable of modeling bonded and unbonded interactions were utilized. In addition, beam elements were used to represent tie bars where necessary. The applicability of the modeling techniques were then tested and affirmed by comparison of the results obtained from ANSYS with beam and plate theories and by comparison with the ISLAB2000 software package.
- The applicability of the 3-D model developed in ANSYS for the composite pavement on Iowa Highway 13 was tested by comparing the results from the finite element analysis to measured deflection and strain data from the field. Deflections from the field were in good agreement with the deflections obtained from analysis. On the other hand, comparisons of analytical and measured strains were inconclusive. This could be due to various factors that could not be adequately controlled experimentally or precisely accounted for in the analytical process. However, based on the results of the deflection comparisons, the finite element models developed for the Iowa Highway 13 composite pavement were deemed adequate to further investigate the structural behavior of the pavement.
- A parametric analysis was performed in order to determine the effects of the whitetopping thickness, joint spacing, joint crack depth, interface bond, widening unit configuration, and tie bar size and spacing. In addition, temperature data collected from the field was utilized to analyze the effect of the temperature gradient on the composite pavement behavior.



## Design Method

- The existing design methods for thin overlays contain much of the same theory and are tailored for the specific needs of the user.
- The Iowa method is designed to use tools available to the state highway department staff in the form of as-built plans, traffic projections, coring, deflection testing, and visual distress surveys to form the inputs to the design process. Much of the Colorado procedure has been incorporated into this process.
- The design process will be validated in one or more construction projects in 2006 and 2007 on state highways. The performance results do match well with existing projects on Iowa Highways 13 and 21 with their 3 and 10 years of experience, respectively.

## *Conclusions*

- The behavior of a composite pavement with fully bonded layers, subjected to actual truckloads and temperature differentials, can be accurately predicted with the 3-D model developed with this study.
- The interface elements in the ANSYS program are suitable for modeling the fully bonded and unbonded interface conditions between the different pavement layers.
- Thicker whitetopping overlays were found to improve pavement performance by lowering deflections and maximum stresses that were induced in the composite pavement under static loading.
- Investigations into pavement behavior as a function of the different joint spacing or different crack depths demonstrate that the condition of the layers underlying the whitetopping greatly influence the behavior of the pavement. With the assumption of undamaged, crack-free base PCC and ACC layers, joint spacing and crack depth did not have a significant effect on pavement performance.
- Composite pavements with fully bonded and unbonded layers exhibited very different behavior. For example, the deflections and maximum stresses induced in pavements with unbonded layers were significantly higher than in pavements with fully bonded layers.
- The width, rather than the depth, of the widening units has a significant effect on reducing the deflection.
- Load transfer between the widening units and the composite section of the pavement section has to be maintained to reduce the deflection induced in the pavement under vertical traffic loads.
- Even in the absence of the aggregate-interlock load transfer mechanism, tie bars with reasonable size and spacing were capable of providing the aforementioned load transfer between the widening units and composite section.
- A PCC overlay design procedure has been developed based on the existing Colorado design procedure and modified to use existing information that can readily be obtained by state highway department staff.

- The overlay design procedure provides for acceptable performance for traffic volumes of up to 2,000 ADT and in excess of 10 years, as indicated in the Iowa Highway 21 research results.
- Thin PCC overlay and widening units do provide a viable and economical alternative in the field of overlay rehabilitation strategies for narrow highway pavements.

### ***Future Recommendations***

The following are the recommendations for further study:

- The FWD deflection data should be normalized such that the effects of variable temperatures and foundation stiffnesses may be isolated.
- The quality of the strain data obtained from the field should be improved by ensuring the integrity of the gages after installation, which can easily be attained if these gages are installed during the construction of new pavements. Also, interference from passing traffic should be eliminated during data collection.
- The non-linear material properties for both asphalt and concrete should be included to account for fundamental material behavior, such as concrete cracking or asphalt viscosity or stripping, that could influence the behavior of the pavement.
- Time factors such as concrete fatigue, creep, and shrinkage need also be incorporated into a study of pavement performance to determine any possible long-term destructive effects.
- Detailed information on the condition of the layers underlying the whitetopping is needed for the precise prediction of pavement behavior. However, this approach could be unfeasible due to the unlimited variation of actual pavement condition in the field over a relatively short length. An alternative approach could be to assume the propagation of whitetopping joints through the thickness of the pavement, with appropriate load transfer efficiency values determined by trial and error, applied between the resulting pavement panels to approximate actual pavement behavior.
- Modeling of the partial bonding condition between the different pavement layers should be an essential part of future work since this factor has a significant effect on the overall behavior and performance of composite pavements.
- The variation in the stresses at the layer interfaces could be significant when the pavement is subjected to temperature differentials. This implies that treatment of the partial bonding mechanism is of particular importance to adequately account for the effects of temperature differentials on composite pavement behavior.
- The effects of using tie bars and aggregate interlock mechanism on the load transfer between the widening units and composite section need to be further investigated.
- The behavior of the composite pavement structure under moving loads, which is a better approximation of the actual traffic loads that a pavement is subjected to during normal operation, should be investigated.
- The unbonded behavior of the composite pavement subjected to temperature differential should be investigated.

- Continued validation of the developed PCC overlay design process by monitoring two pavement design projects currently under development by the Iowa DOT is necessary. Also, continue to test the FWD input method with other potential projects under rehabilitation consideration.

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## **APPENDIX A: STRAIN GAGE DATA**

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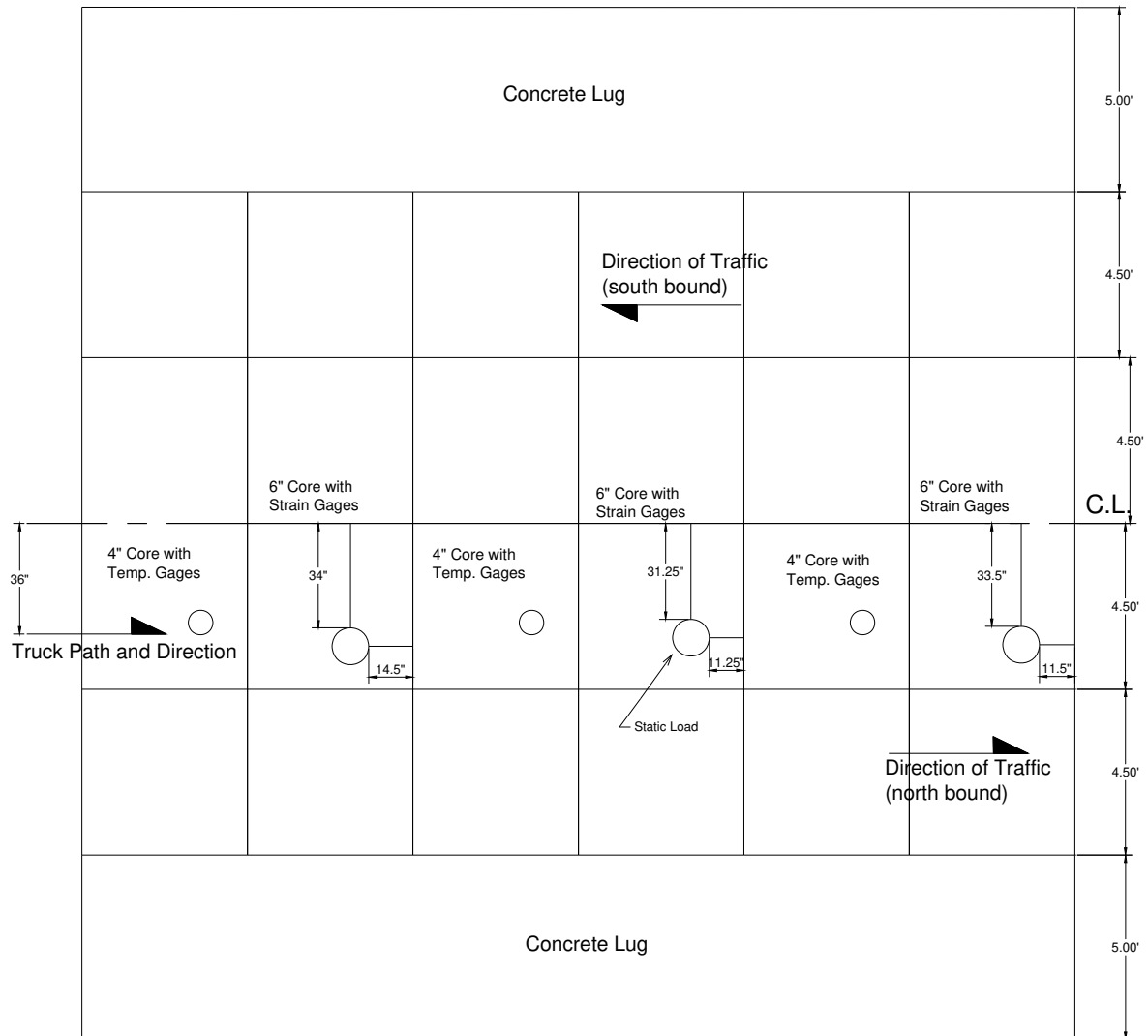
Truck speed 1- 2 mph

Site: # 1

Station: 439+10

Slab size: 4.5' x 4.5'

Gage orientation: longitudinal



Date: 9-10-2004

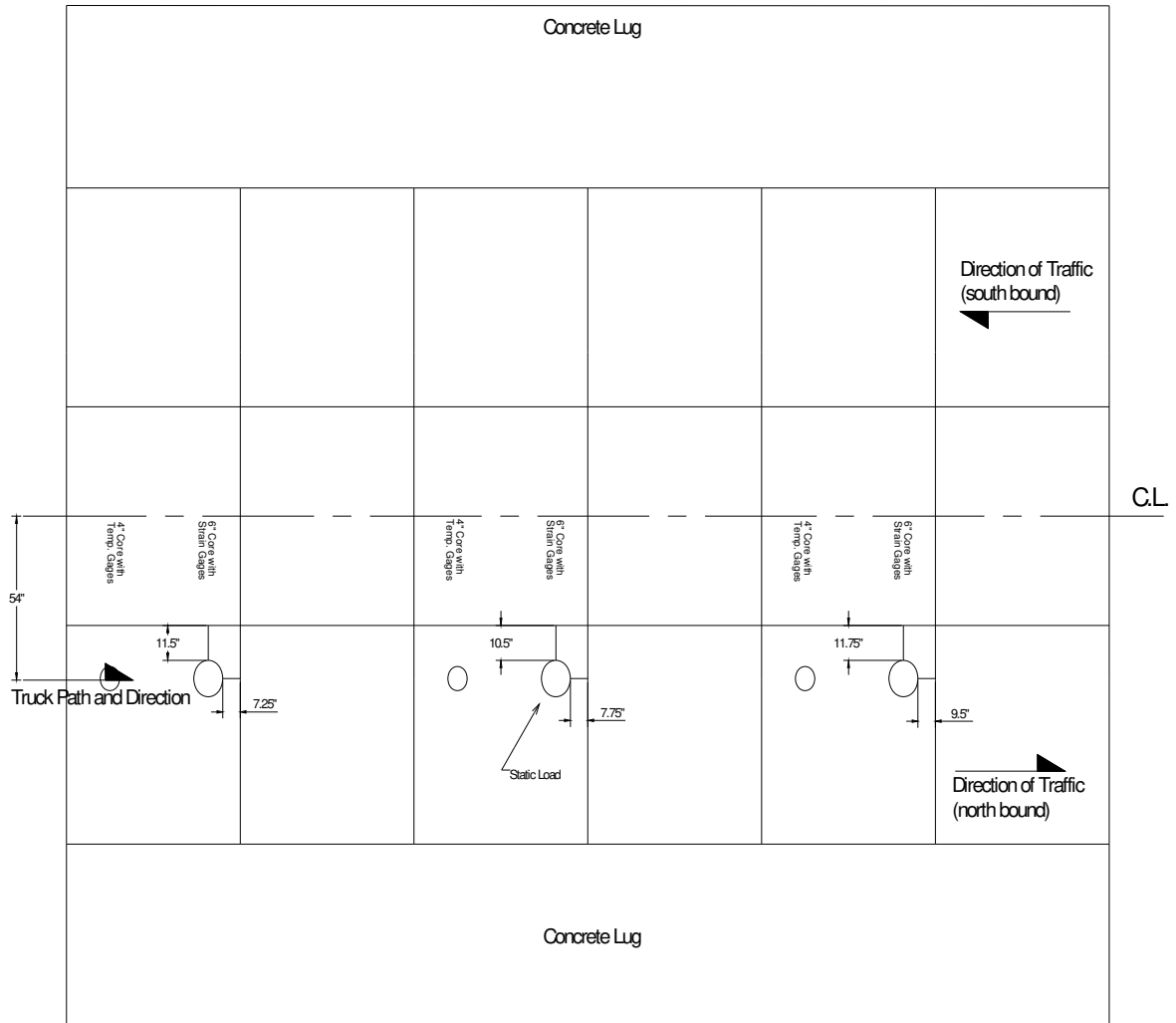
Truck speed 1- 2 mph

Site: # 2

Station:

Slab size: 6' x 6'

Gage orientation: transverse





Date: 9-10-2004

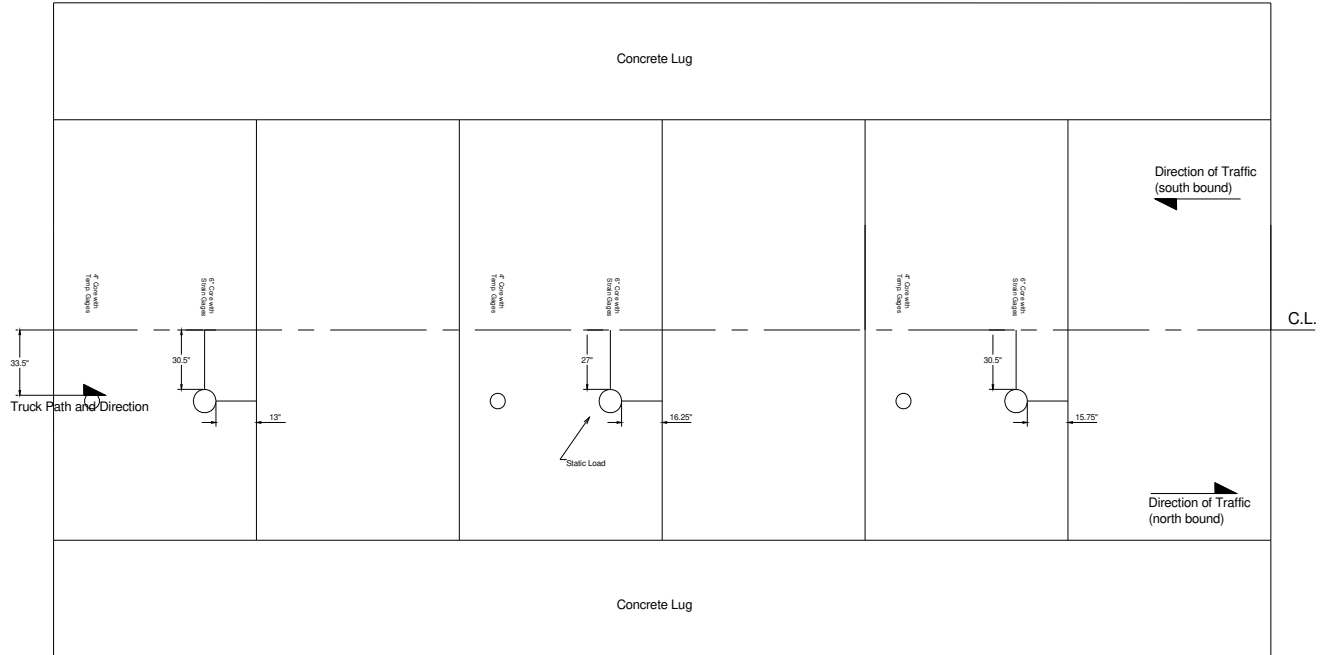
Truck speed 1- 2 mph

Site: # 3

Station: 495+00

Slab size: 9' x 9'

Gage orientation: longitudinal



Date: 9-10-2004

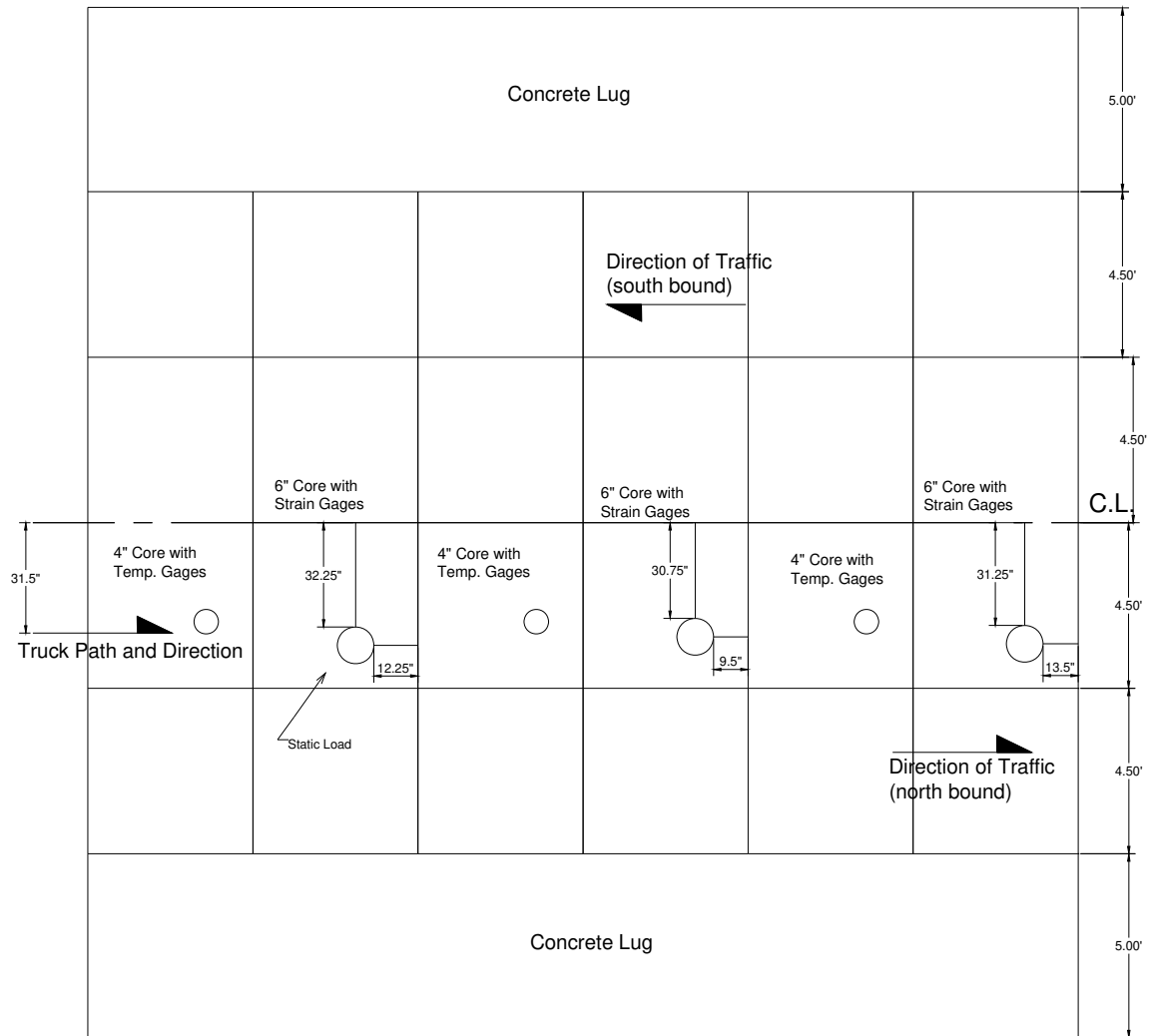
Truck speed 1- 2 mph

Site: # 4

Station: 500+10

Slab size: 4.5' x 4.5'

Gage orientation: transverse



Date: 9-10-2004

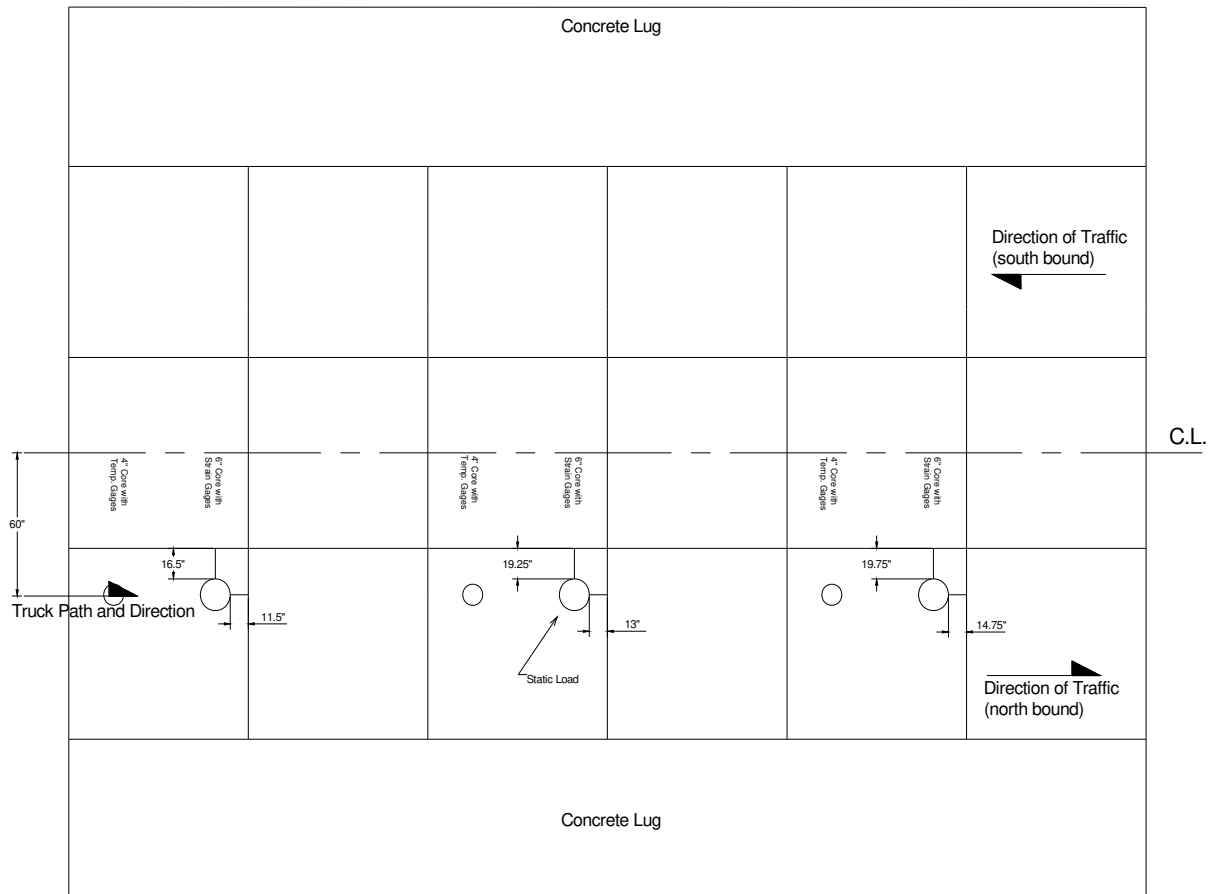
Truck speed 1- 2 mph

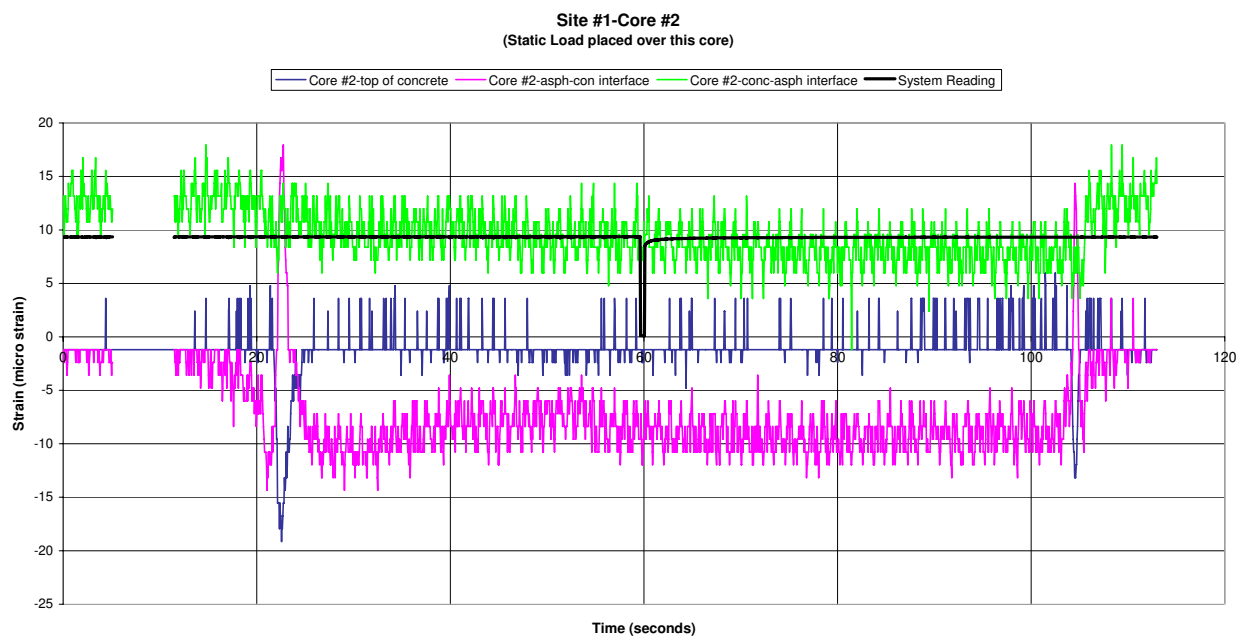
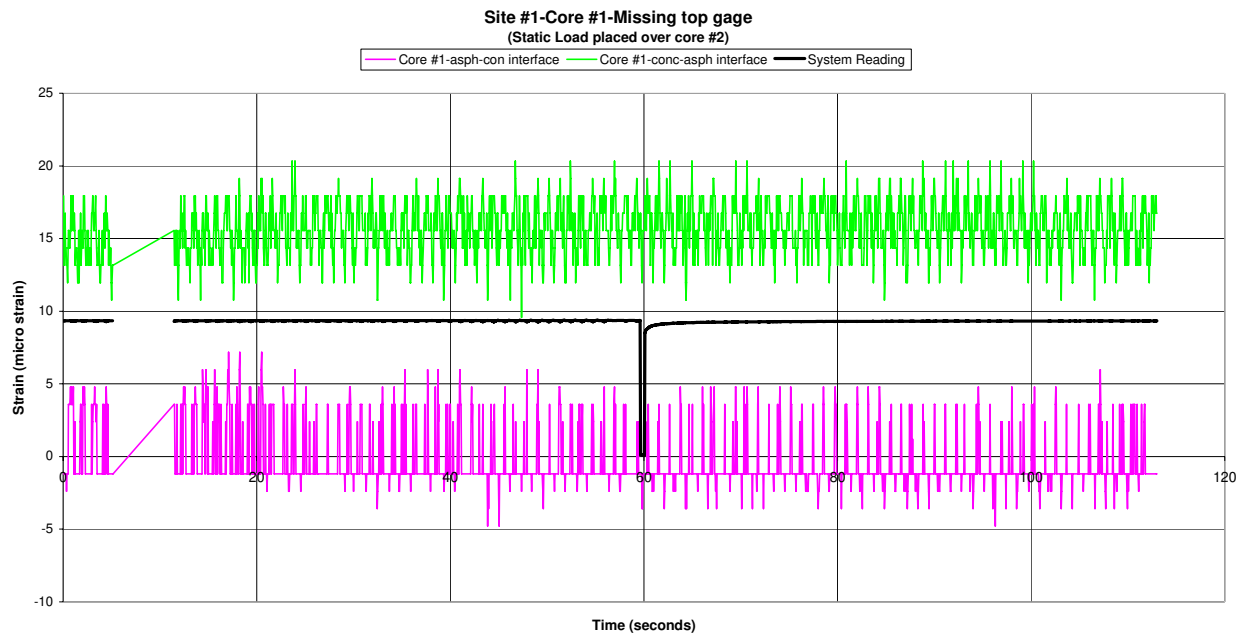
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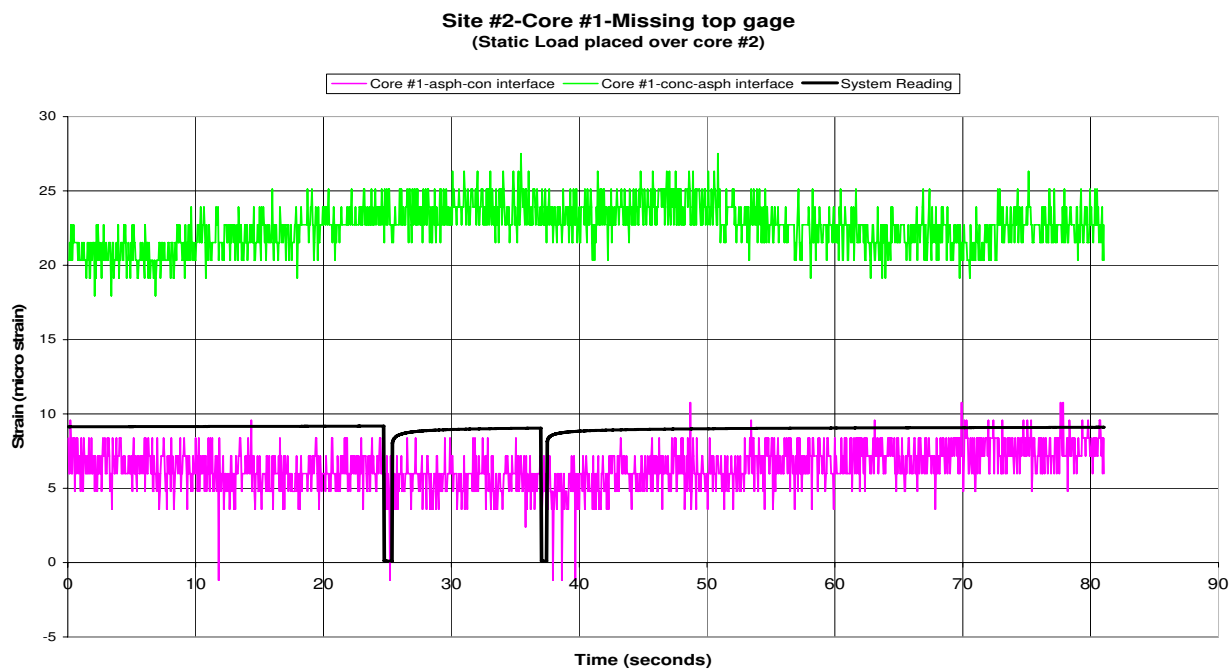
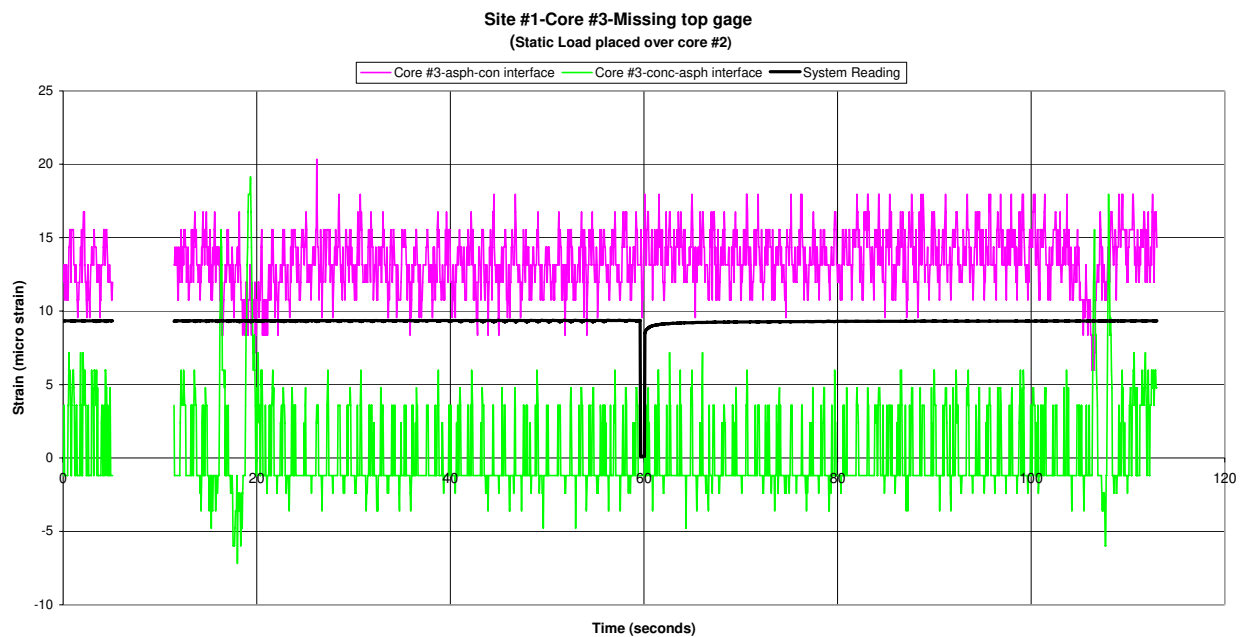
Station: 507+10

Slab size: 6' x 6'

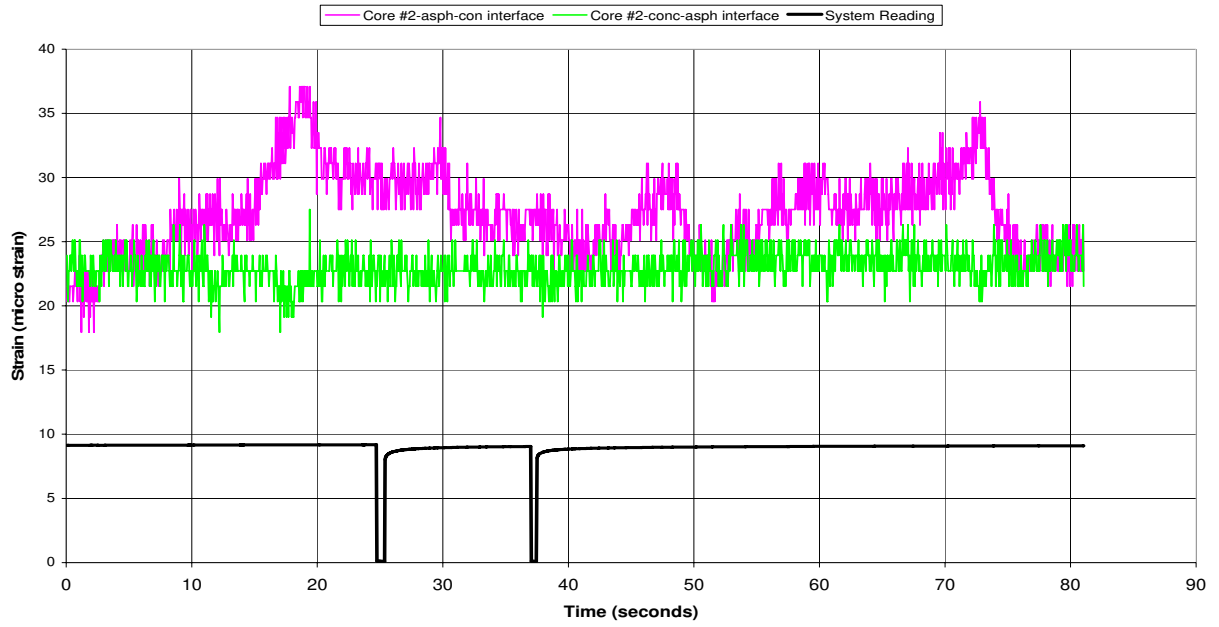
Gage orientation: longitudinal



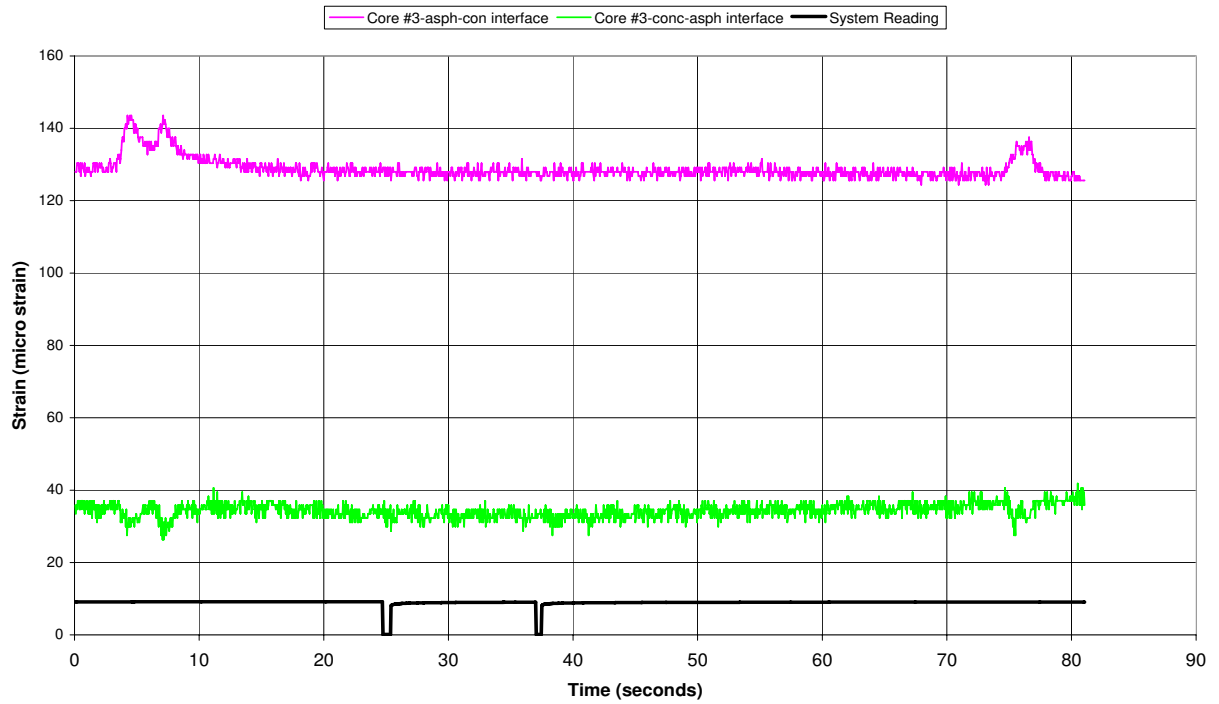




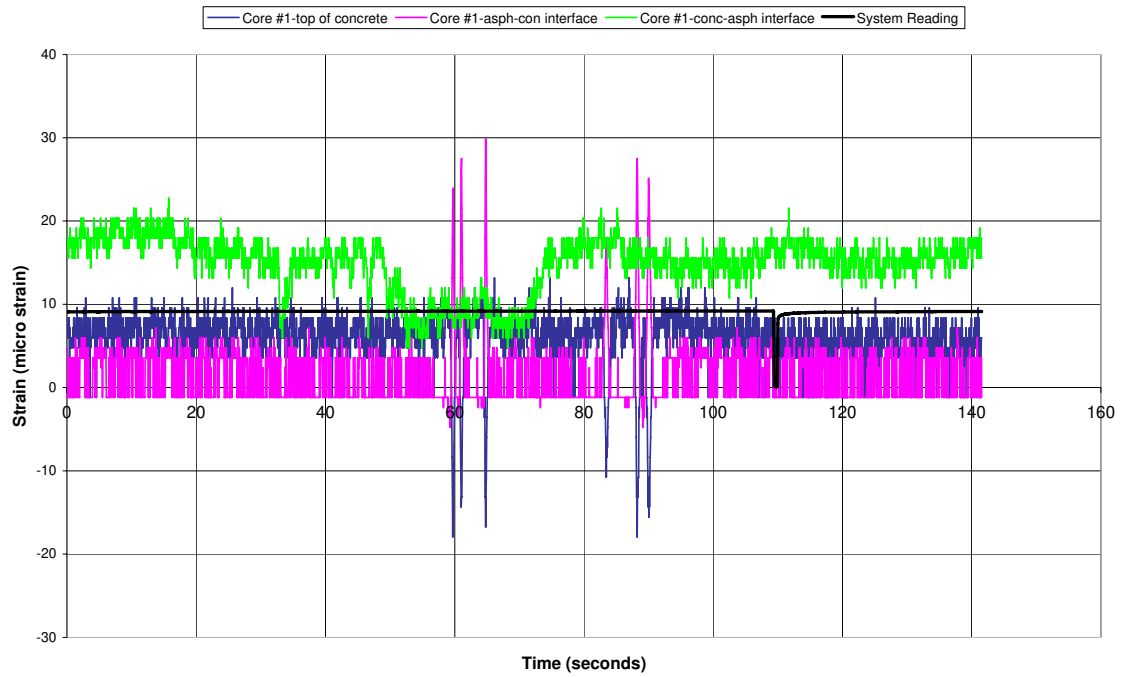
**Site #2-Core #2-Missing top gage**  
(Static Load placed over this core)



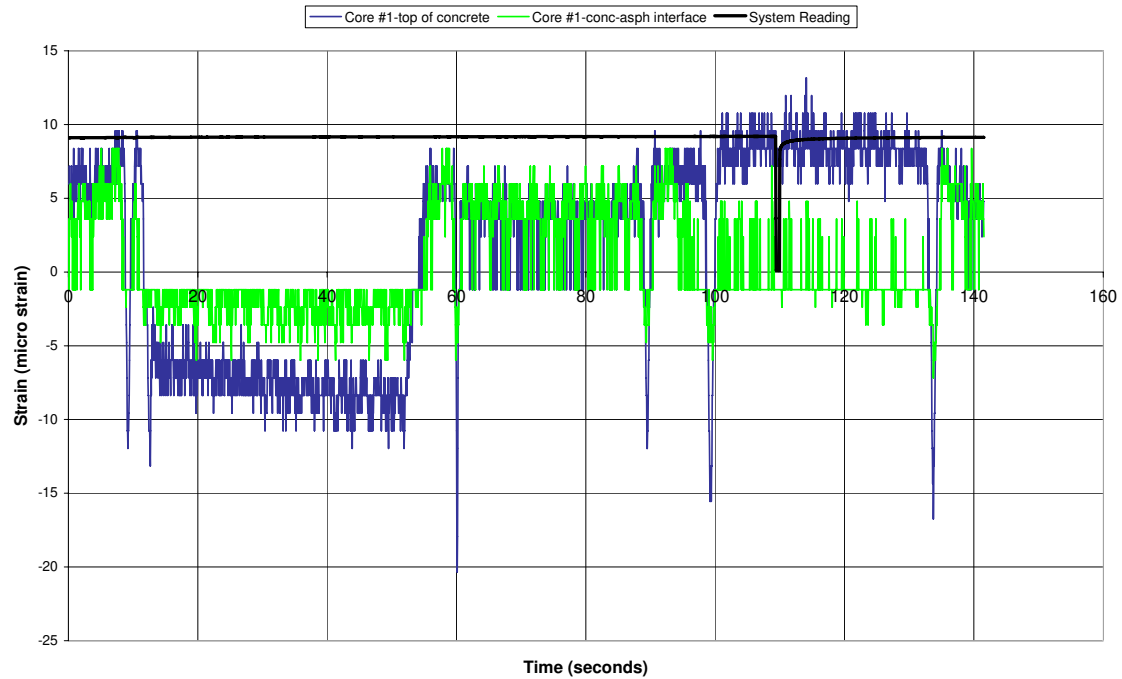
**Site #2-Core #3-Missing top gage**  
(Static Load placed over core 2)



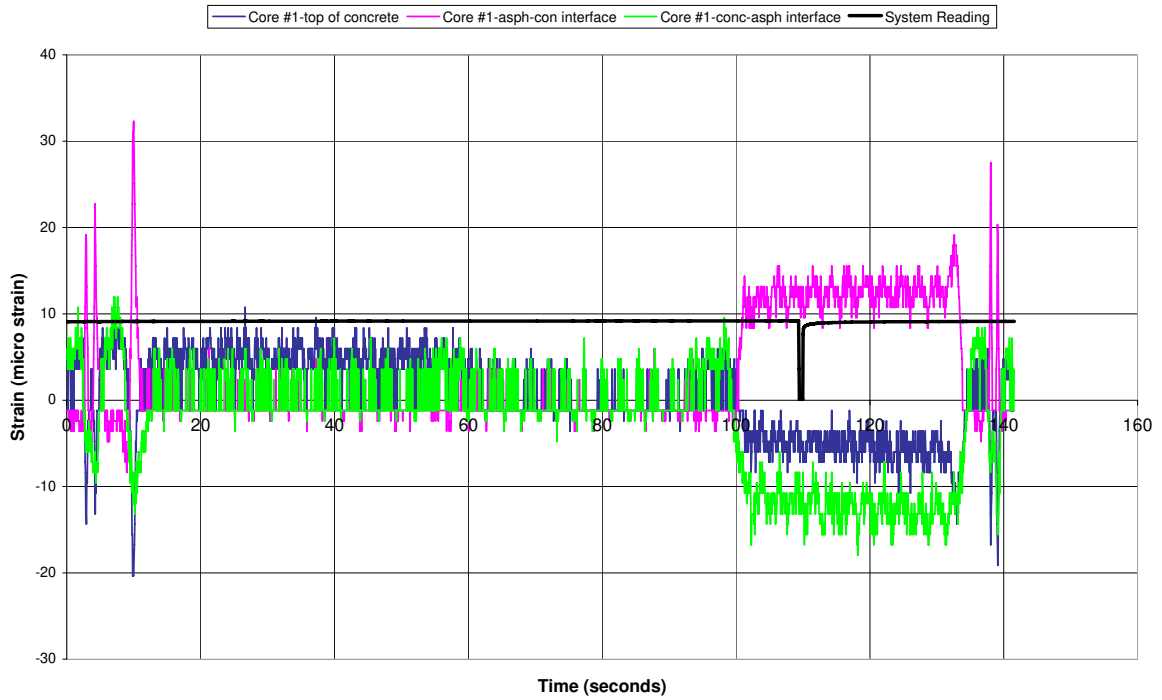
**Site #3-Core #1**  
(Static Load placed over core #2)



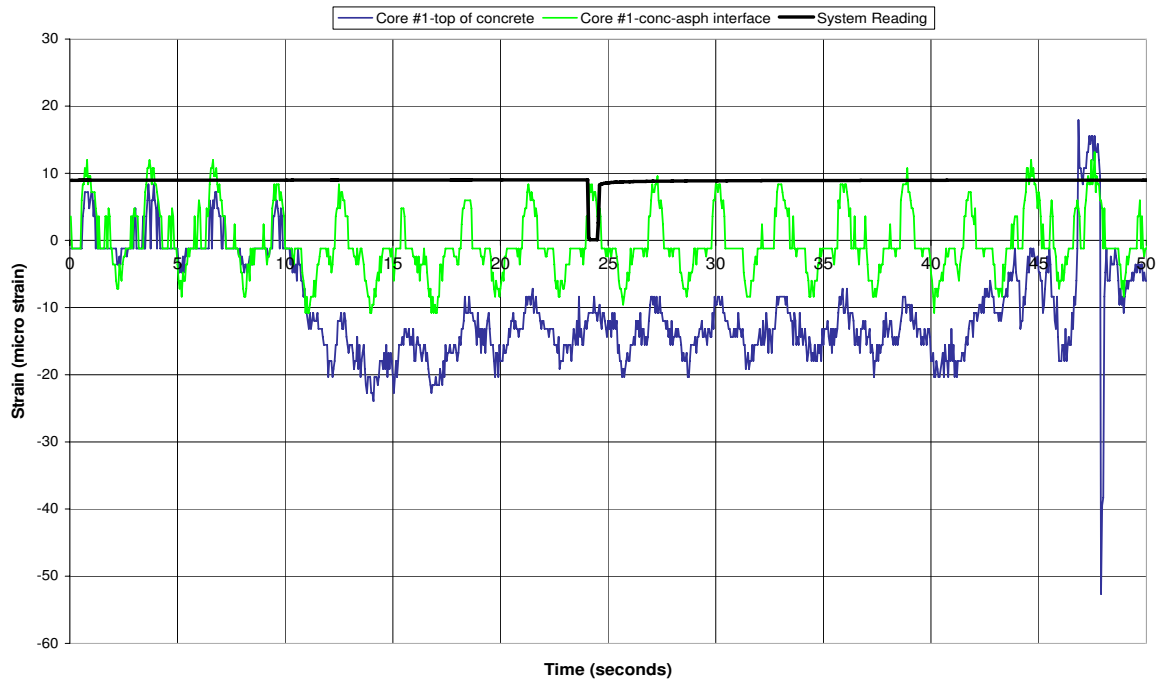
**Site #3-Core #2**  
(Static Load placed over this core)



**Site #3-Core #3**  
(Static Load placed over core #2)

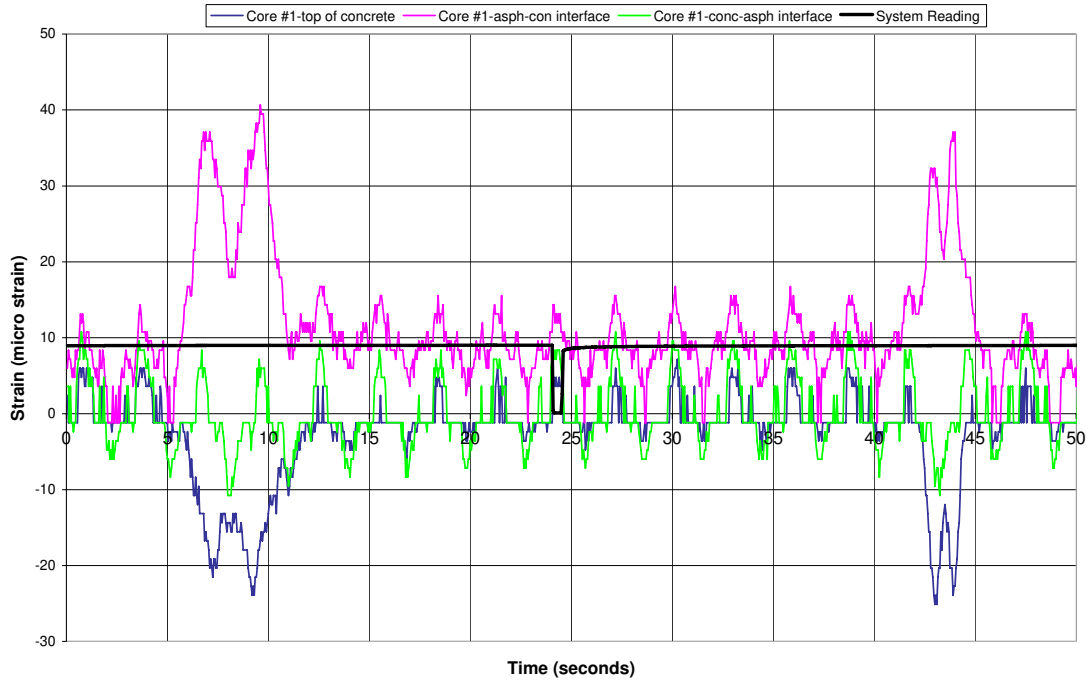


**Site #4**  
**Core #1-Transverse gage orientation**  
(Static Load placed over this core)

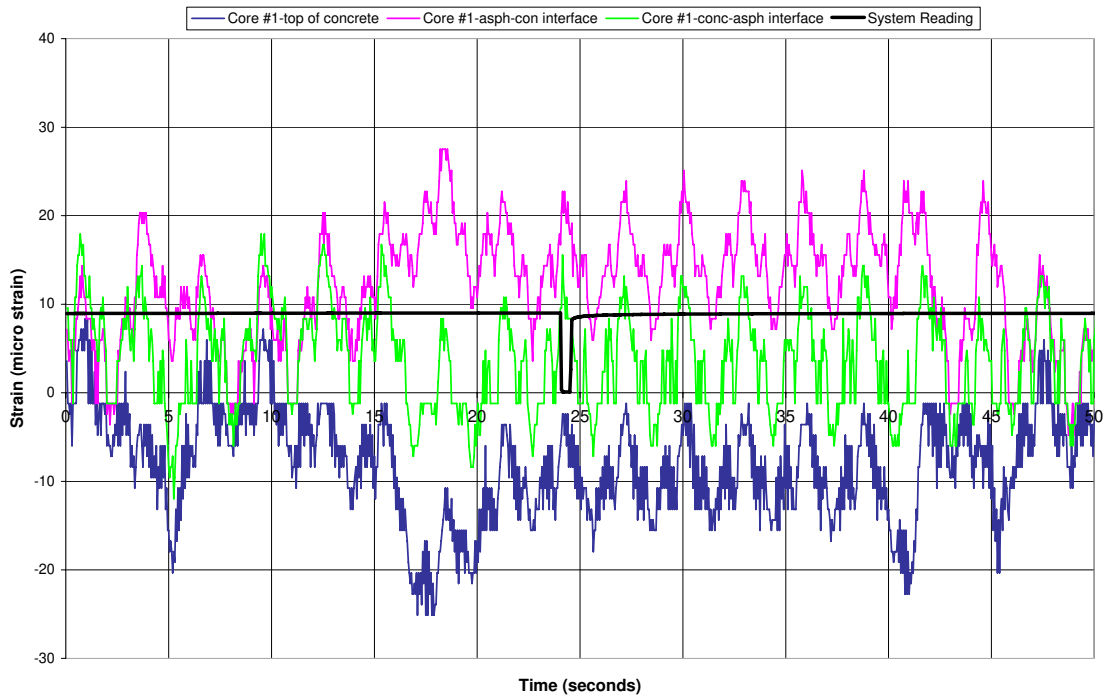




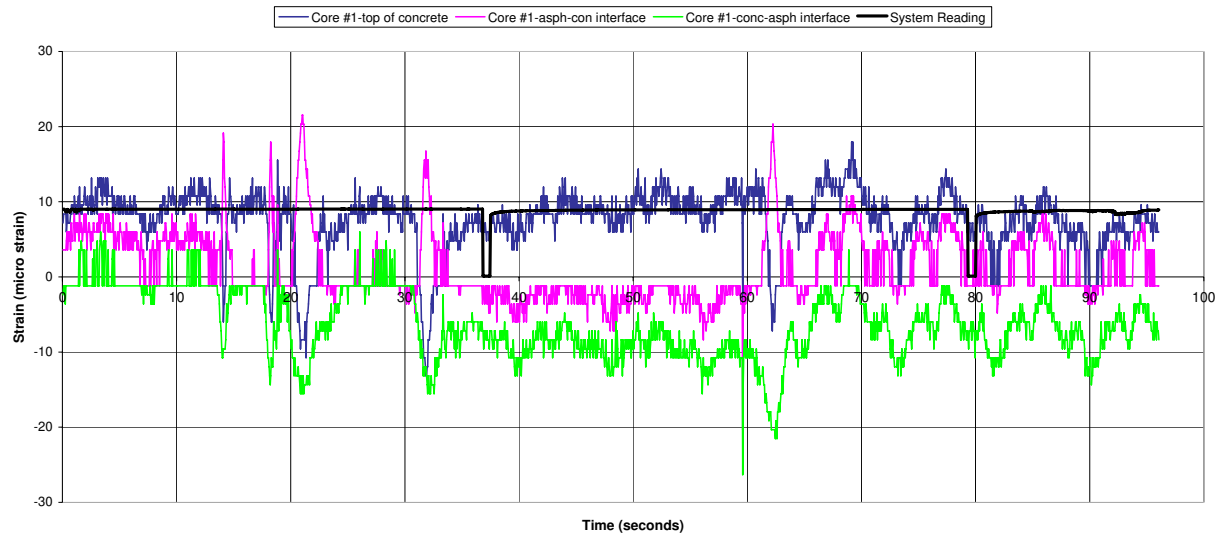
**Site #4**  
**Core #2-Longitudinal gage orientation**  
(Static Load placed over core #1)



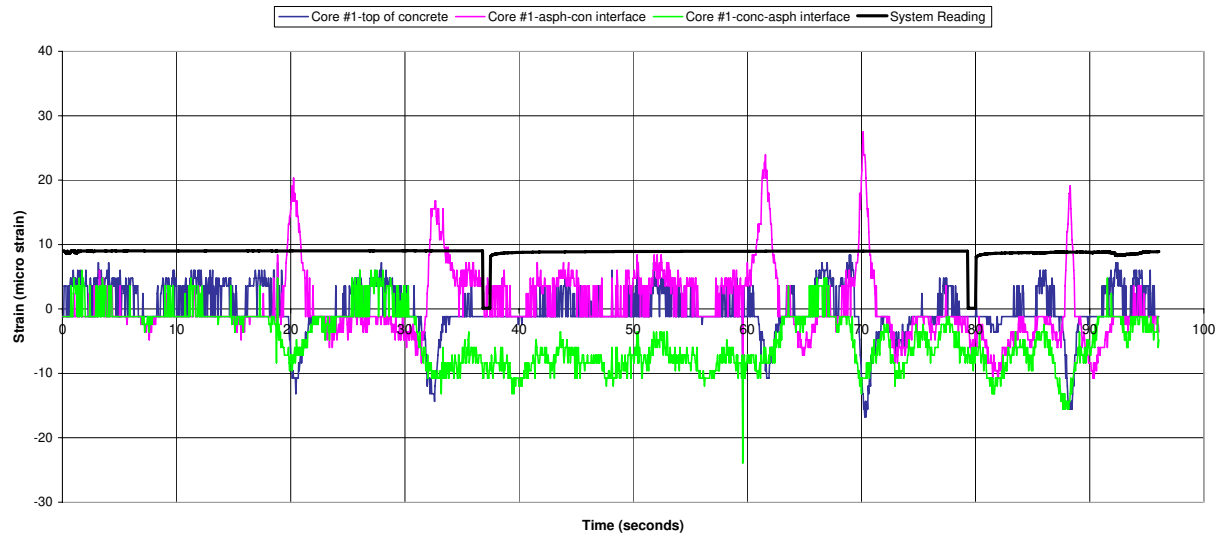
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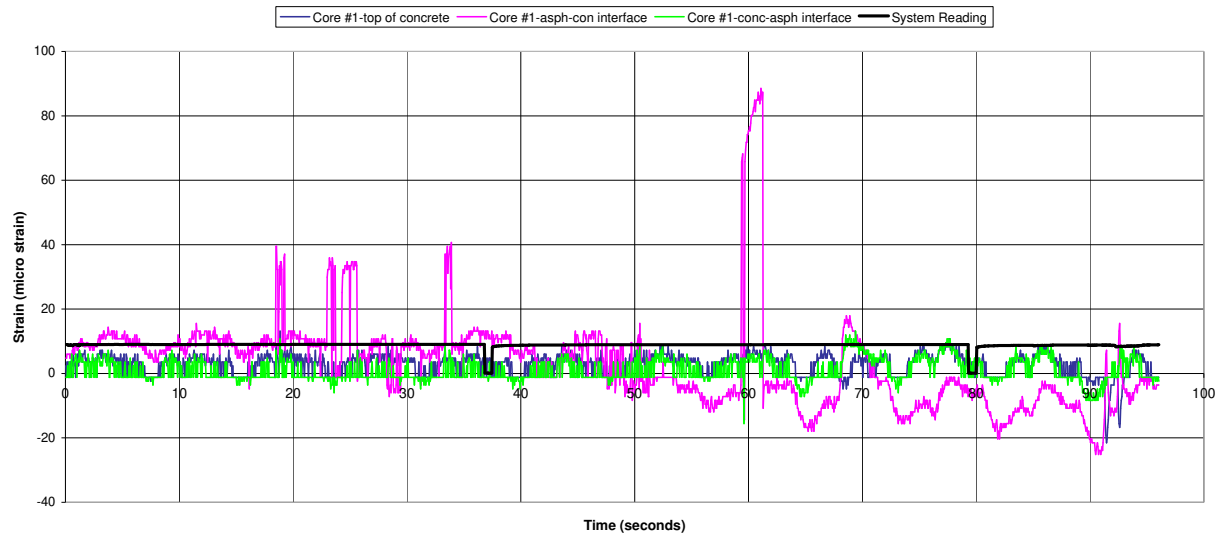
**Site #5**  
**Core #1-Longitudinal gage orientation**  
 (Static Load placed over core #2)



**Site #5**  
**Core #2-Longitudinal gage orientation**  
 (Static Load placed over this core)



Site #5  
Core #3-Longitudinal gage orientation  
(Static Load placed over core #2)



## **APPENDIX B: IOWA 175 DESIGN EXAMPLE**

**Table B.1. Iowa 175 input parameters**

**Existing Pavement Conditions**

Mean Monthly Air Temperature, °F	48.6
Temperature Differential	1.3
Asphalt Fatigue Life Previously Consumed, %	30
Joint Spacing, in	60
Thickness of the Asphalt Layer, in	4.5
Poisson's Ratio of the Asphalt	0.35
Thickness of the PCC Layer, in	8.5
Poisson's Ratio of the PCC	0.15

**Asphalt Layer's Mix Information**

Percent Aggregate Passing #200 Sieve	5.42
Asphalt Content, Percent by Weight of Mix	5.8
Percent Air Voids	2.74
Original $pen_{25}$	119

**Design Values**

Concrete Flexural Strength, psi	650
Asphalt Elastic Modulus, psi	1359876

**Eastbound Lane**

	Bonded Conditions	Unbonded Conditions
Modulus of Subgrade Reaction, pci	57	52
PCC Elastic Modulus at 75% Cumulative, psi	6000000	7850000
Effective Thickness of Existing Pavement, in	16.9	15.4
Predicted Joint Spacing, in	60	60
Trial Thickness, in	3.5	4.5

**Westbound Lane**

	Bonded Conditions	Unbonded Conditions
Modulus of Subgrade Reaction, pci	59	55
PCC Elastic Modulus at 75% Cumulative, psi	8000000	11000000
Effective Thickness of Existing Pavement, in	18	17.2
Predicted Joint Spacing, in	60	60
Trial Thickness, in	3.5	4.5

**Table B.2. Eastbound lane backcalculation of layer parameters**

**Calculated Values**

**FWD inputs**

E <sub>ACC</sub> , psi	1359876	P=	9000
d <sub>o</sub> compress (Bonded)	0.114081 mils	a=	5.9
d <sub>o</sub> compress (Unbonded)	0.2333 mils	F=	18
		t <sub>w</sub> =	0.003

Station	Lane	Joint or Mid slab	Load (kips)		Pavement Surface Deflections d <sub>i</sub> (mils)										Modified Surface Deflections, d <sub>i</sub>			
			Kips	lbs	d <sub>0</sub> (mils)	d <sub>8</sub> (mils)	d <sub>12</sub> (mils)	d <sub>18</sub> (mils)	d <sub>24</sub> (mils)	d <sub>36</sub> (mils)	d <sub>48</sub> (mils)	d <sub>60</sub> (mils)	d <sub>12</sub> (mils)	d <sub>0</sub> (mils)	d <sub>12</sub> (mils)	d <sub>24</sub> (mils)	d <sub>36</sub> (mils)	
1	2	1	8.94	8940	4.56	4.28	4.06	3.78	3.53	3.04	2.51	2.1	4.04	5.61	5.00	4.34	3.74	
2	2	1	8.92	8920	3.9	3.82	3.73	3.61	3.45	3.12	2.66	2.23	3.69	4.81	4.60	4.26	3.85	
3	2	1	8.97	8970	3.62	3.51	3.44	3.28	3.13	2.84	2.45	2.19	3.45	4.44	4.22	3.84	3.48	
4	2	1	8.91	8910	3.77	3.75	3.63	3.49	3.35	3.05	2.64	2.29	3.59	4.66	4.48	4.14	3.77	
5	2	1	9.07	9070	3.86	3.75	3.62	3.46	3.3	2.96	2.54	2.19	3.66	4.68	4.39	4.00	3.59	
6	2	1	8.89	8890	3.89	3.74	3.58	3.42	3.26	2.88	2.42	2.01	3.61	4.81	4.43	4.04	3.56	
7	2	1	8.75	8750	4.1	3.83	3.59	3.47	3.35	2.9	2.36	2.03	3.49	5.16	4.51	4.21	3.65	
8	2	1	8.79	8790	4.72	4.4	4.18	3.95	3.76	3.36	2.85	2.4	4.01	5.91	5.23	4.71	4.21	
9	2	1	9.41	9410	5.37	5.21	5.01	4.77	4.49	3.94	3.27	2.69	5.14	6.28	5.86	5.25	4.61	
10	2	1	9.15	9150	5.35	5.35	5.16	4.95	4.7	4.18	3.54	2.97	5.03	6.43	6.21	5.65	5.03	
11	2	1	9.31	9310	3.88	3.76	3.59	3.4	3.18	2.75	2.27	1.86	3.55	4.59	4.24	3.76	3.25	
12	2	1	9.09	9090	3.17	3.09	2.97	2.87	2.77	2.56	2.24	2.07	2.93	3.84	3.60	3.35	3.10	
13	2	1	9.32	9320	3.61	3.54	3.42	3.3	3.18	2.93	2.57	2.24	3.46	4.26	4.04	3.75	3.46	
14	2	1	9.46	9460	4.9	4.66	4.45	4.18	3.9	3.38	2.76	2.28	4.58	5.70	5.18	4.54	3.93	
15	2	1	9.1	9100	5.37	5.25	5.08	4.84	4.6	4.08	3.46	2.96	5.01	6.49	6.14	5.56	4.93	
16	2	1	9.16	9160	3.31	3.24	3.15	3.01	2.88	2.65	2.22	1.92	3.08	3.98	3.78	3.46	3.18	
17	2	1	9.07	9070	5.26	5.12	4.91	4.7	4.43	3.89	3.24	2.69	4.83	6.38	5.96	5.37	4.72	
18	2	1	9.1	9100	5.72	5.61	5.42	5.18	4.87	4.27	3.52	2.85	5.33	6.92	6.55	5.89	5.16	
19	2	1	9.04	9040	5.57	5.51	5.32	5.08	4.81	4.21	3.49	2.86	5.31	6.78	6.48	5.85	5.12	
20	2	1	8.9	8900	6.62	6.58	6.44	6.27	5.78	4.84	3.92	3.16	6.08	8.18	7.96	7.15	5.98	
21	2	1	9.07	9070	5.03	5	4.85	4.7	4.51	4.1	3.56	3.09	4.81	6.10	5.88	5.47	4.97	
22	2	1	8.96	8960	5.43	5.34	5.15	4.94	4.68	4.17	3.53	2.98	5.1	6.67	6.32	5.75	5.12	
23	2	1	8.94	8940	4.77	4.74	4.59	4.39	4.18	3.71	3.14	2.67	4.57	5.87	5.65	5.14	4.57	
24	2	1	8.92	8920	5.05	4.98	4.81	4.6	4.35	3.81	3.17	2.63	4.78	6.23	5.93	5.37	4.70	
25	2	1	8.84	8840	5.36	5.34	5.19	4.99	4.75	4.24	3.54	2.94	5.06	6.67	6.46	5.91	5.28	
26	2	1	8.94	8940	4.15	4.06	3.91	3.73	3.55	3.13	2.64	2.18	3.94	5.11	4.81	4.37	3.85	
27	2	1	8.95	8950	4.74	4.65	4.51	4.32	4.11	3.7	3.15	2.69	4.56	5.83	5.54	5.05	4.55	
28	2	1	8.86	8860	5.52	5.47	5.3	5.1	4.89	4.41	3.78	3.21	5.29	6.86	6.58	6.07	5.48	
29	2	1	8.81	8810	5.48	5.43	5.27	5.03	4.8	4.29	3.65	3.06	5.24	6.84	6.58	6.00	5.36	
30	2	1	8.77	8770	5.08	4.99	4.82	4.62	4.37	3.85	3.17	2.62	4.78	6.37	6.05	5.48	4.83	
31	2	1	8.86	8860	5.07	5	4.82	4.61	4.37	3.83	3.18	2.64	4.81	6.30	5.99	5.43	4.76	
32	2	1	8.84	8840	5.23	5.11	4.92	4.68	4.46	3.94	3.32	2.82	5.03	6.51	6.12	5.55	4.90	
33	2	1	8.57	8570	5.51	5.47	5.28	5.06	4.82	4.26	3.57	2.94	5.23	7.07	6.78	6.19	5.47	

Station	Lane	Joint or Mid slab	Load (kips)		Pavement Surface Deflections d <sub>i</sub> (mils)										Modified Surface Deflections, d <sub>i</sub>			
			Kips	lbs	d <sub>0</sub> (mils)	d <sub>8</sub> (mils)	d <sub>12</sub> (mils)	d <sub>18</sub> (mils)	d <sub>24</sub> (mils)	d <sub>36</sub> (mils)	d <sub>48</sub> (mils)	d <sub>60</sub> (mils)	d <sub>12</sub> (mils)	d <sub>0</sub> (mils)	d <sub>12</sub> (mils)	d <sub>24</sub> (mils)	d <sub>36</sub> (mils)	
34	2	1	8.82	8820	5.11	4.99	4.8	4.58	4.33	3.81	3.16	2.63	4.79	6.38	5.99	5.40	4.75	
35	2	1	8.79	8790	3.12	3.07	3	2.93	2.79	2.39	1.99	1.73	2.8	3.91	3.76	3.49	2.99	
36	2	1	8.59	8590	6.89	6.8	6.57	6.3	5.97	5.28	4.35	3.53	6.49	8.83	8.42	7.65	6.76	
37	2	1	8.75	8750	6.13	5.98	5.76	5.52	5.22	4.61	3.85	3.23	5.76	7.71	7.24	6.56	5.80	
38	2	1	8.9	8900	5.99	5.95	5.77	5.56	5.32	4.79	4.06	3.47	5.73	7.41	7.13	6.58	5.92	
39	2	1	8.62	8620	4.79	4.77	4.6	4.42	4.21	3.77	3.19	3.52	4.51	6.11	5.87	5.37	4.81	
40	2	1	8.67	8670	3.94	3.92	3.77	3.62	3.48	3.15	2.71	2.34	3.75	5.00	4.78	4.42	4.00	
41	2	1	8.9	8900	4.28	4.21	4.07	3.9	3.74	3.36	2.91	2.47	4.09	5.29	5.03	4.62	4.15	
42	2	1	8.76	8760	4.91	4.85	4.72	4.56	4.4	4.06	3.55	3.12	4.65	6.17	5.93	5.53	5.10	
43	2	1	8.97	8970	5.49	5.47	5.32	5.16	4.97	4.47	3.86	3.35	5.31	6.73	6.53	6.10	5.48	
44	2	1	8.77	8770	6.07	5.9	5.72	5.5	5.22	4.67	3.94	3.29	5.79	7.62	7.18	6.55	5.86	
45	2	1	8.81	8810	5.43	5.25	5.04	4.8	4.54	3.94	3.23	2.64	5.09	6.78	6.29	5.67	4.92	
46	2	1	8.87	8870	5.46	5.38	5.21	4.99	4.76	4.22	3.55	2.96	5.28	6.77	6.46	5.90	5.24	
47	2	1	8.87	8870	5.27	5.14	4.97	4.77	4.54	4.05	3.39	2.81	4.93	6.54	6.17	5.63	5.02	
48	2	1	8.9	8900	4.23	4.14	3.99	3.82	3.69	3.36	2.95	2.59	4.08	5.23	4.93	4.56	4.15	
49	2	1	8.86	8860	4.37	4.32	4.21	4.06	3.89	3.57	3.09	2.69	4.13	5.43	5.23	4.83	4.43	
50	2	1	8.8	8800	6.09	5.8	5.44	5.01	4.64	3.98	3.22	2.9	5.54	7.61	6.80	5.80	4.98	
51	2	1	8.76	8760	4.45	4.4	4.26	4.07	3.9	3.49	2.95	2.52	4.33	5.59	5.35	4.90	4.38	
52	2	1	8.91	8910	5.76	5.65	5.48	5.26	5.01	4.52	3.88	3.34	5.67	7.11	6.77	6.19	5.58	
53	2	1	8.96	8960	5.77	5.72	5.55	5.34	5.12	4.65	3.92	3.34	5.51	7.09	6.82	6.29	5.71	
54	2	1	8.69	8690	6.92	6.49	6.04	5.55	5.1	4.27	3.39	2.96	6.32	8.76	7.65	6.46	5.41	
55	2	1	8.81	8810	5.74	5.75	5.63	5.51	5.24	4.58	3.82	3.2	5.36	7.17	7.03	6.54	5.72	
56	2	1	8.84	8840	5.55	5.44	5.27	5.07	4.87	4.41	3.81	3.28	5.27	6.91	6.56	6.06	5.49	
57	2	1	8.64	8640	6.22	6.17	5.94	5.66	5.41	4.87	4.15	3.53	5.8	7.92	7.56	6.89	6.20	
58	2	1	8.86	8860	5.44	5.38	5.22	5.07	4.87	4.47	3.91	3.43	5.24	6.76	6.48	6.05	5.55	
59	2	1	8.8	8800	4.47	4.46	4.33	4.18	4.03	3.71	3.2	2.62	4.24	5.59	5.41	5.04	4.64	
60	2	1	8.66	8660	5.53	5.33	5.11	4.83	4.56	4.01	3.35	2.82	5.5	7.03	6.49	5.79	5.10	
61	2	1	8.71	8710	5.43	5.33	5.14	4.95	4.69	4.21	3.56	2.98	5.2	6.86	6.49	5.92	5.32	
62	2	1	8.85	8850	4.67	4.59	4.43	4.26	4.06	3.67	3.12	2.64	4.37	5.81	5.51	5.05	4.56	
63	2	1	8.74	8740	5.41	5.23	5.05	4.86	4.64	4.22	3.65	3.15	5.16	6.81	6.36	5.84	5.31	
64	2	1	8.81	8810	5.08	5.05	4.89	4.7	4.52	4.1	3.56	3.09	4.82	6.34	6.11	5.65	5.12	
65	2	1	8.76	8760	5	4.95	4.79	4.63	4.43	4.04	3.49	3	4.81	6.28	6.02	5.56	5.07	
66	2	1	8.84	8840	4.27	4.22	4.08	3.91	3.73	3.38	2.92	2.5	4.14	5.32	5.08	4.64	4.21	
67	2	1	8.86	8860	5.71	5.41	5.15	4.85	4.53	3.95	3.26	2.7	5.24	7.09	6.40	5.63	4.91	
68	2	1	8.91	8910	4.55	4.47	4.3	4.1	3.95	3.63	3.17	2.8	4.3	5.62	5.31	4.88	4.48	
69	2	1	8.82	8820	3.66	3.57	3.39	3.19	3	2.56	2.07	1.65	3.42	4.57	4.23	3.74	3.19	
70	2	1	8.77	8770	5.95	5.88	5.7	5.51	5.27	4.82	4.15	3.56	5.71	7.47	7.15	6.61	6.05	
71	2	1	8.82	8820	4.84	4.84	4.69	4.52	4.33	3.87	3.29	2.76	4.57	6.04	5.85	5.40	4.83	
72	2	1	8.84	8840	4.29	4.27	4.13	3.99	3.84	3.49	3.02	2.61	4.11	5.34	5.14	4.78	4.34	
74	2	1	8.82	8820	4.47	4.37	4.22	4.06	3.88	3.5	2.99	2.56	4.26	5.58	5.26	4.84	4.37	
75	2	1	8.75	8750	5.5	5.45	5.27	5.08	4.84	4.29	3.6	2.99	5.24	6.92	6.63	6.09	5.39	
76	2	1	8.81	8810	4.46	4.35	4.23	4.1	3.97	3.48	2.88	2.55	4.12	5.57	5.28	4.96	4.35	
77	2	1	9	9000	5.04	4.9	4.72	4.51	4.27	3.79	3.17	2.68	4.8	6.16	5.77	5.22	4.63	

Station	Lane	Joint or Mid slab	Load (kips)		Pavement Surface Deflections d <sub>i</sub> (mils)										Modified Surface Deflections, d <sub>i</sub>			
					d <sub>0</sub>	d <sub>8</sub>	d <sub>12</sub>	d <sub>18</sub>	d <sub>24</sub>	d <sub>36</sub>	d <sub>48</sub>	d <sub>60</sub>	d <sub>12</sub>	d <sub>0</sub>	d <sub>12</sub>	d <sub>24</sub>	d <sub>36</sub>	
			Kips	lbs	(mils)	(mils)	(mils)	(mils)	(mils)	(mils)	(mils)	(mils)	(mils)	(mils)	(mils)	(mils)	(mils)	
78	2	1	8.85	8850	6.93	6.67	6.21	5.66	5.18	4.37	3.63	3.06	6.15	8.62	7.72	6.44	5.43	
79	2	1	8.69	8690	7.79	7.5	7.16	6.78	6.41	5.62	4.71	3.95	7.21	9.86	9.07	8.12	7.12	
80	2	1	8.72	8720	5.99	5.85	5.61	5.35	5.06	4.52	3.83	3.25	5.57	7.56	7.08	6.39	5.70	
81	2	1	8.71	8710	5.76	5.73	5.55	5.32	5.06	4.54	3.82	3.21	5.6	7.28	7.01	6.39	5.74	
82	2	1	8.82	8820	5.25	5.17	5.01	4.81	4.58	4.1	3.46	2.88	4.98	6.55	6.25	5.71	5.12	
83	2	1	8.81	8810	6.15	5.93	5.71	5.48	5.23	4.68	3.96	3.36	5.76	7.68	7.13	6.53	5.85	
84	2	1	8.65	8650	6.05	6	5.78	5.54	5.3	4.73	3.96	2.99	5.68	7.70	7.35	6.74	6.02	
85	2	1	8.79	8790	5.66	5.6	5.41	5.22	4.99	4.53	3.9	3.36	5.42	7.09	6.77	6.25	5.67	
86	2	1	9.1	9100	5.18	5.04	4.87	4.69	4.46	4	3.42	2.92	4.97	6.26	5.89	5.39	4.84	
87	2	1	8.76	8760	5.56	5.5	5.3	5.1	4.86	4.37	3.75	3.25	5.34	6.98	6.66	6.10	5.49	
88	2	1	8.77	8770	3.79	3.72	3.58	3.41	3.24	2.87	2.41	1.97	3.58	4.76	4.49	4.07	3.60	
89	2	1	8.74	8740	6.19	6.05	5.83	5.6	5.37	4.91	4.18	3.6	6	7.79	7.34	6.76	6.18	
90	2	1	8.74	8740	5.63	5.63	5.4	5.12	4.82	4.2	3.5	2.97	5.12	7.09	6.80	6.07	5.29	
91	2	1	8.74	8740	6.28	6.15	5.84	5.47	5.14	4.49	3.8	3.19	5.66	7.91	7.35	6.47	5.65	
92	2	1	8.82	8820	5.67	5.59	5.4	5.11	4.83	4.27	3.57	2.98	5.37	7.07	6.74	6.03	5.33	
93	2	2	8.56	8560	5.92	6.83	6.27	5.63	5.04	4.08	3.18	2.76	6.57	7.61	8.06	6.48	5.24	
94	2	1	8.66	8660	5.05	5.01	4.83	4.56	4.28	3.74	3.11	2.56	4.76	6.42	6.14	5.44	4.75	



**Table B.2a. Bonded layer condition (eastbound lane)**

<b>d<sub>PCC</sub> (mils)</b>	<b>AREA<sub>PCC</sub>, in</b>	<b>Radius of Relative Stiffness, I</b>	<b>L/l<sub>est</sub></b>	<b>AF d<sub>o</sub></b>	<b>AF I</b>	<b>Adj d<sub>PCC</sub></b>	<b>Adj I</b>	<b>Dynamic k-Value</b>	<b>Static k- Value</b>	<b>E<sub>PCC</sub></b>
5.50	30.471	36.011	3.999	0.876	0.931	4.918	33.537	200	100	2419429
4.70	33.545	64.034	2.249	0.716	0.797	3.447	51.016	124	62	8052151
4.33	33.185	58.400	2.466	0.745	0.826	3.309	48.215	145	73	7484928
4.54	33.752	67.849	2.122	0.698	0.777	3.249	52.714	124	62	9123117
4.57	32.766	53.106	2.712	0.774	0.852	3.624	45.259	150	75	6016132
4.70	32.162	47.087	3.058	0.809	0.882	3.893	41.511	166	83	4705026
5.04	31.112	39.493	3.646	0.855	0.916	4.406	36.193	192	96	3151178
5.79	30.939	38.487	3.742	0.861	0.921	5.086	35.439	174	87	2616012
6.17	32.106	46.597	3.090	0.811	0.884	5.095	41.188	129	64	3538436
6.32	33.288	59.892	2.404	0.737	0.818	4.744	48.991	98	49	5391472
4.47	31.833	44.390	3.244	0.825	0.894	3.782	39.698	187	93	4425928
3.72	33.388	61.436	2.344	0.729	0.810	2.799	49.768	161	80	9432358
4.15	33.546	64.046	2.248	0.716	0.797	3.053	51.021	140	70	9091840
5.59	31.090	39.363	3.658	0.855	0.917	4.875	36.096	175	87	2832588
6.38	32.658	51.910	2.774	0.781	0.858	5.069	44.547	111	55	4166160
3.86	33.452	62.464	2.305	0.724	0.805	2.880	50.271	153	77	9355792
6.27	32.214	47.543	3.029	0.806	0.879	5.142	41.810	124	62	3613672
6.80	32.504	50.293	2.863	0.790	0.866	5.463	43.559	107	54	3694653
6.67	32.810	53.614	2.686	0.771	0.850	5.228	45.556	103	51	4226014
8.07	32.913	54.838	2.626	0.764	0.844	6.256	46.261	83	42	3642555
5.99	33.739	67.606	2.130	0.699	0.778	4.266	52.610	95	47	6921606
6.55	32.790	53.378	2.698	0.772	0.851	5.151	45.418	105	52	4263220
5.76	33.259	59.473	2.421	0.740	0.820	4.342	48.775	108	54	5838796
6.12	32.784	53.306	2.701	0.773	0.851	4.815	45.376	112	56	4552677
6.56	33.470	62.750	2.295	0.723	0.803	4.822	50.409	91	46	5617790
4.99	32.693	52.284	2.754	0.779	0.856	3.977	44.771	140	70	5364433
5.71	33.036	56.385	2.554	0.756	0.836	4.406	47.127	114	57	5369809
6.74	33.402	61.646	2.336	0.728	0.809	4.994	49.872	90	45	5309678
6.73	33.202	58.641	2.456	0.744	0.824	5.092	48.342	94	47	4890281
6.26	32.734	52.748	2.730	0.776	0.854	4.946	45.048	111	56	4367394
6.18	32.769	53.140	2.710	0.774	0.852	4.872	45.279	112	56	4479346
6.40	32.507	50.323	2.862	0.790	0.866	5.141	43.577	114	57	3929607
6.96	33.072	56.860	2.533	0.753	0.833	5.330	47.388	93	47	4487830
6.26	32.386	49.136	2.931	0.797	0.872	5.078	42.834	120	60	3842560
3.79	33.674	66.347	2.170	0.705	0.785	2.754	52.064	150	75	10499070
8.71	32.785	53.317	2.701	0.773	0.851	6.821	45.383	79	40	3214614
7.59	32.397	49.243	2.924	0.796	0.871	6.136	42.901	99	49	3190357
7.29	33.438	62.225	2.314	0.725	0.806	5.373	50.155	83	41	4991663
6.00	33.303	60.118	2.395	0.736	0.817	4.502	49.106	103	51	5709042
4.89	33.506	63.352	2.273	0.720	0.800	3.599	50.696	121	60	7613476
5.18	33.194	58.530	2.460	0.745	0.825	3.940	48.283	121	61	6305043

<b>d<sub>PCC</sub></b> <b>(mils)</b>	<b>AREA<sub>PCC</sub>,</b> <b>in</b>	<b>Radius of</b> <b>Relative</b> <b>Stiffness,</b> <b>I</b>	<b>L/l<sub>est</sub></b>	<b>AF d<sub>o</sub></b>	<b>AF I</b>	<b>Adj</b> <b>d<sub>PCC</sub></b>	<b>Adj I</b>	<b>Dynamic</b> <b>k-Value</b>	<b>Static</b> <b>k-Value</b>	<b>E<sub>PCC</sub></b>
6.05	33.764	68.097	2.115	0.697	0.776	4.297	52.819	93	47	6926160
6.62	33.849	69.837	2.062	0.689	0.767	4.637	53.536	84	42	6594649
7.50	32.643	51.744	2.783	0.782	0.859	5.953	44.447	95	47	3531740
6.67	31.962	45.401	3.172	0.819	0.890	5.551	40.387	123	61	3121501
6.66	33.004	55.981	2.572	0.758	0.838	5.135	46.904	99	49	4562809
6.42	32.732	52.723	2.731	0.776	0.854	5.074	45.033	108	54	4254265
5.12	33.145	57.854	2.489	0.748	0.828	3.912	47.925	124	62	6254434
5.31	33.727	67.366	2.138	0.700	0.779	3.800	52.508	107	53	7739331
7.50	30.145	34.474	4.177	0.886	0.938	6.746	32.321	157	79	1636719
5.48	33.267	59.581	2.417	0.739	0.820	4.131	48.831	113	57	6151472
7.00	32.995	55.868	2.577	0.759	0.838	5.397	46.841	94	47	4329463
6.97	33.468	62.726	2.296	0.723	0.803	5.123	50.397	86	43	5286062
8.65	29.324	31.145	4.624	0.907	0.950	7.944	29.601	159	79	1162763
7.06	33.957	72.216	1.994	0.678	0.754	4.858	54.465	78	39	6516023
6.79	33.140	57.782	2.492	0.749	0.829	5.171	47.886	94	47	4724621
7.81	32.983	55.716	2.585	0.760	0.839	6.017	46.756	85	42	3869380
6.64	33.654	65.988	2.182	0.707	0.787	4.775	51.905	87	43	6017379
5.48	33.994	73.076	1.971	0.674	0.750	3.766	54.785	99	49	8505634
6.91	31.753	43.778	3.289	0.828	0.897	5.820	39.275	124	62	2814110
6.75	32.822	53.748	2.679	0.770	0.849	5.285	45.635	101	51	4195287
5.69	33.063	56.741	2.538	0.754	0.834	4.378	47.323	114	57	5448366
6.70	32.620	51.495	2.796	0.783	0.860	5.333	44.296	106	53	3915011
6.23	33.567	64.400	2.236	0.715	0.795	4.534	51.186	94	47	6162213
6.17	33.475	62.839	2.292	0.722	0.803	4.537	50.451	97	48	5981625
5.20	33.283	59.831	2.407	0.738	0.818	3.921	48.960	119	59	6515103
6.98	30.894	38.235	3.766	0.862	0.922	6.116	35.249	146	73	2152055
5.50	33.095	57.172	2.519	0.752	0.832	4.224	47.557	117	58	5703835
4.45	31.792	44.074	3.267	0.827	0.896	3.774	39.480	189	95	4385664
7.35	33.404	61.678	2.335	0.728	0.809	5.437	49.887	82	41	4880086
5.92	33.684	66.545	2.164	0.704	0.784	4.252	52.151	97	48	6823187
5.23	33.768	68.176	2.112	0.696	0.775	3.718	52.852	108	54	8014106
5.46	32.995	55.865	2.578	0.759	0.838	4.232	46.839	120	60	5522017
6.80	33.187	58.429	2.465	0.745	0.825	5.153	48.230	93	47	4809636
5.46	33.304	60.131	2.395	0.736	0.817	4.101	49.113	113	56	6268822
6.05	32.406	49.324	2.919	0.795	0.871	4.902	42.952	123	62	4003127
8.50	29.822	33.080	4.353	0.895	0.943	7.708	31.197	147	74	1333135
9.75	31.528	42.164	3.415	0.838	0.905	8.267	38.139	92	46	1867030
7.44	32.300	48.326	2.980	0.801	0.876	6.056	42.317	103	51	3143884
7.16	33.261	59.494	2.420	0.739	0.820	5.381	48.787	87	44	4713744
6.44	33.077	56.934	2.529	0.753	0.833	4.932	47.428	101	50	4858389
7.57	32.303	48.352	2.978	0.801	0.876	6.154	42.333	101	50	3096659
7.58	33.069	56.824	2.534	0.754	0.834	5.800	47.368	86	43	4120889
6.97	33.291	59.942	2.402	0.737	0.818	5.223	49.017	89	44	4902666
6.15	32.734	52.744	2.730	0.776	0.854	4.860	45.045	113	57	4443594

<b>d<sub>PCC</sub></b> <b>(mils)</b>	<b>AREA<sub>PCC</sub>,</b> <b>in</b>	<b>Radius of</b> <b>Relative</b> <b>Stiffness,</b> <b>I</b>	<b>L/l<sub>est</sub></b>	<b>AF d<sub>o</sub></b>	<b>AF I</b>	<b>Adj</b> <b>d<sub>PCC</sub></b>	<b>Adj I</b>	<b>Dynamic</b> <b>k-Value</b>	<b>Static</b> <b>k-Value</b>	<b>E<sub>PCC</sub></b>
6.87	33.086	57.054	2.524	0.752	0.832	5.255	47.493	94	47	4572828
4.64	32.780	53.261	2.704	0.773	0.851	3.676	45.350	147	74	5955386
7.68	32.865	54.259	2.654	0.768	0.846	5.982	45.930	88	44	3754985
6.97	32.689	52.243	2.756	0.779	0.857	5.520	44.747	101	50	3860467
7.79	31.641	42.959	3.352	0.833	0.901	6.588	38.702	113	56	2413256
6.96	32.598	51.269	2.809	0.784	0.861	5.548	44.159	103	51	3740040
7.50	33.473	62.799	2.293	0.723	0.803	5.499	50.432	80	40	4931568
6.30	32.563	50.904	2.829	0.786	0.863	5.046	43.936	114	57	4070375

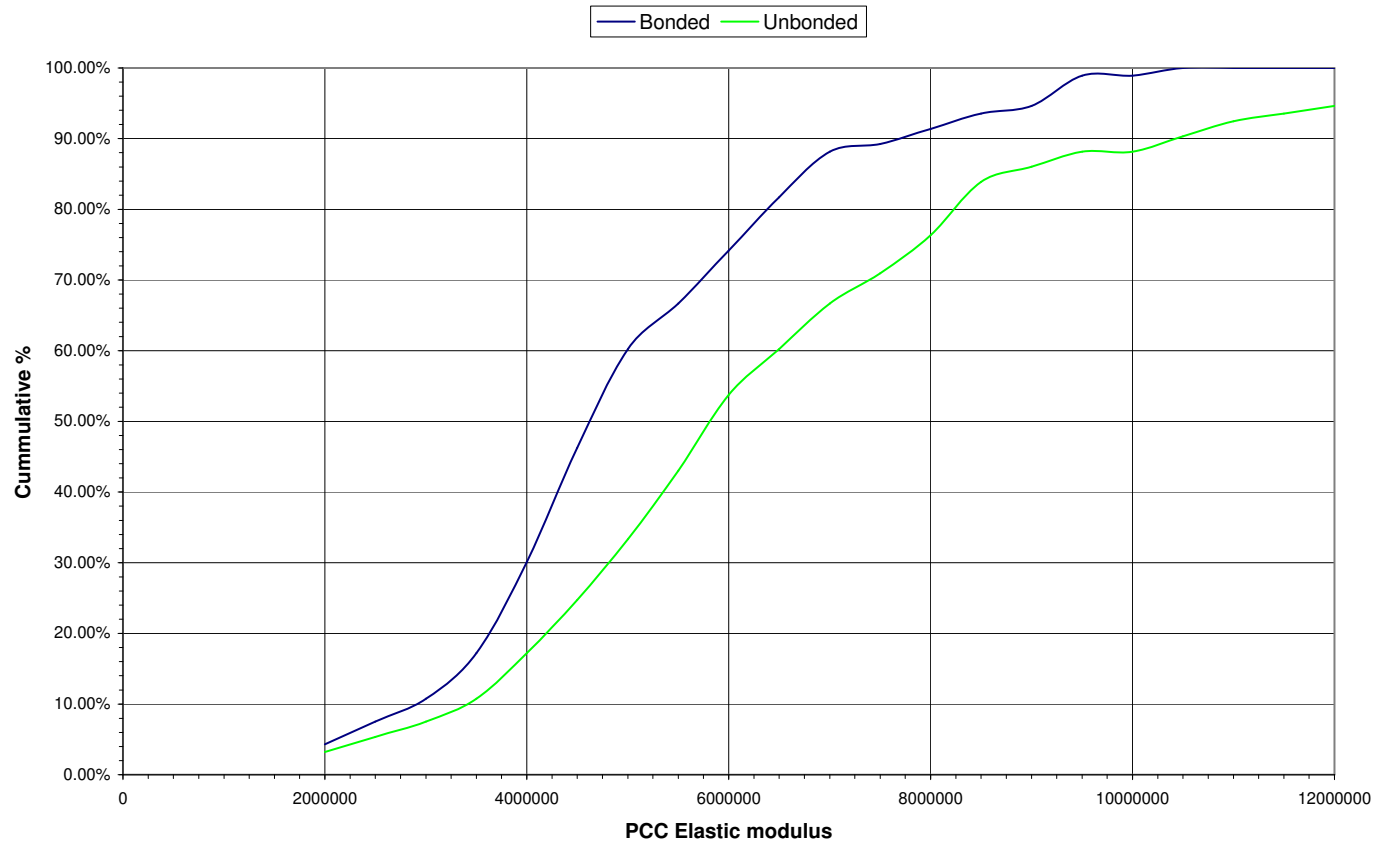
**Table B.2b. Unbonded layer conditions (eastbound lane)**

<b>d<sub>PCC</sub></b> <b>(mils)</b>	<b>AREA<sub>PCC</sub></b>	<b>Radius of</b> <b>Relative</b> <b>Stiffness,</b> <b>I</b>	<b>L/<sub>est</sub></b>	<b>AF d<sub>o</sub></b>	<b>AF I</b>	<b>Adj</b> <b>d<sub>PCC</sub></b>	<b>Adj I</b>	<b>Dynamic</b> <b>k-Value</b>	<b>Static</b> <b>k-Value</b>	<b>E<sub>PCC</sub></b>
5.38	31.013	38.914	3.701	0.858	0.919	4.817	35.760	180	90	2813376
4.58	34.263	80.097	1.798	0.644	0.713	3.097	57.115	111	55	11248235
4.21	33.955	72.167	1.995	0.678	0.754	3.010	54.446	125	63	10508922
4.42	34.500	87.778	1.641	0.613	0.673	2.856	59.089	112	56	13059783
4.45	33.483	62.975	2.287	0.722	0.802	3.380	50.516	129	65	8050875
4.58	32.843	54.000	2.667	0.769	0.848	3.703	45.780	144	72	6026551
4.92	31.720	43.535	3.308	0.830	0.898	4.278	39.106	170	85	3795032
5.68	31.463	41.725	3.451	0.841	0.907	4.968	37.824	156	78	3055295
6.05	32.620	51.503	2.796	0.783	0.860	4.917	44.301	115	58	4247685
6.20	33.812	69.075	2.085	0.692	0.771	4.453	53.226	89	44	6787767
4.35	32.541	50.674	2.842	0.788	0.864	3.612	43.794	161	80	5648996
3.60	34.294	81.027	1.777	0.640	0.708	2.455	57.386	138	69	14321613
4.03	34.361	83.089	1.733	0.632	0.697	2.692	57.954	124	62	13325605
5.47	31.637	42.934	3.354	0.833	0.901	4.750	38.684	156	78	3344036
6.26	33.166	58.141	2.477	0.747	0.827	4.848	48.078	100	50	5080116
3.74	34.327	82.008	1.756	0.636	0.703	2.528	57.662	133	67	14042762
6.15	32.722	52.612	2.737	0.777	0.855	4.957	44.967	111	56	4342197
6.68	32.976	55.627	2.589	0.760	0.840	5.257	46.706	97	49	4419280
6.55	33.298	60.054	2.398	0.737	0.817	4.994	49.074	93	46	5139586
7.95	33.316	60.325	2.387	0.735	0.816	6.017	49.211	77	38	4289664
5.87	34.303	81.277	1.772	0.639	0.707	3.898	57.457	87	43	9042863
6.44	33.286	59.870	2.405	0.738	0.818	4.918	48.980	95	47	5198580
5.64	33.836	69.561	2.070	0.690	0.768	4.050	53.425	97	48	7519089
6.00	33.316	60.320	2.387	0.735	0.816	4.580	49.209	101	50	5635127
6.44	33.978	72.707	1.981	0.675	0.752	4.507	54.649	83	42	7072427
4.87	33.345	60.767	2.370	0.733	0.814	3.744	49.434	122	61	6958010
5.59	33.612	65.206	2.208	0.711	0.791	4.141	51.554	101	51	6844708
6.62	33.895	70.829	2.033	0.684	0.761	4.689	53.931	82	41	6618811
6.61	33.692	66.695	2.159	0.703	0.783	4.814	52.217	85	43	6040969
6.14	33.253	59.389	2.425	0.740	0.821	4.717	48.732	100	50	5365404
6.06	33.295	60.008	2.400	0.737	0.817	4.639	49.050	100	50	5526921
6.28	33.010	56.055	2.569	0.758	0.837	4.933	46.945	103	51	4758261
6.84	33.544	64.000	2.250	0.717	0.797	5.069	51.000	85	42	5471036
6.14	32.898	54.660	2.634	0.765	0.844	4.879	46.160	107	54	4649947
3.67	34.572	90.493	1.591	0.603	0.659	2.356	59.647	133	67	16130848
8.59	33.156	58.004	2.483	0.747	0.828	6.596	48.005	73	37	3722472
7.48	32.818	53.707	2.681	0.771	0.849	5.941	45.610	90	45	3728175
7.17	33.894	70.803	2.034	0.684	0.762	5.066	53.920	76	38	6123574
5.88	33.856	69.994	2.057	0.688	0.766	4.206	53.599	92	46	7288421
4.77	34.194	78.138	1.843	0.652	0.723	3.259	56.516	107	54	10462283
5.06	33.835	69.540	2.071	0.690	0.768	3.651	53.416	107	54	8338560

<b>d<sub>PCC</sub></b> <b>(mils)</b>	<b>AREA<sub>PCC</sub></b>	<b>Radius of</b> <b>Relative</b> <b>Stiffness,</b> <b>I</b>	<b>L/l<sub>est</sub></b>	<b>AF d<sub>o</sub></b>	<b>AF I</b>	<b>Adj</b> <b>d<sub>PCC</sub></b>	<b>Adj I</b>	<b>Dynamic</b> <b>k-Value</b>	<b>Static</b> <b>k-Value</b>	<b>E<sub>PCC</sub></b>
5.93	34.322	81.858	1.759	0.636	0.704	3.926	57.620	86	43	9031630
6.50	34.360	83.031	1.734	0.632	0.698	4.255	57.939	78	39	8425625
7.38	33.073	56.879	2.532	0.753	0.833	5.737	47.398	87	43	4171268
6.55	32.434	49.603	2.903	0.794	0.869	5.384	43.128	111	56	3674733
6.54	33.497	63.198	2.279	0.721	0.801	4.881	50.623	89	45	5598442
6.30	33.238	59.159	2.434	0.741	0.822	4.846	48.613	97	49	5196717
5.00	33.793	68.681	2.097	0.694	0.773	3.629	53.063	109	55	8277103
5.19	34.363	83.156	1.732	0.631	0.697	3.426	57.972	97	49	10475580
7.38	30.535	36.329	3.964	0.874	0.930	6.658	33.785	146	73	1814173
5.36	33.874	70.364	2.047	0.686	0.764	3.835	53.747	101	50	8036965
6.88	33.463	62.644	2.299	0.723	0.804	5.145	50.357	86	43	5254369
6.85	33.946	71.967	2.001	0.679	0.755	4.810	54.370	79	39	6558653
8.53	29.650	32.385	4.447	0.899	0.946	7.877	30.628	150	75	1256773
6.94	34.438	85.597	1.682	0.622	0.684	4.457	58.588	73	37	8225672
6.67	33.625	65.443	2.200	0.709	0.789	4.901	51.662	85	43	5807527
7.69	33.402	61.650	2.336	0.728	0.809	5.770	49.874	78	39	4595633
6.52	34.160	77.226	1.865	0.656	0.728	4.430	56.224	80	40	7618076
5.36	34.617	92.294	1.560	0.597	0.650	3.335	59.979	93	47	11522913
6.79	32.205	47.460	3.034	0.806	0.880	5.666	41.756	113	56	3271379
6.63	33.304	60.142	2.394	0.736	0.817	5.050	49.119	92	46	5092156
5.57	33.642	65.752	2.190	0.708	0.788	4.111	51.800	101	51	6961882
6.58	33.102	57.265	2.515	0.751	0.831	5.117	47.608	96	48	4718822
6.11	34.104	75.773	1.900	0.662	0.736	4.200	55.741	86	43	7896985
6.05	34.017	73.610	1.956	0.671	0.747	4.217	54.981	88	44	7650856
5.08	33.924	71.461	2.015	0.681	0.758	3.620	54.176	105	53	8652059
6.86	31.327	40.830	3.527	0.846	0.911	6.002	37.177	134	67	2442442
5.39	33.695	66.749	2.157	0.703	0.783	3.951	52.241	104	52	7367718
4.33	32.502	50.273	2.864	0.790	0.866	3.607	43.547	163	81	5592562
7.23	33.855	69.977	2.058	0.688	0.766	5.136	53.592	76	38	5967379
5.80	34.253	79.804	1.804	0.645	0.715	3.894	57.028	88	44	8917829
5.11	34.416	84.880	1.697	0.624	0.688	3.335	58.413	98	49	10928082
5.34	33.598	64.950	2.217	0.712	0.792	3.970	51.438	106	53	7107757
6.68	33.672	66.308	2.172	0.705	0.785	4.878	52.047	85	42	5923121
5.34	33.913	71.236	2.021	0.682	0.759	3.800	54.089	101	50	8216361
5.93	32.937	55.129	2.612	0.763	0.842	4.700	46.426	110	55	4883220
8.38	30.161	34.545	4.168	0.885	0.937	7.629	32.378	138	69	1452378
9.63	31.844	44.469	3.238	0.824	0.894	8.129	39.752	87	43	2064506
7.33	32.728	52.679	2.734	0.776	0.854	5.868	45.006	94	47	3674102
7.04	33.722	67.272	2.141	0.701	0.780	5.098	52.467	80	40	5759664
6.32	33.588	64.788	2.223	0.713	0.793	4.668	51.364	91	45	6027434
7.45	32.724	52.631	2.736	0.777	0.855	5.965	44.978	92	46	3609615
7.46	33.501	63.281	2.276	0.720	0.801	5.542	50.662	78	39	4937679
6.85	33.766	68.133	2.114	0.697	0.775	4.935	52.834	81	41	6033915
6.03	33.263	59.522	2.419	0.739	0.820	4.631	48.801	101	51	5480504

<b>d<sub>PCC</sub></b> <b>(mils)</b>	<b>AREA<sub>PCC</sub></b>	<b>Radius of</b> <b>Relative</b> <b>Stiffness,</b> <b>I</b>	<b>L/l<sub>est</sub></b>	<b>AF d<sub>o</sub></b>	<b>AF I</b>	<b>Adj</b> <b>d<sub>PCC</sub></b>	<b>Adj I</b>	<b>Dynamic</b> <b>k-Value</b>	<b>Static</b> <b>k-</b> <b>Value</b>	<b>E<sub>PCC</sub></b>
6.75	33.565	64.369	2.237	0.715	0.795	4.992	51.171	85	43	5593816
4.52	33.486	63.017	2.285	0.721	0.802	3.431	50.536	127	64	7936962
7.56	33.289	59.908	2.404	0.737	0.818	5.746	48.999	81	40	4453062
6.85	33.153	57.961	2.484	0.748	0.828	5.299	47.982	91	46	4629263
7.67	32.039	46.036	3.128	0.815	0.887	6.442	40.815	104	52	2747809
6.84	33.062	56.729	2.538	0.754	0.834	5.334	47.316	93	47	4470639
7.38	33.917	71.307	2.019	0.682	0.759	5.188	54.117	74	37	6023375
6.18	33.076	56.910	2.530	0.753	0.833	4.833	47.415	103	51	4955604

**Cummulative %,Eastbound Lane**



**Table B.3. CDOT whitetopping thickness for 20-year traffic prediction (bonded–eastbound lane)**

**Colorado DOT Whitetopping Design (AI, Eff, Winter)**

**Bonded Slabs**

E <sub>AC</sub> =	1359876	PCC Poisson=	0.15	Trial Thickness=	3.5
t <sub>Base</sub> =	16.9	ACC Poisson=	0.35	Joint Spacing=	60
k=	57	Temperature Differential=	1.3	Existing Asphalt Fatigue=	30
E <sub>PCC</sub> =	6000000	N.A.=	7.08	P <sub>AC</sub> =	5.62
MR=	650	l <sub>e</sub> =	75.75	V <sub>V</sub> =	2.74
		L/l <sub>e</sub> =	.079		

Axle Load, kips	Critical Concrete Stresses and Asphalt Strains					
	Load Induced		Bond Adjustment		Loss of Support Adjustment	
	Stress, psi	Microstrain	Stress, psi	Microstrain	Stress, psi	Microstrain
1	2	3	4	5	6	7
<b>Single Axles</b>						
35	1	25	1	22	1	22
30	0	22	1	19	1	19
26	0	19	1	16	1	16
24	0	17	1	15	1	15
22	0	16	1	13	1	13
20	0	14	0	12	1	12
18	0	13	0	11	0	11
16	0	12	0	10	0	10
12	0	9	0	7	0	7
8	0	6	0	4	0	4
7	0	5	0	4	0	4
3	0	2	0	1	0	1
<b>Tandem Axles</b>						
60	0	17	1	15	1	15
55	0	16	1	13	1	13
50	0	14	1	12	1	12
46	0	13	0	11	1	11
44	0	13	0	10	0	10
42	0	12	0	10	0	10
40	0	11	0	9	0	9
38	0	11	0	9	0	9
36	0	10	0	8	0	8
34	0	10	0	8	0	8
32	0	9	0	7	0	7
30	0	9	0	7	0	7



Axle Load, kips	Expected Repetitions	Concrete Fatigue Analysis			Asphalt Fatigue Analysis		
		Concrete Stress Ratio	Allowable Repetitions, N	Fatigue Percent, %	Asphalt Microstrain	Allowable Repetitions, N	Fatigue Percent, %
1	8	9	10	11	12	13	14
<b>Single Axles</b> Percent Asphalt Concrete Fatigue Life Previously Consumed:							30
35	0	0.001	Unlimited	0.0	22	691588514	0.0
30	504	0.001	Unlimited	0.0	19	1171064542	0.0
26	0	0.001	Unlimited	0.0	16	1915289124	0.0
24	3961	0.001	Unlimited	0.0	15	2525652662	0.0
22	11702	0.001	Unlimited	0.0	13	3416249537	0.0
20	38322	0.001	Unlimited	0.0	12	4764277409	0.0
18	79837	0.001	Unlimited	0.0	11	6897740578	0.0
16	242208	0.001	Unlimited	0.0	10	10466725758	0.0
12	1235348	0.000	Unlimited	0.0	7	29512088266	0.0
8	165948	0.000	Unlimited	0.0	4	135205019314	0.0
7	4238911	0.000	Unlimited	0.0	4	228171366685	0.0
3	12592840	0.000	Unlimited	0.0	1	10714536949257	0.0
<b>Tandem Axles</b>							
60	3589	0.001	Unlimited	0.0	15	2622446134	0.0
55	1794	0.001	Unlimited	0.0	13	3547819359	0.0
50	4988	0.001	Unlimited	0.0	12	4948854914	0.0
46	20709	0.001	Unlimited	0.0	11	6632642204	0.0
44	3590	0.001	Unlimited	0.0	10	7758738720	0.0
42	18149	0.001	Unlimited	0.0	10	9147555310	0.0
40	31109	0.001	Unlimited	0.0	9	10878969089	0.0
38	85463	0.001	Unlimited	0.0	9	13063473215	0.0
36	120720	0.001	Unlimited	0.0	8	15856648407	0.0
34	178092	0.001	Unlimited	0.0	8	19481945019	0.0
32	105799	0.001	Unlimited	0.0	7	24267516006	0.0
30	219452	0.001	Unlimited	0.0	7	30707580046	0.0
			<b>Total Concrete Fatigue, % =</b>	0.0		<b>Total Asphalt Fatigue, % =</b>	30.0

**Table B.4. CDOT whitetopping thickness for 20-year traffic prediction (unbonded–eastbound lane)**

**Colorado DOT Whitetopping Design (AI, Eff, Winter)**

**Unbonded Slabs**

E <sub>Base</sub> =	1359876	PCC Poisson=	0.15	Trial Thickness=	4.5
t <sub>Base</sub> =	15.4	ACC Poisson=	0.35	Joint Spacing=	6
k=	52	Temperature Differential=	1.3	Existing Asphalt Fatigue=	30
E <sub>PCC</sub> =	7850000	N.A.=	5.95	P <sub>AC</sub> =	5.62
MR=	650	le=	78.35	V <sub>V</sub> =	2.74
		L/le=	0.08		

Axle Load, kips	Critical Concrete Stresses and Asphalt Strains					
	Load Induced		Bond Adjustment		Loss of Support Adjustment	
	Stress, psi	Microstrain	Stress, psi	Microstrain	Stress, psi	Microstrain
1	2	3	4	5	6	7
<b>Single Axles</b>						
35	0	21	0	18	0	18
30	0	18	0	15	0	15
26	0	15	0	13	0	13
24	0	14	0	12	0	12
22	0	13	0	11	0	11
20	0	12	0	10	0	10
18	0	11	0	9	0	9
16	0	9	0	8	0	8
12	0	7	0	6	0	6
8	0	5	0	3	0	3
7	0	4	0	3	0	3
3	0	2	0	1	0	1
<b>Tandem Axles</b>						
60	1	14	1	12	1	12
55	0	13	1	11	1	11
50	0	12	1	10	1	10
46	0	11	1	9	1	9
44	0	10	1	8	1	8
42	0	10	1	8	1	8
40	0	9	1	8	1	8
38	0	9	0	7	1	7
36	0	8	0	7	0	7
34	0	8	0	6	0	6
32	0	7	0	6	0	6
30	0	7	0	5	0	5

Axle Load, kips	Expected Repetitions	Concrete Fatigue Analysis			Asphalt Fatigue Analysis		
		Concrete Stress Ratio	Allowable Repetitions, N	Fatigue Percent, %	Asphalt Microstrain	Allowable Repetitions, N	Fatigue Percent, %
1	8	9	10	11	12	13	14
<b>Single Axles</b>						Percent Asphalt Concrete Fatigue Life Previously Consumed: 30	
35	0	0.000	Unlimited	0.0	18	1349487331	0.0
30	504	0.000	Unlimited	0.0	15	2295191788	0.0
26	0	0.000	Unlimited	0.0	13	3771947947	0.0
24	3961	0.000	Unlimited	0.0	12	4989173097	0.0
22	11702	0.000	Unlimited	0.0	11	6773049853	0.0
20	38322	0.000	Unlimited	0.0	10	9487459256	0.0
18	79837	0.000	Unlimited	0.0	9	13811416316	0.0
16	242208	0.000	Unlimited	0.0	8	21104216060	0.0
12	1235348	0.000	Unlimited	0.0	6	60815861991	0.0
8	165948	0.000	Unlimited	0.0	3	292290469635	0.0
7	4238911	0.000	Unlimited	0.0	3	504512781320	0.0
3	12592840	0.000	Unlimited	0.0	1	33985404151020	0.0
<b>Tandem Axles</b>							
60	3589	0.001	Unlimited	0.0	12	5375351188	0.0
55	1794	0.001	Unlimited	0.0	11	7300563274	0.0
50	4988	0.001	Unlimited	0.0	10	10231933224	0.0
46	20709	0.001	Unlimited	0.0	9	13776336002	0.0
44	3590	0.001	Unlimited	0.0	8	16157816096	0.0
42	18149	0.001	Unlimited	0.0	8	19105547494	0.0
40	31109	0.001	Unlimited	0.0	8	22795181297	0.0
38	85463	0.001	Unlimited	0.0	7	27471140969	0.0
36	120720	0.001	Unlimited	0.0	7	33479873434	0.0
34	178092	0.001	Unlimited	0.0	6	41322662461	0.0
32	105799	0.001	Unlimited	0.0	6	51741871632	0.0
30	219452	0.001	Unlimited	0.0	5	65866257320	0.0
			<b>Total Concrete Fatigue, % =</b>	0.0		<b>Total Asphalt Fatigue, % =</b>	30.0

**Table B.5. PCA whitetopping thickness for 20-year traffic prediction (bonded–eastbound lane)**

**PCA Whitetopping Design (AI, Eff, Winter)**

**Bonded Slabs**

$E_{AC}=$	1359876	PCC Poisson=	0.15	Trial Thickness=	3.5
$t_{AC}=$	16.9	ACC Poisson=	0.35	Joint Spacing=	60
$k=$	57	Temperature Differential=	1.3	Existing Asphalt Fatigue=	30
$E_{PCC}=$	6000000	PCC Coef. Of Thermal Expan.=	5.50E+00	$P_{AC}=$	5.62
$MR=$	650	$NA=$	7.08	$V_V=$	2.47
		$I_e=$	75.75		

Axle Load, kips	Multiplied by LSF	Critical Concrete Stresses and Asphalt Strains					
		Load Induced		Temperature Induced		Total	
		Stress, psi	Microstrain	Stress, psi	Microstrain	Stress, psi	Microstrain
1	2	3	4	5	6	7	8
<b>Single Axles</b>							
35	35	94	12	-10	-1	84	11
30	30	81	10	-10	-1	71	10
26	26	70	9	-10	-1	60	8
24	24	65	8	-10	-1	54	8
22	22	59	8	-10	-1	49	7
20	20	54	7	-10	-1	44	6
18	18	49	6	-10	-1	38	6
16	16	43	6	-10	-1	33	5
12	12	32	4	-10	-1	22	4
8	8	22	3	-10	-1	11	2
7	7	19	2	-10	-1	9	2
3	3	8	1	-10	-1	-2	0
<b>Tandem Axles</b>							
60	60	117	13	-10	-1	107	13
55	55	108	12	-10	-1	97	12
50	50	98	11	-10	-1	87	11
46	46	90	10	-10	-1	80	10
44	44	86	10	-10	-1	76	9
42	42	82	9	-10	-1	72	9
40	40	78	9	-10	-1	68	8
38	38	74	9	-10	-1	64	8
36	36	70	8	-10	-1	60	7
34	34	66	8	-10	-1	56	7
32	32	63	7	-10	-1	52	7
30	30	59	7	-10	-1	48	6

Axle Load, kips	Expected Repetitions	Concrete Fatigue Analysis			Asphalt Fatigue Analysis		
		Concrete Stress Ratio	Allowable Repetitions, N	Fatigue Percent, %	Asphalt Microstrain	Allowable Repetitions, N	Fatigue Percent, %
1	9	10	11	12	13	14	15
<b>Single Axles</b>							
35	0	0.129	Unlimited	0.0	11	8249426602	0.0
30	471	0.109	Unlimited	0.0	10	14132502607	0.0
26	0	0.092	Unlimited	0.0	8	23410601637	0.0
24	4936	0.084	Unlimited	0.0	8	31121598138	0.0
22	13897	0.075	Unlimited	0.0	7	42504428950	0.0
20	46454	0.067	Unlimited	0.0	6	59977366629	0.0
18	86535	0.059	Unlimited	0.0	6	88113810789	0.0
16	299737	0.051	Unlimited	0.0	5	136223154283	0.0
12	1547743	0.034	Unlimited	0.0	4	407330557745	0.0
8	193338	0.017	Unlimited	0.0	2	212835107365	0.0
7	3211582	0.013	Unlimited	0.0	2	3826023524879	0.0
3	8759889	-0.003	Unlimited	0.0	0	560975949646842	0.0
<b>Tandem Axles</b>							
60	4850	0.165	Unlimited	0.0	13	5727041078	0.0
55	2425	0.150	Unlimited	0.0	12	7741922845	0.0
50	6454	0.135	Unlimited	0.0	11	10789073855	0.0
46	18914	0.123	Unlimited	0.0	10	14446793284	0.0
44	4849	0.117	Unlimited	0.0	9	16890787351	0.0
42	24233	0.111	Unlimited	0.0	9	19902815656	0.0
40	42024	0.104	Unlimited	0.0	8	23654893944	0.0
38	113822	0.098	Unlimited	0.0	8	28384691222	0.0
36	162742	0.092	Unlimited	0.0	7	34426423255	0.0
34	237278	0.086	Unlimited	0.0	7	42259402234	0.0
32	137234	0.080	Unlimited	0.0	7	52586375617	0.0
30	277840	0.074	Unlimited	0.0	6	66463748070	0.0
			<b>Total Concrete Fatigue, % =</b>	0.0		<b>Total Asphalt Fatigue, % =</b>	0.0

**Table B.6. PCA whitetopping thickness for 20-year traffic prediction (unbonded–  
eastbound lane)**

**Whitetopping thickness for 20-year Traffic Prediction**

**PCA Whitetopping Design (AI, Eff, Winter)**

**Unbonded Slabs**

E <sub>AC</sub> =	1359876	PCC Poisson=	0.15	Trial Thickness=	4.5
t <sub>AC</sub> =	15.4	ACC Poisson=	0.35	Joint Spacing=	60
k=	52	Temperature Differential=	1.3	Existing Asphalt	30
				Fatigue=	
E <sub>PCC</sub> =	7850000	PCC Coef. Of Thermal	5.50E+00	P <sub>AC</sub> =	5.62
		Expan.=			
MR=	650	NA=	5.95	V <sub>V</sub> =	2.74
		l <sub>e</sub> =	78.35		

Axle Load, kips	Multiplied by LSF	Critical Concrete Stresses and Asphalt Strains					
		Load Induced		Temperature Induced		Total	
		Stress, psi	Microstrain	Stress, psi	Microstrain	Stress, psi	Microstrain
1	2	3	4	5	6	7	8
<b>Single Axles</b>							
35	35	92	10	-10	-1	82	9
30	30	79	9	-10	-1	69	8
26	26	68	8	-10	-1	59	7
24	24	63	7	-10	-1	53	6
22	22	58	7	-10	-1	48	6
20	20	53	6	-10	-1	43	5
18	18	47	5	-10	-1	38	4
16	16	42	5	-10	-1	32	4
12	12	32	4	-10	-1	22	3
8	8	21	2	-10	-1	11	1
7	7	18	2	-10	-1	9	1
3	3	8	1	-10	-1	-2	0
<b>Tandem Axles</b>							
60	60	115	12	-10	-1	105	11
55	55	105	11	-10	-1	95	10
50	50	95	10	-10	-1	86	9
46	46	88	9	-10	-1	78	8
44	44	84	9	-10	-1	74	8
42	42	80	8	-10	-1	70	7
40	40	76	8	-10	-1	67	7
38	38	73	8	-10	-1	63	7
36	36	69	7	-10	-1	59	6
34	34	65	7	-10	-1	55	6
32	32	61	6	-10	-1	51	5
30	30	57	6	-10	-1	47	5

Axle Load, kips	Expected Repetitions	Concrete Fatigue Analysis			Asphalt Fatigue Analysis		
		Concrete Stress Ratio	Allowable Repetitions, N	Fatigue Percent, %	Asphalt Microstrain	Allowable Repetitions, N	Fatigue Percent, %
1	9	10	11	12	13	14	15
<b>Single Axles</b>							
35	0	0.127	Unlimited	0.0	9	15912380968	0.0
30	471	0.106	Unlimited	0.0	8	28150430079	0.0
26	0	0.090	Unlimited	0.0	7	48324292909	0.0
24	4936	0.082	Unlimited	0.0	6	65727357782	0.0
22	13897	0.074	Unlimited	0.0	6	92281662146	0.0
20	46454	0.066	Unlimited	0.0	5	134725856289	0.0
18	86535	0.058	Unlimited	0.0	4	206620728515	0.0
16	299737	0.050	Unlimited	0.0	4	337828229415	0.0
12	1547743	0.033	Unlimited	0.0	3	1215396040455	0.0
8	193338	0.017	Unlimited	0.0	1	10170711350111	0.0
7	3211582	0.013	Unlimited	0.0	1	23711075888810	0.0
3	8759889	-0.003	Unlimited	0.0	0	Unlimited	0.0
<b>Tandem Axles</b>							
60	4850	0.161	Unlimited	0.0	11	9581221563	0.0
55	2425	0.146	Unlimited	0.0	10	13138133135	0.0
50	6454	0.132	Unlimited	0.0	9	18630062902	0.0
46	18914	0.120	Unlimited	0.0	8	25370920707	0.0
44	4849	0.114	Unlimited	0.0	8	29952582651	0.0
42	24233	0.108	Unlimited	0.0	7	35675049747	0.0
40	42024	0.102	Unlimited	0.0	7	42909904140	0.0
38	113822	0.097	Unlimited	0.0	7	52181956939	0.0
36	162742	0.091	Unlimited	0.0	6	64247546408	0.0
34	237278	0.085	Unlimited	0.0	6	80221711643	0.0
32	137234	0.079	Unlimited	0.0	5	101791169817	0.0
30	277840	0.073	Unlimited	0.0	5	131583617181	0.0
			<b>Total Concrete Fatigue, % =</b>	0.0		<b>Total Asphalt Fatigue, % =</b>	0.0

**Table B.7. Westbound lane backcalculation of layer parameters**

**Calculated Values**

**FWD inputs**

$E_{ACC}$	1359876	$P=$	9000
$d_{o \text{ compress}}$ (Bonded)	0.114081 mils	$a=$	5.9
$d_{o \text{ compress}}$ (Unbonded)	0.2333 mils	$F=$	18
		$t_w=$	0.003

Station	Lane	Joint or Mid slab	Load (kips)		Pavement Surface Deflections d <sub>i</sub> (mils)										Modified Surface Deflections, d <sub>i</sub>			
			Kips	lbs	d <sub>0</sub> (mils)	d <sub>8</sub> (mils)	d <sub>12</sub> (mils)	d <sub>18</sub> (mils)	d <sub>24</sub> (mils)	d <sub>36</sub> (mils)	d <sub>48</sub> (mils)	d <sub>60</sub> (mils)	d <sub>12</sub> (mils)	d <sub>0</sub> (mils)	d <sub>12</sub> (mils)	d <sub>24</sub> (mils)	d <sub>36</sub> (mils)	
5	1	1	9.19	9190	4.43	4.33	4.23	4.07	3.86	3.46	2.95	2.53	4.2	5.30	5.06	4.62	4.14	
6	1	1	9.1	9100	4.11	4.03	3.94	3.79	3.66	3.32	2.9	2.54	5.61	4.97	4.76	4.43	4.01	
7	1	1	9.19	9190	3.4	3.33	3.26	3.13	3.01	2.73	2.38	2.01	3.69	4.07	3.90	3.60	3.27	
8	1	1	9.04	9040	4.2	3.92	3.81	3.63	3.42	3.05	2.59	2.15	4.96	5.11	4.64	4.16	3.71	
9	1	1	9.11	9110	3.8	3.61	3.62	3.46	3.3	3.01	2.61	2.28	5.2	4.59	4.37	3.99	3.64	
10	1	1	8.91	8910	5.44	5.27	5.26	5.02	4.82	4.4	3.84	3.37	4.29	6.72	6.50	5.95	5.43	
11	1	1	8.97	8970	3.97	3.8	3.83	3.68	3.53	3.19	2.74	2.35	3.45	4.87	4.70	4.33	3.91	
12	1	1	8.99	8990	4.18	4.02	3.99	3.84	3.68	3.34	2.9	2.55	4.41	5.12	4.88	4.50	4.09	
13	1	1	8.9	8900	3.74	3.63	3.55	3.39	3.21	2.85	2.41	2.05	4.49	4.62	4.39	3.97	3.52	
14	1	1	8.95	8950	4.11	4.01	3.94	3.81	3.65	3.33	2.87	2.48	4.41	5.05	4.84	4.49	4.09	
15	1	1	8.95	8950	4.06	3.92	3.86	3.71	3.53	3.17	2.7	2.31	3.73	4.99	4.75	4.34	3.90	
16	1	1	8.38	8380	3.43	3.38	3.32	3.19	3.07	2.76	2.38	2.1	4.95	4.50	4.36	4.03	3.62	
17	1	1	8.77	8770	4.62	4.41	4.33	4.14	3.96	3.55	3.04	2.6	4.95	5.80	5.43	4.97	4.45	
18	1	1	8.95	8950	4	3.89	3.83	3.67	3.5	3.15	2.69	2.29	4.42	4.92	4.71	4.30	3.87	
19	1	1	8.86	8860	4.66	4.58	4.52	4.36	4.19	3.82	3.32	2.89	2.99	5.79	5.61	5.20	4.74	
20	1	1	8.8	8800	4.8	4.69	4.62	4.45	4.27	3.9	3.38	2.96	2.51	6.00	5.78	5.34	4.88	
21	1	1	8.94	8940	4.12	4.02	3.96	3.83	3.71	3.41	2.99	2.64	6.17	5.07	4.87	4.57	4.20	
22	1	1	8.72	8720	4.13	4	3.93	3.77	3.59	3.19	2.7	2.26	5.19	5.21	4.96	4.53	4.03	
23	1	1	8.79	8790	3.92	3.83	3.79	3.64	3.52	3.21	2.8	2.44	5.59	4.91	4.74	4.41	4.02	
24	1	1	8.81	8810	4.13	4.01	4	3.88	3.75	3.42	2.94	2.55	5.28	5.16	5.00	4.68	4.27	
25	1	1	8.86	8860	3.75	3.59	3.57	3.43	3.29	3.01	2.6	2.29	4.69	4.66	4.43	4.09	3.74	
26	1	1	8.64	8640	4.73	4.38	4.43	4.18	3.94	3.45	2.84	2.33	4.68	6.02	5.64	5.02	4.39	
27	1	1	8.67	8670	4.03	4	3.89	3.72	3.58	3.24	2.81	2.42	5.07	5.11	4.94	4.54	4.11	
28	1	1	8.84	8840	4.61	4.54	4.39	4.2	4.03	3.68	3.19	2.78	4.12	5.74	5.46	5.02	4.58	
29	1	1	8.82	8820	4.54	4.42	4.26	4.04	3.83	3.41	2.92	2.47	4.69	5.66	5.31	4.78	4.25	
30	1	1	8.72	8720	4.36	4.31	4.2	4.06	3.9	3.55	3.07	2.67	4.7	5.50	5.30	4.92	4.48	
31	1	1	8.76	8760	4.37	4.32	4.19	4.03	3.85	3.5	3.04	2.63	4.49	5.49	5.26	4.84	4.40	
32	1	1	8.72	8720	4.42	4.36	4.23	4.07	3.87	3.51	3.03	2.61	5.01	5.58	5.34	4.88	4.43	
33	1	1	8.71	8710	3.73	3.71	3.6	3.47	3.32	3	2.6	2.25	3.99	4.71	4.55	4.19	3.79	
34	1	1	8.86	8860	4.55	4.52	4.4	4.22	4.04	3.65	3.1	2.62	4.37	5.65	5.46	5.02	4.53	
35	1	1	8.7	8700	3.92	3.91	3.8	3.67	3.52	3.22	2.8	2.42	3.31	4.96	4.81	4.45	4.07	
36	1	1	8.7	8700	3.83	3.78	3.67	3.53	3.39	3.09	2.68	2.32	4.48	4.84	4.64	4.29	3.91	
37	1	1	8.62	8620	4.17	4.14	4.01	3.88	3.73	3.41	3.01	2.63	5.45	5.32	5.12	4.76	4.35	
38	1	1	8.61	8610	4.38	4.34	4.22	4.08	3.91	3.57	3.09	2.7	4.09	5.60	5.39	5.00	4.56	



Station	Lane	Joint or Mid slab	Load (kips)		Pavement Surface Deflections d <sub>i</sub> (mils)									Modified Surface Deflections, d <sub>i</sub>			
			Kips	lbs	d <sub>0</sub> (mils)	d <sub>8</sub> (mils)	d <sub>12</sub> (mils)	d <sub>18</sub> (mils)	d <sub>24</sub> (mils)	d <sub>36</sub> (mils)	d <sub>48</sub> (mils)	d <sub>60</sub> (mils)	d <sub>12</sub> (mils)	d <sub>0</sub> (mils)	d <sub>12</sub> (mils)	d <sub>24</sub> (mils)	d <sub>36</sub> (mils)
39	1	1	8.56	8560	4.76	4.75	4.61	4.46	4.3	3.96	3.47	3.06	3.21	6.12	5.93	5.53	5.09
40	1	1	8.6	8600	4.62	4.67	4.59	4.51	4.42	3.9	3.2	2.72	4.29	5.91	5.87	5.66	4.99
41	1	1	8.46	8460	4.41	4.35	4.23	4.06	3.88	3.51	3.02	2.57	3.79	5.74	5.50	5.05	4.57
42	1	1	8.55	8550	3.79	3.77	3.66	3.51	3.39	3.1	2.72	2.39	4.27	4.88	4.71	4.36	3.99
43	1	1	8.66	8660	4.59	4.55	4.4	4.23	4.04	3.63	3.11	2.64	4.03	5.83	5.59	5.13	4.61
44	1	1	8.61	8610	3.92	3.79	3.67	3.54	3.41	3.11	2.7	2.38	4.24	5.01	4.69	4.36	3.97
46	1	1	8.74	8740	4.09	4.03	3.91	3.77	3.6	3.26	2.82	2.47	3.93	5.15	4.92	4.53	4.10
47	1	1	8.51	8510	5.06	4.97	4.78	4.54	4.33	3.88	3.32	2.84	4.93	6.54	6.18	5.60	5.02
48	1	1	8.26	8260	4.23	4.11	3.98	3.79	3.6	3.18	2.71	2.31	5.93	5.63	5.30	4.80	4.24
49	1	1	8.33	8330	4.67	4.63	4.47	4.28	4.04	3.57	2.97	2.36	6.93	6.17	5.90	5.34	4.72
50	1	1	8.39	8390	5.56	5.56	5.37	5.17	4.94	4.44	3.79	3.25	7.93	7.29	7.04	6.48	5.82
51	1	1	8.6	8600	5.63	5.57	5.39	5.19	4.94	4.45	3.8	3.26	8.93	7.20	6.90	6.32	5.69
52	1	1	8.5	8500	3.58	3.53	3.44	3.31	3.2	2.96	2.61	2.31	9.93	4.63	4.45	4.14	3.83
53	1	1	9.2	9200	4.74	4.59	4.43	4.25	4.04	3.62	3.08	2.62	10.93	5.67	5.30	4.83	4.33
54	1	1	9.21	9210	4.39	4.35	4.24	4.1	3.93	3.62	3.17	2.75	4.2	5.24	5.07	4.70	4.32
55	1	1	9.14	9140	5.89	5.85	5.65	5.41	5.12	4.52	3.78	3.17	5.61	7.09	6.80	6.16	5.44
56	1	1	9.17	9170	3.92	3.84	3.7	3.53	3.36	2.98	2.49	2.11	3.69	4.70	4.44	4.03	3.58
57	1	1	9.1	9100	5.17	5.11	4.98	4.77	4.56	4.1	3.48	2.99	4.96	6.25	6.02	5.51	4.96
58	1	1	9.15	9150	5.51	5.47	5.3	5.09	4.87	4.35	3.68	3.13	5.2	6.63	6.37	5.86	5.23
59	1	1	9.2	9200	4.5	4.48	4.36	4.19	3.99	3.6	3.11	2.7	4.29	5.38	5.21	4.77	4.31
60	1	1	8.96	8960	3.67	3.66	3.52	3.36	3.18	2.8	2.34	1.94	3.45	4.51	4.32	3.91	3.44
61	1	1	8.99	8990	4.66	4.61	4.45	4.23	4.01	3.5	2.91	2.41	4.41	5.70	5.45	4.91	4.28
62	1	1	9.02	9020	4.72	4.67	4.51	4.31	4.08	3.58	3	2.49	4.49	5.76	5.50	4.98	4.37
63	1	1	9.12	9120	4.73	4.67	4.53	4.33	4.15	3.73	3.16	2.67	4.41	5.71	5.47	5.01	4.50
64	1	1	9.04	9040	3.94	3.91	3.78	3.6	3.44	3.08	2.62	2.34	3.73	4.80	4.60	4.19	3.75
65	1	1	9.1	9100	5.2	5.17	5	4.79	4.54	4.04	3.4	2.89	4.95	6.29	6.05	5.49	4.89
66	1	1	8.95	8950	5.22	5.18	5.03	4.84	4.63	4.17	3.57	3.04	4.95	6.42	6.18	5.69	5.13
67	1	1	9.14	9140	4.67	4.6	4.47	4.3	4.13	3.77	3.26	2.83	4.42	5.62	5.38	4.97	4.54
68	1	1	9.1	9100	3.17	3.1	3	2.89	2.78	2.56	2.23	1.95	2.99	3.83	3.63	3.36	3.10
69	1	1	9.17	9170	2.68	2.63	2.54	2.46	2.37	2.19	1.94	1.78	2.51	3.22	3.05	2.84	2.63
70	1	1	8.86	8860	6.55	6.52	6.3	6.04	5.73	5.05	4.24	3.49	6.17	8.13	7.82	7.12	6.27
71	1	1	9.04	9040	5.55	5.51	5.34	5.12	4.85	4.29	3.56	2.96	5.19	6.76	6.50	5.90	5.22
72	1	1	8.97	8970	5.89	5.87	5.71	5.51	5.29	4.8	4.16	3.34	5.59	7.23	7.00	6.49	5.89
73	1	1	8.89	8890	5.53	5.5	5.33	5.12	4.89	4.39	3.76	3.22	5.28	6.84	6.60	6.05	5.43
74	1	1	8.85	8850	4.98	4.98	4.81	4.64	4.43	3.96	3.33	2.78	4.69	6.19	5.98	5.51	4.92
75	1	1	9.02	9020	4.98	4.81	4.64	4.4	4.15	3.61	2.99	2.46	4.68	6.08	5.66	5.06	4.40
76	1	1	8.71	8710	5.37	5.36	5.18	4.95	4.69	4.12	3.43	2.81	5.07	6.78	6.54	5.92	5.20
77	1	1	8.61	8610	4.32	4.28	4.15	3.99	3.8	3.42	2.9	2.46	4.12	5.52	5.30	4.86	4.37
78	1	1	9.01	9010	4.98	4.9	4.75	4.57	4.31	3.81	3.19	2.63	4.69	6.08	5.80	5.26	4.65
79	1	1	9	9000	5	4.92	4.76	4.54	4.31	3.81	3.18	2.64	4.7	6.11	5.82	5.27	4.66
80	1	1	8.82	8820	4.7	4.65	4.51	4.31	4.11	3.69	3.15	2.66	4.49	5.86	5.63	5.13	4.60
81	1	1	8.89	8890	5.44	5.33	5.15	4.92	4.65	4.08	3.39	2.86	5.01	6.73	6.37	5.76	5.05
82	1	1	8.92	8920	4.24	4.21	4.11	3.95	3.8	3.43	2.89	2.47	3.99	5.23	5.07	4.69	4.23
83	1	1	9.02	9020	4.55	4.43	4.3	4.07	3.83	3.36	2.79	2.3	4.37	5.55	5.25	4.67	4.10

Station	Lane	Joint or Mid slab	Load (kips)		Pavement Surface Deflections $d_i$ (mils)									Modified Surface Deflections, $d_i$			
			Kips	lbs	$d_0$ (mils)	$d_8$ (mils)	$d_{12}$ (mils)	$d_{18}$ (mils)	$d_{24}$ (mils)	$d_{36}$ (mils)	$d_{48}$ (mils)	$d_{60}$ (mils)	$d_{12}$ (mils)	$d_0$ (mils)	$d_{12}$ (mils)	$d_{24}$ (mils)	$d_{36}$ (mils)
84	1	1	9.14	9140	3.52	3.44	3.32	3.17	2.94	2.55	2.09	1.71	3.31	4.24	4.00	3.54	3.07
85	1	1	9.07	9070	4.77	4.64	4.51	4.3	4.09	3.66	3.08	2.65	4.48	5.79	5.47	4.96	4.44
86	1	1	8.84	8840	5.87	5.79	5.63	5.44	5.22	4.31	3.35	2.64	5.45	7.31	7.01	6.50	5.36
87	1	1	8.97	8970	4.66	4.22	4.05	3.84	3.65	3.26	2.75	2.34	4.09	5.72	4.97	4.48	4.00
88	1	1	9.09	9090	3.48	3.35	3.22	3.08	2.91	2.57	2.17	1.85	3.21	4.21	3.90	3.52	3.11
89	1	1	9.01	9010	4.54	4.46	4.33	4.16	3.96	3.53	2.96	2.45	4.29	5.54	5.29	4.84	4.31
90	1	1	9.07	9070	3.98	3.85	3.73	3.55	3.36	2.99	2.52	2.12	3.79	4.83	4.53	4.08	3.63
91	1	1	9.06	9060	4.44	4.41	4.31	4.16	4	3.64	3.17	2.72	4.27	5.39	5.23	4.86	4.42
92	1	1	8.91	8910	4.48	4.25	4.09	3.92	3.74	3.34	2.81	2.38	4.03	5.53	5.05	4.62	4.12
93	1	1	8.9	8900	4.64	4.56	4.41	4.19	3.95	3.48	2.91	2.44	4.24	5.74	5.45	4.88	4.30
94	1	1	8.89	8890	3.14	3.08	2.98	2.83	2.68	2.4	2.02	1.79	2.93	3.89	3.69	3.32	2.97

**Table B.7a. Bonded layer condition (westbound lane)**

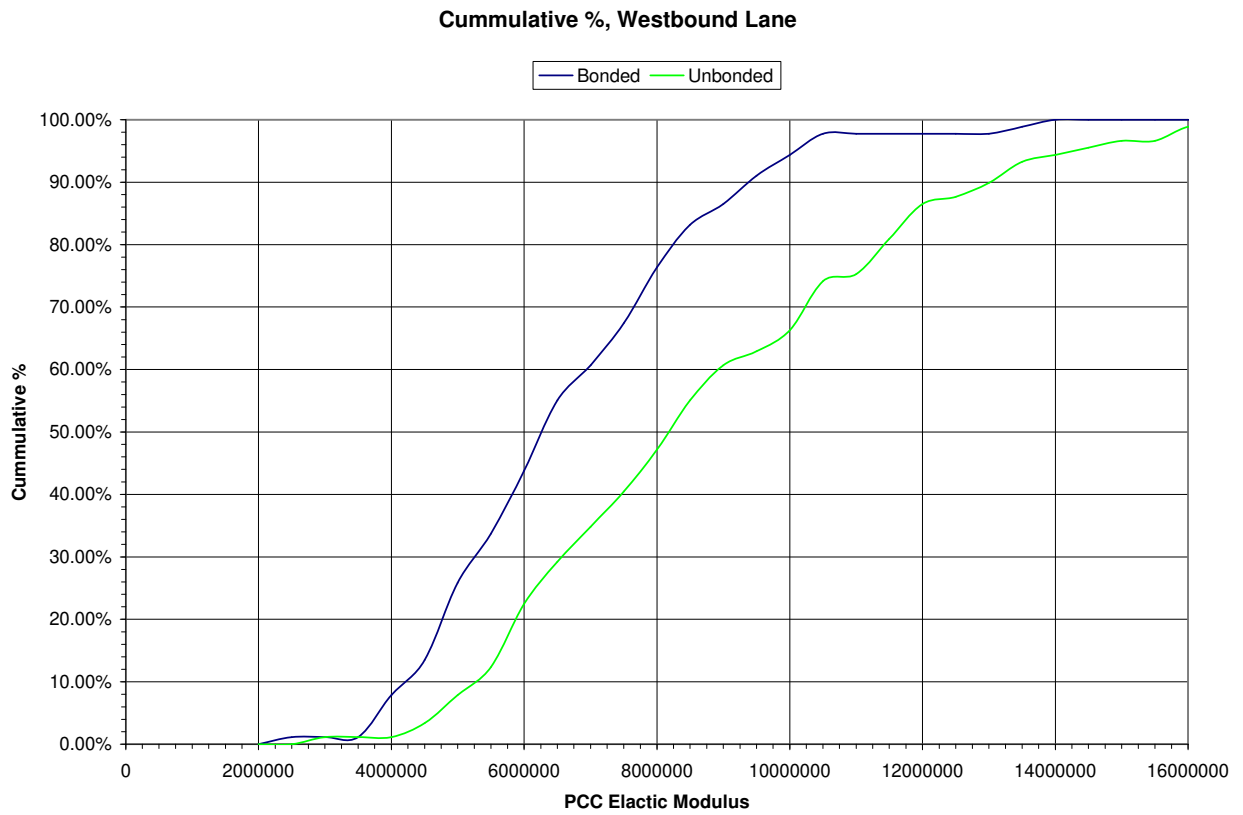
<b>d<sub>PCC</sub> (mils)</b>	<b>AREA<sub>PCC</sub>, in</b>	<b>Radius of Relative Stiffness, I</b>	<b>L/I<sub>est</sub></b>	<b>AF d<sub>o</sub></b>	<b>AF I</b>	<b>Adj d<sub>PCC</sub></b>	<b>Adj I</b>	<b>Dynamic k-Value</b>	<b>Static k-Value</b>	<b>E<sub>PCC</sub></b>
5.19	33.185	58.408	2.465	0.745	0.826	3.953	48.219	121	61	6267852
4.86	33.672	66.310	2.172	0.705	0.785	3.505	52.048	118	59	8243786
3.96	33.724	67.308	2.139	0.700	0.780	2.852	52.483	142	71	10303742
5.00	31.585	42.565	3.383	0.836	0.903	4.272	38.424	176	88	3667718
4.48	33.283	59.829	2.407	0.738	0.818	3.386	48.959	137	69	7544196
6.60	33.556	64.219	2.242	0.715	0.796	4.807	51.102	89	44	5793297
4.76	33.717	67.178	2.144	0.701	0.780	3.414	52.427	119	60	8587117
5.00	33.425	62.019	2.322	0.727	0.807	3.717	50.054	120	60	7185945
4.51	32.926	55.003	2.618	0.763	0.843	3.530	46.355	147	73	6481547
4.94	33.646	65.832	2.187	0.708	0.787	3.575	51.836	116	58	8015351
4.88	33.148	57.885	2.488	0.748	0.828	3.733	47.941	130	65	6558838
4.39	33.890	70.723	2.036	0.684	0.762	3.083	53.889	125	62	10052022
5.68	32.668	52.012	2.769	0.780	0.858	4.522	44.608	124	62	4683272
4.80	33.349	60.829	2.367	0.733	0.813	3.603	49.466	127	63	7239379
5.67	33.898	70.885	2.031	0.684	0.761	3.957	53.953	97	49	7849739
5.89	33.625	65.448	2.200	0.709	0.789	4.258	51.664	98	49	6685318
4.96	33.934	71.699	2.008	0.680	0.757	3.448	54.268	110	55	9113881
5.10	33.077	56.929	2.529	0.753	0.833	3.925	47.425	126	63	6105013
4.79	33.940	71.837	2.005	0.679	0.756	3.334	54.321	114	57	9445219
5.04	34.108	75.876	1.898	0.662	0.735	3.412	55.776	105	53	9732366
4.54	33.440	62.266	2.313	0.725	0.806	3.378	50.175	131	66	7945953
5.91	32.105	46.595	3.090	0.811	0.884	4.888	41.187	134	67	3688261
5.00	33.684	66.551	2.164	0.704	0.784	3.601	52.154	114	57	8056288
5.62	33.249	59.321	2.427	0.740	0.821	4.249	48.697	111	55	5948214
5.55	32.422	49.484	2.910	0.795	0.870	4.500	43.053	134	67	4380934
5.39	33.754	67.904	2.121	0.698	0.777	3.838	52.737	105	52	7730132
5.38	33.454	62.489	2.304	0.724	0.805	3.975	50.283	111	56	6781566
5.46	33.314	60.293	2.388	0.735	0.816	4.101	49.195	112	56	6289331
4.60	33.761	68.027	2.117	0.697	0.776	3.285	52.789	122	61	9050721
5.54	33.630	65.544	2.197	0.709	0.789	4.006	51.707	104	52	7117377
4.84	33.981	72.758	1.979	0.675	0.751	3.348	54.668	112	56	9527177
4.73	33.611	65.194	2.209	0.711	0.791	3.443	51.549	122	61	8231932
5.21	33.775	68.318	2.108	0.696	0.774	3.703	52.912	108	54	8065519
5.48	33.730	67.416	2.136	0.700	0.779	3.918	52.529	103	52	7512396
6.00	33.975	72.637	1.982	0.676	0.752	4.135	54.623	91	45	7700722
5.80	35.028	113.872	1.265	0.528	0.541	3.118	61.623	94	47	13012129
5.62	33.388	61.435	2.344	0.729	0.810	4.184	49.767	108	54	6309969
4.76	33.882	70.540	2.041	0.685	0.763	3.343	53.817	115	58	9245314
5.72	33.345	60.766	2.370	0.733	0.814	4.274	49.434	107	53	6093861
4.90	33.050	56.569	2.546	0.755	0.835	3.782	47.228	132	66	6281641
5.04	33.424	62.007	2.322	0.727	0.807	3.741	50.049	119	60	7137667
6.43	32.671	52.043	2.767	0.780	0.858	5.103	44.627	110	55	4153735
5.52	32.552	50.784	2.836	0.787	0.864	4.435	43.862	131	65	4615250
6.05	32.952	55.326	2.603	0.762	0.841	4.699	46.537	110	55	4908243

<b>d<sub>PCC</sub> (mils)</b>	<b>AREA<sub>PCC</sub>, in</b>	<b>Radius of Relative Stiffness, I</b>	<b>L/l<sub>est</sub></b>	<b>AF d<sub>o</sub></b>	<b>AF I</b>	<b>Adj d<sub>PCC</sub></b>	<b>Adj I</b>	<b>Dynamic k-Value</b>	<b>Static k-Value</b>	<b>E<sub>PCC</sub></b>
7.18	33.473	62.804	2.293	0.723	0.803	5.269	50.435	83	42	5147303
7.09	33.191	58.489	2.462	0.745	0.825	5.365	48.262	89	45	4626069
4.52	33.905	71.044	2.027	0.683	0.760	3.165	54.015	121	60	9835758
5.56	32.560	50.867	2.831	0.787	0.863	4.459	43.913	130	65	4600938
5.13	33.887	70.650	2.038	0.685	0.762	3.592	53.860	107	54	8618167
6.98	32.981	55.682	2.586	0.760	0.839	5.388	46.737	95	47	4318046
4.59	32.824	53.775	2.678	0.770	0.849	3.623	45.650	148	74	6123622
6.14	33.401	61.642	2.336	0.728	0.809	4.554	49.870	99	49	5822090
6.51	33.357	60.940	2.363	0.732	0.813	4.850	49.522	94	47	5389313
5.27	33.653	65.957	2.183	0.707	0.787	3.805	51.892	109	54	7547879
4.39	33.173	58.235	2.473	0.746	0.826	3.363	48.128	143	72	7339277
5.59	32.828	53.827	2.675	0.770	0.849	4.392	45.680	122	61	5058665
5.64	32.923	54.965	2.620	0.764	0.843	4.397	46.333	118	59	5198746
5.59	33.298	60.052	2.398	0.737	0.817	4.204	49.073	110	55	6105591
4.68	33.330	60.536	2.379	0.734	0.815	3.521	49.318	130	65	7363858
6.17	33.170	58.194	2.474	0.746	0.827	4.693	48.106	103	51	5254467
6.30	33.489	63.065	2.283	0.721	0.802	4.629	50.559	94	47	5888346
5.51	33.500	63.260	2.276	0.720	0.801	4.049	50.652	107	54	6755409
3.72	33.545	64.031	2.249	0.716	0.797	2.746	51.015	156	78	10105775
3.10	33.877	70.439	2.044	0.686	0.763	2.205	53.777	175	88	13992080
8.02	33.045	56.507	2.548	0.755	0.835	6.144	47.194	82	41	3861259
6.64	33.128	57.622	2.499	0.749	0.830	5.062	47.800	96	48	4808626
7.11	33.738	67.591	2.130	0.699	0.778	5.051	52.604	80	40	5843742
6.73	33.397	61.572	2.339	0.729	0.809	4.988	49.835	90	45	5307389
6.08	33.544	64.001	2.250	0.717	0.797	4.437	51.001	97	48	6251302
5.96	32.019	45.867	3.139	0.816	0.887	4.956	40.701	136	68	3551760
6.67	33.115	57.442	2.507	0.750	0.830	5.090	47.703	96	48	4762814
5.41	33.399	61.612	2.337	0.729	0.809	4.022	49.855	112	56	6587127
5.97	32.927	55.008	2.618	0.763	0.843	4.643	46.358	112	56	4928632
6.00	32.841	53.973	2.668	0.769	0.848	4.702	45.765	113	57	4742608
5.75	33.249	59.328	2.427	0.740	0.821	4.341	48.700	108	54	5822135
6.62	32.568	50.950	2.826	0.786	0.863	5.293	43.964	109	54	3885218
5.12	33.848	69.819	2.062	0.689	0.767	3.602	53.529	108	54	8487970
5.44	32.415	49.420	2.914	0.795	0.870	4.412	43.013	136	68	4459869
4.12	32.398	49.252	2.924	0.796	0.871	3.373	42.907	179	90	5805601
5.67	32.767	53.113	2.711	0.774	0.852	4.479	45.263	121	61	4869548
7.19	33.008	56.025	2.570	0.758	0.838	5.538	46.928	91	46	4235531
5.60	30.515	36.229	3.975	0.875	0.930	5.001	33.707	195	97	2403684
4.10	32.281	48.147	2.991	0.802	0.877	3.380	42.202	185	92	5602775
5.43	33.135	57.718	2.495	0.749	0.829	4.152	47.852	117	59	5875629
4.71	32.511	50.366	2.859	0.789	0.866	3.812	43.604	154	77	5306275
5.28	33.970	72.515	1.986	0.676	0.753	3.647	54.577	103	51	8716290
5.42	31.982	45.568	3.160	0.818	0.889	4.523	40.500	150	75	3852686
5.62	32.651	51.828	2.778	0.781	0.859	4.481	44.497	126	63	4702238
3.77	33.009	56.046	2.569	0.758	0.838	2.945	46.940	172	86	7968045

**Table B.7b. Unbonded layer condition (westbound lane)**

<b>d<sub>PCC</sub> (mils)</b>	<b>AREA<sub>PCC</sub></b>	<b>Radius of Relative Stiffness, I</b>	<b>L/l<sub>est</sub></b>	<b>AF d<sub>o</sub></b>	<b>AF I</b>	<b>Adj d<sub>PCC</sub></b>	<b>Adj I</b>	<b>Dynamic k-Value</b>	<b>Static k-Value</b>	<b>E<sub>PCC</sub></b>
5.07	33.824	69.323	2.077	0.691	0.769	3.665	53.328	107	54	8278914
4.74	34.368	83.309	1.729	0.631	0.696	3.134	58.012	106	53	11467097
3.84	34.585	91.007	1.582	0.601	0.656	2.448	59.745	128	64	15575672
4.88	32.210	47.512	3.031	0.806	0.880	4.121	41.790	155	77	4505359
4.36	34.030	73.930	1.948	0.670	0.745	3.075	55.096	120	60	10535605
6.48	34.063	74.729	1.927	0.666	0.741	4.478	55.380	81	41	7311119
4.64	34.430	85.338	1.687	0.623	0.686	3.033	58.526	108	54	12063462
4.88	34.095	75.525	1.907	0.663	0.737	3.392	55.656	106	53	9747621
4.39	33.658	66.045	2.180	0.707	0.786	3.267	51.931	127	63	8804092
4.82	34.330	82.106	1.754	0.635	0.703	3.211	57.689	105	52	11067392
4.76	33.828	69.395	2.075	0.691	0.769	3.447	53.357	114	57	8811539
4.27	34.669	94.450	1.525	0.589	0.639	2.653	60.334	116	58	14659081
5.56	33.239	59.181	2.433	0.741	0.822	4.296	48.624	110	55	5864719
4.68	34.046	74.305	1.938	0.668	0.743	3.287	55.230	111	56	9905731
5.55	34.496	87.657	1.643	0.614	0.674	3.552	59.062	90	45	10488914
5.77	34.196	78.205	1.841	0.652	0.723	3.911	56.538	89	45	8726864
4.84	34.623	92.513	1.557	0.596	0.649	3.022	60.017	103	51	12733672
4.98	33.725	67.336	2.139	0.700	0.780	3.650	52.495	111	56	8054076
4.67	34.653	93.781	1.535	0.591	0.642	2.902	60.229	106	53	13353443
4.92	34.789	99.997	1.440	0.570	0.611	2.941	61.049	102	51	13539686
4.42	34.180	77.758	1.852	0.653	0.725	3.043	56.396	115	58	11157501
5.79	32.643	51.743	2.783	0.782	0.859	4.708	44.447	120	60	4465016
4.88	34.361	83.068	1.734	0.632	0.698	3.231	57.949	103	52	11100574
5.50	33.839	69.631	2.068	0.690	0.768	3.957	53.453	99	49	7704841
5.43	33.002	55.954	2.574	0.758	0.838	4.295	46.888	118	59	5451836
5.27	34.382	83.766	1.719	0.629	0.694	3.460	58.132	96	48	10431010
5.26	34.077	75.073	1.918	0.665	0.739	3.650	55.500	99	50	9007524
5.34	33.924	71.463	2.015	0.681	0.758	3.799	54.177	100	50	8245350
4.48	34.500	87.769	1.641	0.613	0.673	2.890	59.087	111	55	12901993
5.42	34.238	79.392	1.814	0.647	0.717	3.654	56.904	94	47	9462526
4.72	34.687	95.230	1.512	0.586	0.635	2.907	60.452	105	53	13430837
4.61	34.325	81.956	1.757	0.636	0.703	3.081	57.647	109	55	11517095
5.09	34.426	85.194	1.690	0.623	0.687	3.318	58.491	99	49	11013603
5.36	34.346	82.600	1.743	0.634	0.700	3.546	57.823	94	47	10069012
5.89	34.542	89.341	1.612	0.607	0.665	3.717	59.419	85	43	10146040
5.68	35.637	195.361	0.737	0.363	0.182	2.147	35.640	407	203	6268891
5.50	33.982	72.784	1.978	0.675	0.751	3.872	54.677	97	48	8239354
4.64	34.597	91.490	1.574	0.600	0.654	2.925	59.835	107	53	13077019
5.60	33.928	71.552	2.013	0.681	0.758	3.970	54.211	96	48	7899973
4.78	33.725	67.324	2.139	0.700	0.780	3.509	52.490	116	58	8376147
4.92	34.089	75.392	1.910	0.664	0.738	3.417	55.611	106	53	9660808
6.31	33.175	58.260	2.472	0.746	0.826	4.881	48.141	99	49	5059435
5.40	33.138	57.750	2.494	0.749	0.829	4.219	47.869	115	58	5786838
5.94	33.494	63.152	2.280	0.721	0.801	4.446	50.600	98	49	6139570
7.06	33.937	71.761	2.007	0.680	0.757	4.957	54.292	76	38	6346152

<b>d<sub>PCC</sub> (mils)</b>	<b>AREA<sub>PCC</sub></b>	<b>Radius of Relative Stiffness, I</b>	<b>L/<sub>est</sub></b>	<b>AF d<sub>o</sub></b>	<b>AF I</b>	<b>Adj d<sub>PCC</sub></b>	<b>Adj I</b>	<b>Dynamic k-Value</b>	<b>Static k-Value</b>	<b>E<sub>PCC</sub></b>
6.97	33.656	66.015	2.181	0.707	0.786	5.091	51.917	81	41	5647397
4.40	34.661	94.105	1.530	0.590	0.641	2.736	60.280	113	56	14191074
5.44	33.142	57.812	2.491	0.748	0.829	4.243	47.902	115	57	5762522
5.01	34.550	89.647	1.606	0.606	0.664	3.180	59.481	99	50	11883576
6.86	33.450	62.424	2.307	0.724	0.805	5.137	50.251	86	43	5240668
4.47	33.539	63.929	2.253	0.717	0.797	3.372	50.967	127	64	8213686
6.02	33.944	71.924	2.002	0.679	0.756	4.245	54.354	89	45	7427609
6.39	33.867	70.221	2.051	0.687	0.765	4.551	53.690	85	43	6758861
5.15	34.293	80.988	1.778	0.640	0.708	3.445	57.375	99	49	10204382
4.27	33.931	71.623	2.011	0.680	0.757	3.066	54.239	124	62	10237910
5.47	33.413	61.830	2.329	0.727	0.808	4.149	49.962	108	54	6413367
5.52	33.504	63.328	2.274	0.720	0.800	4.145	50.684	105	52	6607799
5.47	33.893	70.785	2.034	0.684	0.762	3.905	53.913	98	49	7943446
4.56	34.045	74.280	1.939	0.668	0.743	3.206	55.222	114	57	10152860
6.05	33.705	66.940	2.151	0.702	0.782	4.415	52.324	92	46	6613848
6.18	34.019	73.654	1.955	0.671	0.747	4.308	54.997	86	43	7493852
5.39	34.109	75.884	1.898	0.661	0.735	3.719	55.778	97	48	8930668
3.60	34.458	86.286	1.669	0.619	0.681	2.373	58.752	137	68	15537305
2.98	34.991	111.453	1.292	0.535	0.553	1.719	61.644	171	86	23621202
7.90	33.453	62.475	2.305	0.724	0.805	5.891	50.276	75	37	4574469
6.52	33.624	65.433	2.201	0.710	0.789	4.793	51.657	87	44	5937512
6.99	34.211	78.632	1.831	0.650	0.721	4.695	56.671	74	37	7303899
6.61	33.891	70.743	2.036	0.684	0.762	4.684	53.897	82	41	6616960
5.96	34.095	75.530	1.907	0.663	0.737	4.105	55.658	88	44	8055107
5.84	32.550	50.763	2.837	0.787	0.864	4.782	43.849	121	61	4277734
6.55	33.609	65.151	2.210	0.711	0.791	4.823	51.529	87	44	5871683
5.29	34.017	73.623	1.956	0.671	0.747	3.707	54.985	100	50	8705810
5.85	33.476	62.849	2.291	0.722	0.803	4.393	50.456	100	50	6178694
5.88	33.385	61.386	2.346	0.730	0.810	4.461	49.743	101	51	5912802
5.63	33.826	69.366	2.076	0.691	0.769	4.050	53.345	97	48	7496150
6.50	33.055	56.640	2.542	0.755	0.835	5.081	47.267	98	49	4683887
5.00	34.512	88.237	1.632	0.612	0.671	3.199	59.189	100	50	11697593
5.32	33.008	56.025	2.570	0.758	0.838	4.207	46.928	120	60	5575628
4.00	33.184	58.394	2.466	0.745	0.826	3.158	48.212	152	76	7842044
5.55	33.341	60.704	2.372	0.733	0.814	4.243	49.403	108	54	6131009
7.07	33.463	62.639	2.299	0.723	0.804	5.285	50.355	83	42	5114731
5.48	31.048	39.116	3.681	0.857	0.918	4.899	35.912	176	88	2789997
3.98	33.068	56.811	2.535	0.754	0.834	3.175	47.361	157	78	7525784
5.31	33.745	67.710	2.127	0.699	0.778	3.873	52.655	104	52	7636256
4.60	33.199	58.599	2.457	0.744	0.825	3.593	48.320	133	66	6923710
5.16	34.616	92.258	1.561	0.597	0.650	3.218	59.972	97	48	11938448
5.30	32.567	50.939	2.827	0.786	0.863	4.350	43.957	133	66	4726542
5.50	33.228	59.019	2.440	0.742	0.822	4.256	48.540	111	56	5898665
3.65	33.891	70.739	2.036	0.684	0.762	2.660	53.895	145	72	11652523



**Table B.8. CDOT whitetopping thickness for 20-year traffic prediction (bonded–westbound lane)**

**Colorado DOT Whitetopping Design (AI, Eff, Winter)**

**Bonded Slabs**

E <sub>AC</sub> =	1359867	PCC Poisson=	0.15	Trial Thickness=	3.5
t <sub>Base</sub> =	18	ACC Poisson=	0.35	Joint Spacing=	60
k=	59	Temperature Differential=	1.3	Existing Asphalt Fatigue=	30
E <sub>PCC</sub> =	8000000	N.A.=	6.76	P <sub>AC</sub> =	5.62
MR=	650	le=	80.03	V <sub>V</sub> =	2.74
		L/le=	0.75		

Axle Load, kips	Critical Concrete Stresses and Asphalt Strains					
	Load Induced		Bond Adjustment		Loss of Support Adjustment	
	Stress, psi	Microstrain	Stress, psi	Microstrain	Stress, psi	Microstrain
1	2	3	4	5	6	7
<b>Single Axles</b>						
35	0	16	0	14	0	14
30	0	14	0	12	0	12
26	0	12	0	10	0	10
24	0	11	0	9	0	9
22	0	10	0	8	0	8
20	0	9	0	8	0	8
18	0	8	0	7	0	7
16	0	7	0	6	0	6
12	0	6	0	4	0	4
8	0	4	0	3	0	3
7	0	3	0	2	0	2
3	0	1	0	0	0	0
<b>Tandem Axles</b>						
60	0	11	0	9	0	9
55	0	10	0	8	0	8
50	0	9	0	7	0	7
46	0	8	0	7	0	7
44	0	8	0	6	0	6
42	0	8	0	6	0	6
40	0	7	0	6	0	6
38	0	7	0	5	0	5
36	0	7	0	5	0	5
34	0	6	0	5	0	5
32	0	6	0	4	0	4
30	0	5	0	4	0	4



Axle Load, kips	Expected Repetitions	Concrete Fatigue Analysis			Asphalt Fatigue Analysis		
		Concrete Stress Ratio	Allowable Repetitions, N	Fatigue Percent, %	Asphalt Microstrain	Allowable Repetitions, N	Fatigue Percent, %
1	8	9	10	11	12	13	14
<b>Single Axles</b>						<b>Percent Asphalt Concrete Fatigue Life Previously Consumed:</b>	30
35	0	0.000	Unlimited	0.0	14	3124028745	0.0
30	504	0.000	Unlimited	0.0	12	5350577415	0.0
26	0	0.000	Unlimited	0.0	10	8860815314	0.0
24	3961	0.000	Unlimited	0.0	9	11777318964	0.0
22	11702	0.000	Unlimited	0.0	8	16081514903	0.0
20	38322	0.000	Unlimited	0.0	8	22686533731	0.0
18	79837	0.000	Unlimited	0.0	7	33318461595	0.0
16	242208	0.000	Unlimited	0.0	6	51488771123	0.0
12	1235348	0.000	Unlimited	0.0	4	153757901744	0.0
8	165948	0.000	Unlimited	0.0	3	801040070306	0.0
7	4238911	0.000	Unlimited	0.0	2	1437713259787	0.0
3	12592840	0.000	Unlimited	0.0	0	204079249715264	0.0
<b>Tandem Axles</b>							
60	3589	0.000	Unlimited	0.0	9	13008413080	0.0
55	1794	0.000	Unlimited	0.0	8	17776338428	0.0
50	4988	0.000	Unlimited	0.0	7	25101258217	0.0
46	20709	0.000	Unlimited	0.0	7	34043478927	0.0
44	3590	0.000	Unlimited	0.0	6	40096162605	0.0
42	18149	0.000	Unlimited	0.0	6	47631304468	0.0
40	31109	0.000	Unlimited	0.0	6	57123414634	0.0
38	85463	0.000	Unlimited	0.0	5	69239078323	0.0
36	120720	0.000	Unlimited	0.0	5	84933178420	0.0
34	178092	0.000	Unlimited	0.0	5	105603919524	0.0
32	105799	0.000	Unlimited	0.0	4	133350075146	0.0
30	219452	0.000	Unlimited	0.0	4	171412409753	0.0
		<b>Total Concrete Fatigue, % =</b>		0.0		<b>Total Asphalt Fatigue, % =</b>	30.0

**Table B.9. CDOT whitetopping thickness for 20-year traffic prediction (unbonded–westbound lane)**

**Colorado DOT Whitetopping Design (AI, Eff, Winter)**

**Unbonded Slabs**

$E_{AC}=$	1359867	PCC Poisson=	0.15	Trial Thickness=	4.5
$t_{Base}=$	17.2	ACC Poisson=	0.35	Joint Spacing=	60
$k=$	55	Temperature Differential=	1.3	Existing Asphalt Fatigue=	30
$E_{PCC}=$	11000000	N.A.=	5.73	$P_{AC}=$	5.62
$MR=$	650	$l_e=$	84.50	$V_V=$	2.74
		$L/l_e=$	0.71		

Axle Load, kips	Critical Concrete Stresses and Asphalt Strains					
	Load Induced		Bond Adjustment		Loss of Support Adjustment	
	Stress, psi	Microstrain	Stress, psi	Microstrain	Stress, psi	Microstrain
1	2	3	4	5	6	7
<b>Single Axles</b>						
35	0	11	0	9	0	9
30	0	9	0	7	0	7
26	0	8	0	6	0	6
24	0	7	0	6	0	6
22	0	7	0	5	0	5
20	0	6	0	5	0	5
18	0	5	0	4	0	4
16	0	5	0	4	0	4
12	0	4	0	2	0	2
8	0	2	0	1	0	1
7	0	2	0	1	0	1
3	0	1	0	0	0	0
<b>Tandem Axles</b>						
60	0	7	0	5	0	5
55	0	6	0	5	0	5
50	0	6	0	4	0	4
46	0	5	0	4	0	4
44	0	5	0	4	0	4
42	0	5	0	4	0	4
40	0	5	0	3	0	3
38	0	4	0	3	0	3
36	0	4	0	3	0	3
34	0	4	0	3	0	3
32	0	4	0	3	0	3
30	0	3	0	2	0	2

Axle Load, kips	Expected Repetitions	Concrete Fatigue Analysis			Asphalt Fatigue Analysis		
		Concrete Stress Ratio	Allowable Repetitions, N	Fatigue Percent, %	Asphalt Microstrain	Allowable Repetitions, N	Fatigue Percent, %
1	8	9	10	11	12	13	14
<b>Single Axles</b>						<b>Percent Asphalt Concrete Fatigue Life Previously Consumed:</b>	30
35	0	0.000	Unlimited	0.0	9	14633832218	0.0
30	504	0.000	Unlimited	0.0	7	25535789302	0.0
26	0	0.000	Unlimited	0.0	6	43169566857	0.0
24	3961	0.000	Unlimited	0.0	6	58139449961	0.0
22	11702	0.000	Unlimited	0.0	5	80656316991	0.0
20	38322	0.000	Unlimited	0.0	5	116019342387	0.0
18	79837	0.000	Unlimited	0.0	4	174607551459	0.0
16	242208	0.000	Unlimited	0.0	4	278500568301	0.0
12	1235348	0.000	Unlimited	0.0	2	921675374728	0.0
8	165948	0.000	Unlimited	0.0	1	6163149073697	0.0
7	4238911	0.000	Unlimited	0.0	1	12603091983632	0.0
3	12592840	0.000	Unlimited	0.0	0	1532688097395160000	0.0
<b>Tandem Axles</b>							
60	3589	0.000	Unlimited	0.0	5	70237020288	0.0
55	1794	0.000	Unlimited	0.0	5	97677779973	0.0
50	4988	0.000	Unlimited	0.0	4	140928665922	0.0
46	20709	0.000	Unlimited	0.0	4	195213877531	0.0
44	3590	0.000	Unlimited	0.0	4	232752624218	0.0
42	18149	0.000	Unlimited	0.0	4	280281007652	0.0
40	31109	0.000	Unlimited	0.0	3	341291008049	0.0
38	85463	0.000	Unlimited	0.0	3	420827245651	0.0
36	120720	0.000	Unlimited	0.0	3	526347015451	0.0
34	178092	0.000	Unlimited	0.0	3	669165870853	0.0
32	105799	0.000	Unlimited	0.0	3	866974770469	0.0
30	219452	0.000	Unlimited	0.0	2	1148404600753	0.0
			<b>Total Concrete Fatigue, % =</b>	0.0		<b>Total Asphalt Fatigue, % =</b>	30.0

**Table B.10. PCA whitetopping thickness for 20-year traffic prediction (bonded–westbound lane)**

**PCA Whitetopping Design (AI, Eff, Winter)**

**Bonded Slabs**

$E_{AC}=$	1359867	PCC Poisson=	0.15	Trial Thickness=	3.5
$t_{AC}=$	18	ACC Poisson=	0.35	Joint Spacing=	60
$k=$	59	Temperature Differential=	1.3	Existing Asphalt Fatigue=	30
$E_{PCC}=$	8000000	PCC Coef. Of Thermal Expan. =	5.50E+00	$P_{AC}=$	5.62
$MR=$	650	$NA=$	6.76	$V_V=$	2.47
		$I_e=$	80.03		

Axle Load, kips	Multiplied by LSF	Critical Concrete Stresses and Asphalt Strains					
		Load Induced		Temperature Induced		Total	
		Stress, psi	Microstrain	Stress, psi	Microstrain	Stress, psi	Microstrain
1	2	3	4	5	6	7	8
<b>Single Axles</b>							
35	35	83	8	-10	-1	74	7
30	30	71	7	-10	-1	62	6
26	26	62	6	-10	-1	52	5
24	24	57	5	-10	-1	48	4
22	22	52	5	-10	-1	43	4
20	20	48	5	-10	-1	38	3
18	18	43	4	-10	-1	33	3
16	16	38	4	-10	-1	29	2
12	12	29	3	-10	-1	19	1
8	8	19	2	-10	-1	9	0
7	7	17	2	-10	-1	7	0
3	3	7	1	-10	-1	-2	-1
<b>Tandem Axles</b>							
60	60	102	9	-10	-1	92	8
55	55	93	9	-10	-1	84	7
50	50	85	8	-10	-1	75	7
46	46	78	7	-10	-1	69	6
44	44	75	7	-10	-1	65	6
42	42	71	7	-10	-1	62	5
40	40	68	6	-10	-1	58	5
38	38	65	6	-10	-1	55	5
36	36	61	6	-10	-1	52	4
34	34	58	5	-10	-1	48	4
32	32	54	5	-10	-1	45	4
30	30	51	5	-10	-1	41	3

Axle Load, kips	Expected Repetitions	Concrete Fatigue Analysis			Asphalt Fatigue Analysis		
		Concrete Stress Ratio	Allowable Repetitions, N	Fatigue Percent, %	Asphalt Microstrain	Allowable Repetitions, N	Fatigue Percent, %
1	9	10	11	12	13	14	15
<b>Single Axles</b>							
35	0	0.113	Unlimited	0.0	7	48757385480	0.0
30	471	0.095	Unlimited	0.0	6	90499489286	0.0
26	0	0.081	Unlimited	0.0	5	164089324437	0.0
24	4936	0.073	Unlimited	0.0	4	231335742162	0.0
22	13897	0.066	Unlimited	0.0	4	339478083701	0.0
20	46454	0.059	Unlimited	0.0	3	524074795527	0.0
18	86535	0.051	Unlimited	0.0	3	864379044443	0.0
16	299737	0.044	Unlimited	0.0	2	1559908477896	0.0
12	1547743	0.029	Unlimited	0.0	1	8065905978524	0.0
8	193338	0.015	Unlimited	0.0	0	249705011599240	0.0
7	3211582	0.011	Unlimited	0.0	0	1892371915515730	0.0
3	8759889	-0.004	Unlimited	0.0	-1	Unlimited	0.0
<b>Tandem Axles</b>							
60	4850	0.142	Unlimited	0.0	8	25338906785	0.0
55	2425	0.129	Unlimited	0.0	7	35442606641	0.0
50	6454	0.116	Unlimited	0.0	7	51503249181	0.0
46	18914	0.105	Unlimited	0.0	6	71848696549	0.0
44	4849	0.100	Unlimited	0.0	6	86019204059	0.0
42	24233	0.095	Unlimited	0.0	5	104063423889	0.0
40	42024	0.090	Unlimited	0.0	5	127374781283	0.0
38	113822	0.085	Unlimited	0.0	5	157985530849	0.0
36	162742	0.079	Unlimited	0.0	4	198932460438	0.0
34	237278	0.074	Unlimited	0.0	4	254880603488	0.0
32	137234	0.069	Unlimited	0.0	4	333227565839	0.0
30	277840	0.064	Unlimited	0.0	3	446145141353	0.0
			<b>Total Concrete Fatigue, % =</b>	0.0		<b>Total Asphalt Fatigue, % =</b>	0.0

**Table B.11. PCA whitetopping thickness for 20-year traffic prediction (unbonded–westbound lane)**

**PCA Whitetopping Design (AI, Eff, Winter)**

**Unbonded Slabs**

E <sub>AC</sub> =	1359867	PCC Poisson=	0.15	Trial Thickness=	4.5
t <sub>Base</sub> =	17.2	ACC Poisson=	0.35	Joint Spacing=	60
k=	55	Temperature Differential=	1.3	Existing Asphalt Fatigue=	30
E <sub>PCC</sub> =	11000000	PCC Coef. Of Thermal Expan.=	5.50E+00	P <sub>AC</sub> =	5.62
MR=	650	NA=	5.73	V <sub>V</sub> =	2.74
		I <sub>e</sub> =	84.50		

Axle Load, kips	Multiplied by LSF	Critical Concrete Stresses and Asphalt Strains					
		Load Induced		Temperature Induced		Total	
		Stress, psi	Microstrain	Stress, psi	Microstrain	Stress, psi	Microstrain
1	2	3	4	5	6	7	8
<b>Single Axles</b>							
35	35	77	6	-9	-2	68	4
30	30	66	5	-9	-2	57	3
26	26	57	4	-9	-2	49	2
24	24	53	4	-9	-2	44	2
22	22	49	4	-9	-2	40	2
20	20	44	3	-9	-2	35	1
18	18	40	3	-9	-2	31	1
16	16	35	3	-9	-2	26	1
12	12	27	2	-9	-2	18	0
8	8	18	1	-9	-2	9	-1
7	7	15	1	-9	-2	7	-1
3	3	7	0	-9	-2	-2	-1
<b>Tandem Axles</b>							
60	60	94	7	-9	-2	85	5
55	55	86	7	-9	-2	77	5
50	50	78	6	-9	-2	69	4
46	46	72	6	-9	-2	63	4
44	44	69	5	-9	-2	60	3
42	42	66	5	-9	-2	57	3
40	40	63	5	-9	-2	54	3
38	38	59	5	-9	-2	51	3
36	36	56	4	-9	-2	47	2
34	34	53	4	-9	-2	44	2
32	32	50	4	-9	-2	41	2
30	30	47	4	-9	-2	38	2

Axle Load, kips	Expected Repetitions	Concrete Fatigue Analysis			Asphalt Fatigue Analysis		
		Concrete Stress Ratio	Allowable Repetitions, N	Fatigue Percent, %	Asphalt Microstrain	Allowable Repetitions, N	Fatigue Percent, %
1	9	10	11	12	13	14	15
<b>Single Axles</b>							
35	0	0.105	Unlimited	0.0	4	318114132260	0.0
30	471	0.088	Unlimited	0.0	3	712946565378	0.0
26	0	0.075	Unlimited	0.0	2	1630994471997	0.0
24	4936	0.068	Unlimited	0.0	2	2709818003389	0.0
22	13897	0.061	Unlimited	0.0	2	4940515459044	0.0
20	46454	0.054	Unlimited	0.0	1	10306117833832	0.0
18	86535	0.047	Unlimited	0.0	1	26604723481723	0.0
16	299737	0.041	Unlimited	0.0	1	101374982690248	0.0
12	1547743	0.027	Unlimited	0.0	0	Unlimited	0.0
8	193338	0.014	Unlimited	0.0	-1	Unlimited	0.0
7	3211582	0.010	Unlimited	0.0	-1	Unlimited	0.0
3	8759889	-0.003	Unlimited	0.0	-1	Unlimited	0.0
<b>Tandem Axles</b>							
60	4850	0.131	Unlimited	0.0	5	105731872607	0.0
55	2425	0.119	Unlimited	0.0	5	157742070969	0.0
50	6454	0.107	Unlimited	0.0	4	248758902666	0.0
46	18914	0.097	Unlimited	0.0	4	377123569121	0.0
44	4849	0.092	Unlimited	0.0	3	474458486341	0.0
42	24233	0.087	Unlimited	0.0	3	607291477740	0.0
40	42024	0.083	Unlimited	0.0	3	793041579438	0.0
38	113822	0.078	Unlimited	0.0	3	1060308707898	0.0
36	162742	0.073	Unlimited	0.0	2	1458114757734	0.0
34	237278	0.068	Unlimited	0.0	2	2074912003885	0.0
32	137234	0.063	Unlimited	0.0	2	3080567886888	0.0
30	277840	0.059	Unlimited	0.0	2	4827576637260	0.0
			<b>Total Concrete Fatigue, % =</b>	0.0		<b>Total Asphalt Fatigue, % =</b>	0.0